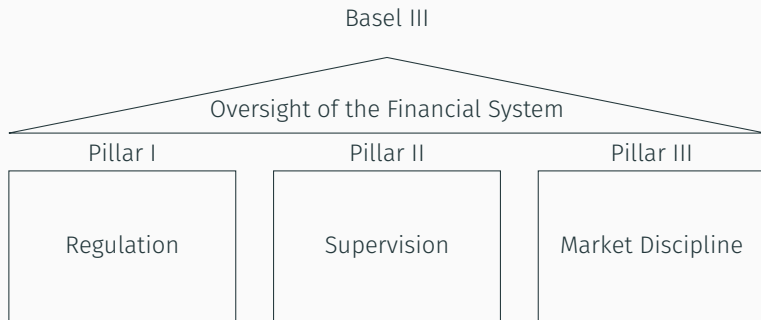
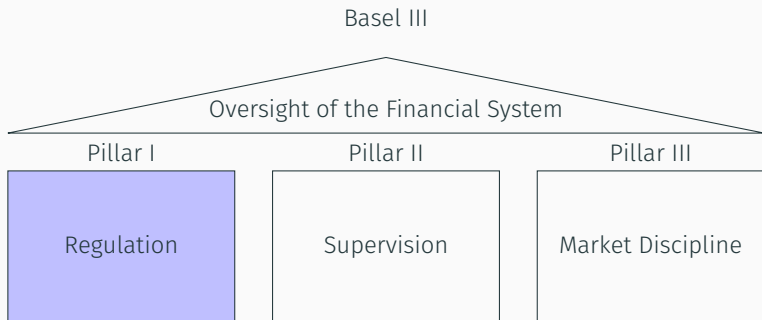


Rules versus Disclosure: Prudential Regulation and Market Discipline

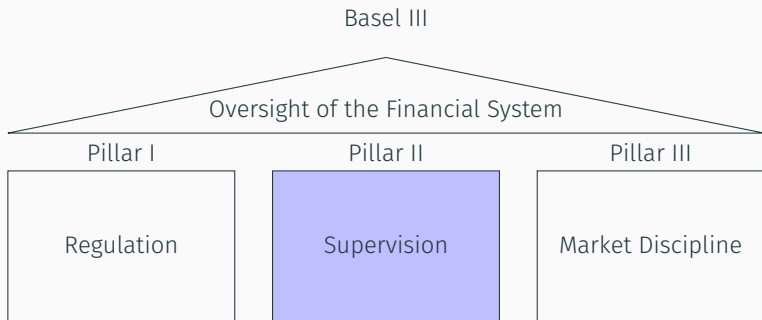
William Fuchs, Satoshi Fukuda, and Daniel Neuhann
Duke University, April 3, 2024

Introduction

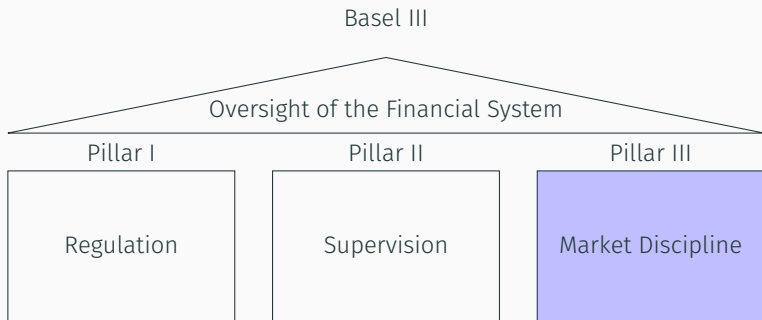




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1. **Regulation:** ex-ante rules regarding operations, incl. risk management.
2. **Supervision** aims to induce sound governance and risk management.
3. **Market Discipline:** disclosure of information to other market participants.

- Limited disclosure may induce moral hazard that requires regulation.
- Effective regulation may allow the regulator to disclose less.

We ask three main questions:

1. What is the optimal disclosure policy if banks can adjust asset quality?
 - Trade-off between ex-post insurance and ex-ante incentives.
2. What is the optimal *joint* design of regulation and disclosure.
 - Rules ensure incentives, but may have excessive “red tape.”
3. To what extent do banks and regulators agree about optimal policy?

A model with bank moral hazard and externalities

Regulator wants high effort, and can induce it using one or both tools.

- Regulation: can directly target effort, but cannot respond to shocks.
- Disclosure: state-contingent, but obfuscation creates moral hazard.

- It is optimal to always use both regulation and (partial) disclosure.
 - ⇒ Rationale for key aspects of Basel III
- Absent regulation, full disclosure can be an optimal policy.
- Absent disclosure, optimal regulation entails “prudential” effort.
 - Dodd-Frank: this is stricter for “systemically important institutions.”
- Optimal disclosure is state-contingent and reduces prudential effort.
- Banks like some regulation, would prefer more disclosure.

- Stress Testing as an information design problem.
 - Gick & Pausch (2012), Spargoli (2012), Morrison & White (2013), Bouvard et al. (2015), Parlatore (2015), Shapiro & Skeie (2015), Dang et al. (2017), Faria-e-Castro et al. (2017), Monnet & Quintin (2017), Williams (2017), Goldstein & Leitner (2018), Leitner & Yilmaz (2019), Alvarez & Barlevy (2021), Huang (2021), Parlasca (2021), Inostroza (2023), Inostroza & Pavan (2023), Leitner & Williams (2023), Orlov et al. (2023), Parlatore & Philippon (2023), Rhee & Dogra (2024), Dai et al. (Forthcoming), Shapiro & Zeng (Forthcoming), Quigley & Walther (Forthcoming).
 - Survey: Goldstein & Sapra (2013), Goldstein & Leitner (2022)
- Interaction between Bank Supervision and Regulation
 - Bhattacharya et al. (2002), Décamps et al. (2004), Eisenbach et al. (2016), Agarwal & Goel (2022)
- Moral hazard and information design
 - Methodology: Rodina & Farragut (2018), Boleslavsky & Kim (2021)
 - Application to Grading: Dubey and Geanakoplos (2010), Boleslavsky & Cotton (2015), Zubrickas (2015)
 - Application to Certification: Albano & Lizzeri (2001), Zapechelnyuk (2022)

Outline

Outline of the Rest of Presentation

- 1 Model
- 2 Benchmarks
- 3 Optimal Disclosure
- 4 Regulation without Disclosure
- 5 Joint Design: Regulation + Disclosure
- 6 Race to the Bottom?

Model

- One bank, two periods.
- Bank first originates assets of uncertain quality and may later sell them.
- The state of the economy: $\theta \sim U([1 - \varepsilon, 1 + \varepsilon])$.
 - ε : Uncertainty of the environment.
- Asset quality depends on bank's privately exerted effort $e \in [0, \frac{1}{2}]$.
- Cost $c(e)$: increasing, convex, $c(0) = c'(0) = 0$, and $c(\frac{1}{2}) = c'(\frac{1}{2}) = \infty$.

▶ Example Cost Functions

- The asset produced by the bank has quality $q \in \{L, H\}$ with

$$\text{Prob}(q = H \mid e) = \theta e.$$

- In the 2nd period, assets can be sold to a competitive fringe of buyers.
- Asset of quality $q \in \{L, H\}$ has value v_q for buyers and ρ_q for sellers.

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Assumption 1: $v_H > \rho_H > \rho_L > v_L$.

- **Externality:** Additional social value $g > 0$ of trading each asset, with

$$v_L + g > \rho_L.$$

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- **Externality:** Additional social value $g > 0$ of trading each asset, with

$$v_L + g > \rho_L.$$

- Potential rationales for this externality:
 - (a) Bank better able to deal with a troubled loan, planner prefers to spread risk.
 - (b) Or, induced preferences from “too big too fail.”

NB: Could also modeled by assuming a richer type space and adverse selection such that low types would not trade in eq.

1. Regulation

- The regulator can set up (before state θ is realized) a system that bounds from below the level of effort (i.e., minimum effort level).

2. Stress test/Disclosure

- Before trades take place, the regulator can conduct a state contingent stress test that publicly reveals some information about each of the assets:

$$\pi_L, \pi_H : [1 - \varepsilon, 1 + \varepsilon] \rightarrow \Delta(\{\ell, h\}).$$

- Information obfuscation ex-post \Rightarrow ex-ante moral hazard: expecting obfuscation, banks are less willing to exert effort.

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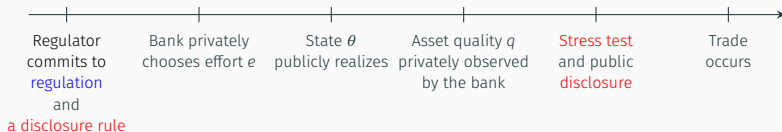
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Benchmarks

1. There is no equilibrium in which trade occurs for sure.
 - The bank would have no incentive to exert any effort, but $v_L < \rho_H$.

No Information (Laissez Faire)

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2. There also does not exist an equilibrium with no trade iff

$$\underbrace{(c')^{-1}(\rho_H - \rho_L)}_{\text{bank effort under no trade}} > \underbrace{\frac{\rho_H - v_L}{v_H - v_L} \frac{1}{1 + \varepsilon}}_{\substack{\text{cutoff effort s.t.} \\ \text{average quality} \leq \rho_H \\ \text{for all } \theta}} .$$

► Details

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► Details

3. Assume this holds, so that trade occurs for some θ but not for others.

1. $\theta^*(e)$: the state at which the *conditional* buyer value given e is ρ_H , i.e.

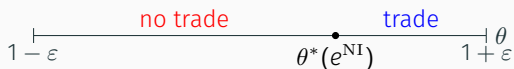
$$\theta^*(e)ev_H + (1 - \theta^*(e)e)v_L = \rho_H.$$

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2. e^* is the effort at which the *unconditional* buyer value is equal to ρ_H ,

$$e^* = \frac{\rho_H - v_L}{v_H - v_L}.$$

No Information Equilibrium (Laissez Faire)

The bank's decision problem is:

$$\max_{e \in [0, \frac{1}{2})} \frac{1}{2\varepsilon} \int_{1-\varepsilon}^{\theta^*(e)} \underbrace{\left(\theta e \rho_H + (1-\theta e) \rho_L \right)}_{\text{asset quality under no trade}} d\theta + \frac{1}{2\varepsilon} \int_{\theta^*(e)}^{1+\varepsilon} \underbrace{\left(\theta e v_H + (1-\theta e^{\text{NI}}) v_L \right)}_{\text{price}} d\theta - c(e).$$

The unique solution e^{NI} is

$$\underbrace{\frac{\rho_H - \rho_L}{4\varepsilon} \left(\left(\frac{e^*}{e^{\text{NI}}} \right)^2 - (1-\varepsilon)^2 \right)}_{\substack{\text{marginal benefit} \\ \text{prob. no trade} \times \text{expected marginal increase in asset quality}}} = \underbrace{c'(e^{\text{NI}})}_{\text{marginal cost}}.$$

1. With full information, there is trade at H and no trade at L . Bank solves:

$$\max_{e \in [0, \frac{1}{2})} \mathbb{E}_\theta \left[\theta e \underbrace{v_H}_{\text{price}} + (1 - \theta e) \rho_L \right] - c(e).$$

2. The solution is

$$e^{\text{FI}} = (c')^{-1}(v_H - \rho_L).$$

- $e^{\text{NI}} < e^{\text{FI}}$: full information provides incentives to exert higher effort.
- $e^{\text{FI}} < (c')^{-1}(v_H - v_L)$: Bad assets do not trade, which is socially inefficient.

Optimal Disclosure

It is optimal to consider policies of the following form:

- After H , the policy reports h with probability 1;
- After L , the policy reports h with probability $\beta(\theta)$.

Hence, $\beta(\theta) = 1$ means no disclosure while $\beta(\theta) = 0$ means full disclosure.

Information Disclosure: Planner's Problem

$$\max_{e, \beta} \frac{1}{2\varepsilon} \int_{1-\varepsilon}^{1+\varepsilon} \left(\underbrace{\theta e}_H \cdot \underbrace{(v_H + g)}_{\text{trade}} + \underbrace{(1 - \theta e)}_L \left(\underbrace{\beta(\theta) (v_L + g)}_{\text{trade}} + \underbrace{(1 - \beta(\theta)) \rho_L}_{\text{no trade}} \right) \right) d\theta - c(e)$$

$$\text{s.t. } \underbrace{p(\theta | e, \beta)}_{\text{Price given } h} := \frac{\theta e \cdot v_H + (1 - \theta e)\beta(\theta)v_L}{\theta e + (1 - \theta e)\beta(\theta)} \geq \rho_H \text{ for each } \theta$$

$$e \in \operatorname{argmax}_{\hat{e} \in [0, \frac{1}{2})} \frac{1}{2\varepsilon} \int_{1-\varepsilon}^{1+\varepsilon} \left(\underbrace{(\theta \hat{e} + (1 - \theta \hat{e})\beta(\theta)) p(\theta | e, \beta)}_{\text{prob. receiving } h} + \underbrace{(1 - \theta \hat{e})(1 - \beta(\theta)) \rho_L}_{\text{prob. receiving } \ell} \right) d\theta - c(\hat{e}).$$

► IC Constraint

Optimal policy trades off ex-post insurance and ex-ante moral hazard.

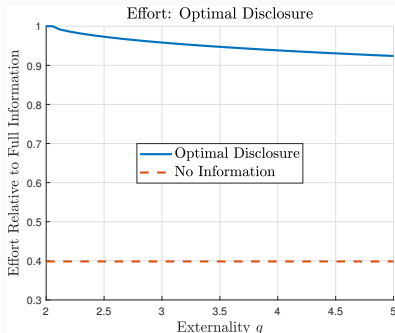
Key properties:

- No disclosure ($\beta = 1$) is never optimal.
- When externality g is low, full disclosure is optimal.
- When externality g is high, partial obfuscation is optimal.
- Disclosure is non-monotone in state θ .

Information Disclosure without Regulation

Proposition

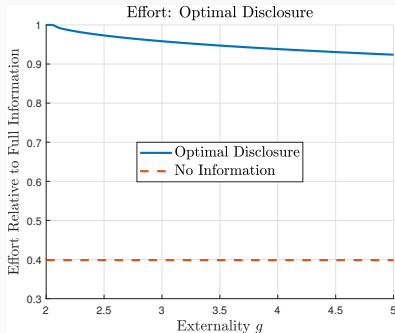
1. There is a \underline{g} such that if $g < \underline{g}$ then full information ($e^{\text{FI}}, \beta = 0$) is optimal.
2. If instead $g > \bar{g}$ then some information obfuscation is optimal:
 $e^{\text{D}} < e^{\text{FI}}$ and $\beta^{\text{D}}(\theta) > 0$ for some θ .



Information Disclosure without Regulation

Intuition: Low g

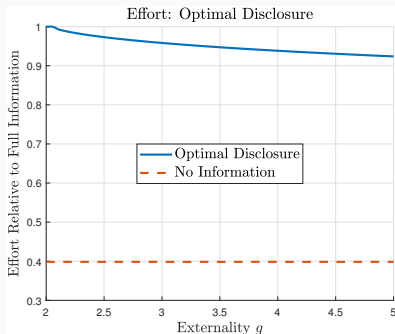
- Cost of moral hazard $>$ Welfare gain from selling bad assets



Information Disclosure without Regulation

Intuition: High g

- Welfare gain from trading bad quality assets increases.
- To ensure trade, engage in more information obfuscation: $\beta \uparrow$.
- To respect incentive compatibility, effort e goes down.



Intuition: High g

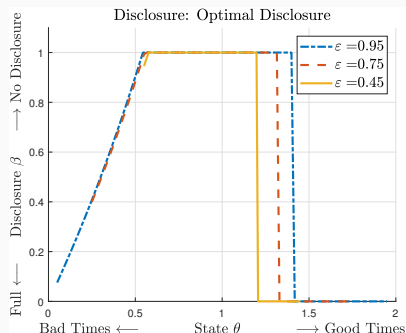
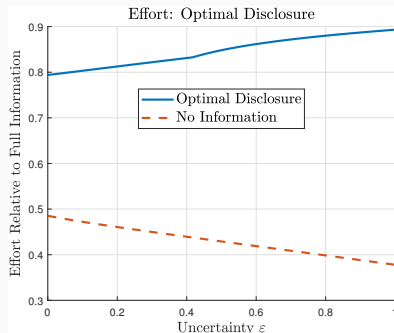
- Welfare gain from trading bad quality assets increases.
- To ensure trade, engage in more information obfuscation: $\beta \uparrow$.
- To respect incentive compatibility, effort e goes down.

High $g \approx$ systemically important financial institutions

- The planner is more opaque about the assets of large institutions.
- As a result, their quality is relatively low.

⇒ **If** regulation can induce effort, then SIFIs should be regulated more tightly.

Effects of Volatility on Optimal Disclosure



- Higher θ : Easier to provide effort incentives through disclosure
- Low θ : Pricing constraint is binding (can't obfuscate too much).

Regulation without Disclosure

- **Assume:** regulator can induce minimum effort through regulation.
- This can address moral hazard but is not state contingent.

- Effort e pins down the set of states for which trade occurs.
- As before, there is a cutoff state $\theta^*(e)$ at which buyer value is ρ_H .



Assume the regulation is binding. Then the planner solves:

$$\begin{aligned} \max_{e \in [0, \frac{1}{2})} \quad & \frac{1}{2\varepsilon} \int_{\theta \leq \theta^*(e)} \underbrace{(\theta e \cdot \rho_H + (1 - \theta e) \rho_L)}_{\text{no trade}} d\theta \\ & + \frac{1}{2\varepsilon} \int_{\theta \geq \theta^*(e)} \underbrace{(\theta e \cdot v_H + (1 - \theta e) v_L + g)}_{\text{trade}} d\theta - c(e). \end{aligned}$$

Regulation without Disclosure: Key Considerations

1. When ε is small, trade occurs for all θ at efficient effort $e = (c')^{-1}(v_H - v_L)$.
2. As ε increases, for a given effort level, there are states θ such that the realized average quality is below ρ_H .



3. Prudential regulation: costly increase in effort to induce more trade.



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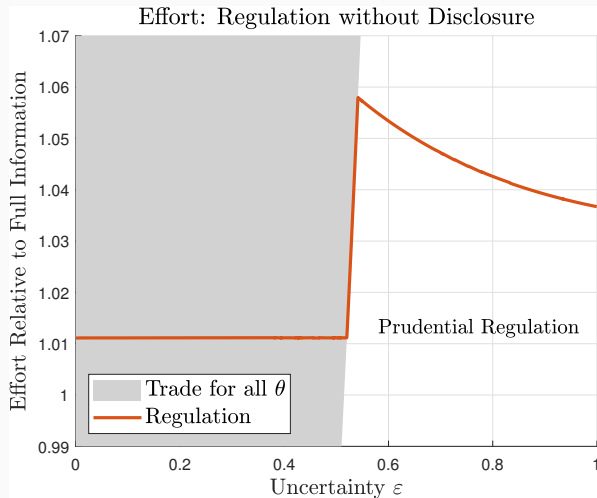
With sufficient volatility, regulator may decide to “give up” on some states.

► Formal Details

Proposition

1. When ε is small, the optimal regulation is the efficient effort level.
2. When ε is intermediate, excess effort (prudential regulation) that ensures trade of all assets is optimal.
3. When ε is high, full insurance is too costly and less prudential regulation to provide partial insurance is optimal.
4. Optimal regulation is increasing in externality g .

Regulation without Disclosure: Optimal Policy



Joint Design: Regulation + Disclosure

Joint Design: Planner's Problem

Idea: regulation deals with the moral hazard, disclosure adapts to the state.

Planner's Problem:

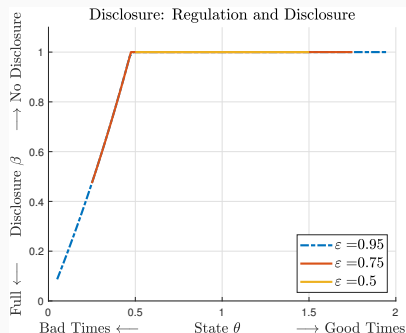
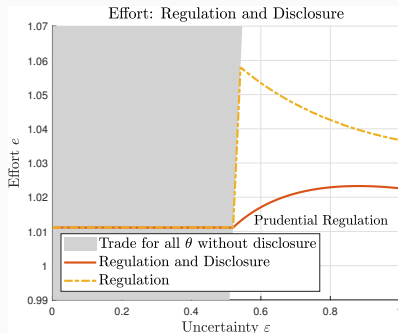
$$\max_{e, \beta} \frac{1}{2\varepsilon} \int_{1-\varepsilon}^{1+\varepsilon} \left(\underbrace{\theta e}_H \cdot \underbrace{(v_H + g)}_{\text{trade}} + \underbrace{(1 - \theta e)}_L \left(\underbrace{\beta(\theta)(v_L + g)}_{\text{trade}} + \underbrace{(1 - \beta(\theta)) \rho_L}_{\text{no trade}} \right) \right) d\theta - c(e)$$

$$\text{s.t. } \underbrace{p(\theta | e, \beta)}_{\text{Price given } h} := \frac{\theta e \cdot v_H + (1 - \theta e)\beta(\theta)v_L}{\theta e + (1 - \theta e)\beta(\theta)} \geq \rho_H \text{ for each } \theta$$

$$e \in \operatorname{argmax}_{\hat{e} \in [0, \frac{1}{2})} \frac{1}{2\varepsilon} \int_{1-\varepsilon}^{1+\varepsilon} ((\theta \hat{e} + (1 - \theta \hat{e})\beta(\theta))p(\theta | e, \beta) + (1 - \theta \hat{e})(1 - \beta(\theta))\rho_L) d\theta - c(\hat{e}).$$

- Regulation and disclosure are substitutes.
 - For two effort levels with $e < e'$, $\beta(e, \theta) < \beta(e', \theta)$ for all θ .
- Information will never be fully disclosed: $\beta(\cdot) > 0$.
- Disclosure always reduces regulation level vis-à-vis no-disclosure.
- Optimal regulation is increasing in externality g .

Optimal Joint Design: Key Properties



► Formal Result

Race to the Bottom?

How Much Regulation do Banks Want?

Basel III is a *framework* that sets minimal standards.

- Implementation is left to a variety of agencies.

This leaves open the possibility of a “race to the bottom.”

How much disclosure and regulation do banks want?

The bank does not care about selling bad assets.

Ex-ante, it would therefore like to commit to full disclosure.

⇒ Obfuscation is only due to the externality.

▶ Details

Bank-Optimal Regulation (No Disclosure)

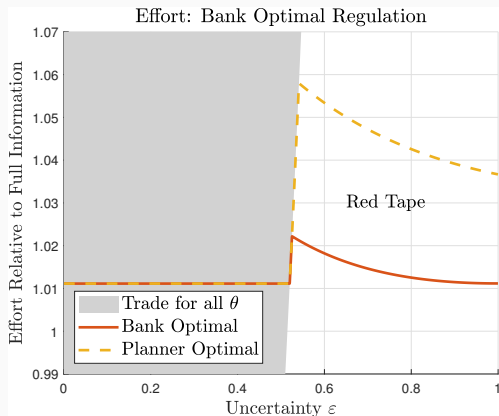
Suppose the bank could commit to some effort e . Trading probabilities are:



The bank's decision problem:

$$\begin{aligned} \max_{e \in [0, \frac{1}{2})} \frac{1}{2\varepsilon} \int_{\theta^*(e) > \theta} & \underbrace{(\theta e \cdot \rho_H + (1 - \theta e)\rho_L)}_{\substack{\text{average quality} \\ \text{under no trade}}} d\theta \\ + \frac{1}{2\varepsilon} \int_{\theta^*(e) \leq \theta} & \underbrace{(\theta e \cdot v_H + (1 - \theta e)v_L)}_{\text{price}} d\theta - c(e). \end{aligned}$$

Bank-Optimal Regulation (No Disclosure)



- The bank would welcome some regulation.
- “Red tape:” difference between optimal and bank-preferred regulation .

► Formal Details

- The bank prefers full disclosure, but the social planner doesn't.
- Under full disclosure, bank perceives no marginal benefit of regulation.

Can Banks fully disclose on their own?

- Maybe using credit ratings, but subject to limited commitment etc.
- Given the planner-optimal disclosure policy, the bank-optimal regulation $<$ the planner optimal regulation (i.e., red tape) for high uncertainty ϵ .

- It is optimal to always use both regulation and information disclosure (obfuscation), even though they are policy substitutes.
 - ⇒ Rationale for Basel III
- Full disclosure can be an optimal disclosure policy absent regulation.
- Optimal regulation entails “excess effort” (prudential regulation).
- Optimal disclosure is state-contingent and reduces excess effort.
- Stricter standards for systemically important (high g) institutions.
 - ⇒ Dodd-Frank Act

Appendix

Examples of Cost Functions

- $c(e) = -k(2e + \log(1 - 2e))$.

- $c(e) = \frac{ke^2}{1-2e}$.

▶ Back

No Information Benchmark: No Trade

- The bank's effort solves:

$$\mathbb{E}[\theta e \rho_H + (1 - \theta e) \rho_L] - c(e).$$

- \Rightarrow The bank's equilibrium effort:

$$(c')^{-1}(\rho_H - \rho_L).$$

- The bank would be tempted to trade if the average quality of the asset is as high as ρ_H for some θ .
- Cutoff state $\theta^*(e)$ at which the average quality is ρ_H :

$$\theta^*(e) e v_H + (1 - \theta^*(e) e) v_L = \rho_H$$

$$\Rightarrow \theta^*(e) = \frac{e^*}{e}, \text{ where } e^* = \frac{\rho_H - v_L}{v_H - v_L}.$$

- The bank would be tempted to trade for some θ if and only if

$$(c')^{-1}(\rho_H - \rho_L) > \frac{\rho_H - v_L}{v_H - v_L} \frac{1}{1 + \varepsilon}.$$

Lemma

The bank's IC constraint can be replaced with its first-order condition:

$$\frac{1}{2\varepsilon} \int_{1-\varepsilon}^{1+\varepsilon} \theta(1 - \beta(\theta))(p(\theta | e, \beta) - \rho_L)d\theta = c'(e).$$

Regulation

- Given an effort level e , there exists a unique cutoff $\theta^*(e)$ such that the average quality

$$\theta e v_H + (1 - \theta e) v_L$$

is at least as high as ρ_H if and only if $\theta \geq \theta^*(e)$.

- Thus:

$$\theta^*(e) = \frac{e^*}{e}.$$

- Given a minimal effort level e (which is binding),
 - no trade occurs if $\theta < \theta^*(e)$;
 - trade occurs if $\theta \geq \theta^*(e)$.
- The planner would choose e to maximize welfare.

The planner's problem:

$$\begin{aligned} \max_{e \in [0, \frac{1}{2})} & \frac{1}{2\varepsilon} \int_{1-\varepsilon}^{\text{med}(1-\varepsilon, \theta^*(e), 1+\varepsilon)} (\theta e \rho_H + (1 - \theta e) \rho_L) d\theta \\ & + \frac{1}{2\varepsilon} \int_{\text{med}(1-\varepsilon, \theta^*(e), 1+\varepsilon)}^{1+\varepsilon} (\theta e v_H + (1 - \theta e) v_L + g) d\theta - c(e). \end{aligned}$$

Proposition

The optimal process regulation is uniquely given by:

$$e^R = \begin{cases} e^\diamond & \text{if } \varepsilon \leq 1 - \frac{e^*}{e^\diamond} \\ \min\left(e^\dagger, \frac{e^*}{1-\varepsilon}\right) & \text{if } \varepsilon \geq 1 - \frac{e^*}{e^\diamond} \end{cases},$$

where $e^\dagger \in (e^\diamond, \frac{1}{2})$ is a unique solution $e \in (0, \frac{1}{2})$ satisfying

$$\left(\frac{v_H - v_L}{2}(1 + \varepsilon)^2 - \frac{\rho_H - \rho_L}{2}(1 - \varepsilon)^2\right) + \left(\frac{v_H - \rho_H + \rho_L - v_L}{2}e^* + (v_L + g - \rho_L)\right) \frac{e^*}{e^2} = 2\varepsilon c'(e)$$

and

$$e^\diamond = (c')^{-1}(v_H - v_L).$$

- Information Disclosure
 - After H , the policy reports h with probability 1;
 - After L , the policy reports h with probability $\beta(\theta)$.

- The planner would choose each $\beta(\theta)$ so that:
 - the average quality is ρ_H if $\theta < \theta^*(e)$:

$$\frac{\theta e v_H + (1 - \theta e) \beta(\theta) v_L}{\theta e + (1 - \theta e) \beta(\theta)} = \rho_H;$$

- $\beta(\theta) = 1$ (no disclosure) if $\theta \geq \theta^*(e)$.

Regulation and Information Disclosure

- The planner's problem is:

$$\max_{e \in [0, \frac{1}{2})} \frac{1}{2\varepsilon} \int_{1-\varepsilon}^{1+\varepsilon} (\theta e(v_H + g) + (1 - \theta e)(\beta(\theta)(v_L + g) + (1 - \beta(\theta))\rho_L)) d\theta - c(e).$$

- The optimal disclosure policy (given e) is:

$$\beta(\theta) = \begin{cases} \frac{v_H - \rho_H}{\rho_H - v_L} \frac{\theta e}{1 - \theta e} & \text{if } \theta \leq \theta^*(e) \\ 1 & \text{if } \theta \geq \theta^*(e) \end{cases}.$$

- After algebra, the planner's problem is:

$$\begin{aligned} \max_{e \in [0, \frac{1}{2})} \frac{1}{2\varepsilon} \int_{1-\varepsilon}^{\text{med}(1-\varepsilon, \theta^*(e), 1+\varepsilon)} \left(\frac{e\theta}{e^*}(\rho_H + g) + \left(1 - \frac{e\theta}{e^*}\right)\rho_L \right) d\theta \\ + \frac{1}{2\varepsilon} \int_{\text{med}(1-\varepsilon, \theta^*(e), 1+\varepsilon)}^{1+\varepsilon} (\theta e v_H + (1 - \theta e)v_L + g) d\theta - c(e). \end{aligned}$$

Proposition

The optimal regulation (with disclosure) is uniquely given by:

$$e^{\text{RD}} = \begin{cases} e^\diamond & \text{if } \varepsilon \leq 1 - \frac{e^*}{e^\diamond} \\ e^\ddagger & \text{if } \varepsilon \geq 1 - \frac{e^*}{e^\diamond} \end{cases},$$

where $e^\ddagger \in \left(e^\diamond, \frac{e^*}{1-\varepsilon}\right)$ is a unique solution $e \in (0, 1)$ satisfying

$$\frac{v_H - v_L}{2}(1 + \varepsilon)^2 - \frac{\rho_H - \rho_L + g}{2e^*}(1 - \varepsilon)^2 + \frac{v_L + g - \rho_L}{2} \frac{e^*}{e^2} = 2\varepsilon c'(e)$$

and

$$e^\diamond = (c')^{-1}(v_H - v_L).$$

The Bank's Problem

$$\max_{e, \beta} \frac{1}{2\varepsilon} \int_{1-\varepsilon}^{1+\varepsilon} \left(\underbrace{\theta e}_{H} \cdot \underbrace{v_H}_{\text{trade}} + \underbrace{(1 - \theta e)}_L \left(\beta(\theta) \underbrace{v_L}_{\text{trade}} + (1 - \beta(\theta)) \underbrace{\rho_L}_{\text{no trade}} \right) \right) d\theta - c(e)$$

s.t. $\underbrace{p(\theta | e, \beta)}_{\text{Price given } h} := \frac{\theta e \cdot v_H + (1 - \theta e)\beta(\theta)v_L}{\theta e + (1 - \theta e)\beta(\theta)} \geq \rho_H \text{ for each } \theta.$

Proposition

A unique solution e^{BO} exists and satisfies the following:

$$e^{\text{BO}} = \begin{cases} e^{\text{FB}} & \text{if } \varepsilon \leq 1 - \frac{e^*}{e^{\text{FB}}} \\ \min\left(e^{\circ}, \frac{e^*}{1-\varepsilon}\right) & \text{if } \varepsilon > 1 - \frac{e^*}{e^{\text{FB}}} \end{cases},$$

where e° is a unique solution $e \in \left(\frac{e^*}{1+\varepsilon}, \frac{1}{2}\right)$ such that

$$\frac{v_H - v_L}{4\varepsilon} (1 + \varepsilon)^2 - \frac{\rho_H - \rho_L}{4\varepsilon} (1 - \varepsilon)^2 + \frac{1}{4\varepsilon} \frac{e^*}{e^2} \left(\frac{v_H - \rho_H}{v_H - v_L} - (\rho_L - v_L) \right) = c'(e).$$