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**Ruiz-Alsop, Rosa Nery**

**EFFECT OF RELATIVE HUMIDITY AND ADDITIVES ON THE REACTION OF  
SULFUR DIOXIDE WITH CALCIUM HYDROXIDE**

*The University of Texas at Austin*

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**EFFECT OF RELATIVE HUMIDITY AND ADDITIVES  
ON THE REACTION OF SULFUR DIOXIDE  
WITH CALCIUM HYDROXIDE**

by

**ROSA NERY RUIZ-ALSOP, B.S., M.S.**

**DISSERTATION**

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August, 1986

**EFFECT OF RELATIVE HUMIDITY AND ADDITIVES  
ON THE REACTION OF SULFUR DIOXIDE  
WITH CALCIUM HYDROXIDE**

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**To Chuck**

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Rosa Ruiz-Alsop

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## Chapter 1

### Project Summary

#### 1.1 Abstract

Previous results with flue gas desulfurization by spray drying of  $\text{Ca}(\text{OH})_2$  show that a significant amount of  $\text{SO}_2$  removal occurs in the bag filters used to collect the solids. This research program investigates the reaction of  $\text{SO}_2$  with  $\text{Ca}(\text{OH})_2$  at conditions similar to those of commercial scale bag filters, 19 to 74% relative humidity, 30.4 to 95°C, and 300 to 4000 ppm  $\text{SO}_2$ . The study was carried out in a bench scale fixed bed reactor, with powder reagent  $\text{Ca}(\text{OH})_2$  dispersed in silica sand. The gas phase was a mixture of  $\text{N}_2$ ,  $\text{SO}_2$ , and water vapor. The effect of  $\text{Ca}(\text{OH})_2$  loading, temperature, relative humidity, inlet  $\text{SO}_2$  concentration, and additives were investigated. Of the additives tried (buffers acids, organic deliquescents, and inorganic deliquescents) only the deliquescent salts improved  $\text{Ca}(\text{OH})_2$  reactivity towards  $\text{SO}_2$ . The improvement depends on the type and amount of salt and on the relative humidity. The experimental data was modelled by a shrinking core model with zero order kinetics in  $\text{SO}_2$ , using an empirical correlation to account for shape and surface roughness of the  $\text{Ca}(\text{OH})_2$  particles. The diffusion coefficient of the  $\text{SO}_2$  through the product layer ( $D_p$ ) increases linearly with relative humidity and amount of additive, and the kinetic rate constant ( $k_p$ ) increases exponentially with relative

humidity and amount of additive.  $D_e$  values ranging from  $0.75E-9$  to  $1.20E-6$  ( $\text{cm}^2/\text{s}$ ) and  $k_g$  values ranging from  $1.0E-9$  to  $8.23E-9$  ( $\text{cm}^4/\text{gmol s}$ ) simulated the experimental results.

## 1.2 Introduction

Flue gas desulfurization by spray drying of  $\text{Ca}(\text{OH})_2$  slurry has become increasingly important in recent years as an alternative to the more traditional wet lime or limestone scrubbing. During spray drying, the  $\text{SO}_2$  containing flue gas is contacted in the dryer with a finely atomized aqueous solution or slurry of an alkali (typically slaked lime or soda ash), which absorbs and neutralizes the  $\text{SO}_2$ . Simultaneously, the water is evaporated from the slurry droplets leaving a solid material which can be collected using conventional solids collection equipment such as bag filters or electrostatic precipitators. Bag filters are the preferred collection equipment, because the unreacted  $\text{Ca}(\text{OH})_2$  present in the solids reacts with  $\text{SO}_2$  in the bag filters, thus producing additional  $\text{SO}_2$  removal (Kelly and Dickerman, 1981, Kelly et al., 1983, Stevens, 1981, Samuel et al., 1983, Samuel et al., 1984, Bresowar et al., 1981, Blythe and Rhudy, 1984). The reaction between lime solids and  $\text{SO}_2$  taking place in the ducts and bag filters of a spray dryer system is the subject of the present research.

Most of the information available in the literature for this reaction is reported results of  $\text{SO}_2$  removal across the bag filters of pilot and demonstration spray dryer plants (Blythe and Rhudy, 1984, Bresowar et al., 1981, Samuel et al., 1984, Yeh et al., 1983, Jankura et al., 1984, Lewis and Gehri, 1983, Parsons et al., 1981, Robards et al., 1985, Kelly et al., 1983, Gustke et al., 1984, Donnelly et al., 1985). These results are difficult to interpret, because the conditions of the flue

gas entering the bag filters will be dependent on the spray absorber behavior. Any variable changes that affect the SO<sub>2</sub> removal across the spray absorber will change the concentration of SO<sub>2</sub> entering the bag filters. Therefore, two variables will have effectively been changed in the bag filters and the contribution of each one can not be isolated.

Two bench scale studies regarding the reaction of interest have been reported, one at the Lund Institute of Technology-Sweden (Klingspor, Karlsson, and Bjerle, 1983, 1984) and one at EPA (Acurex, 1985, Jorgensen et al., 1986). However, the characterization of this reaction is far from complete.

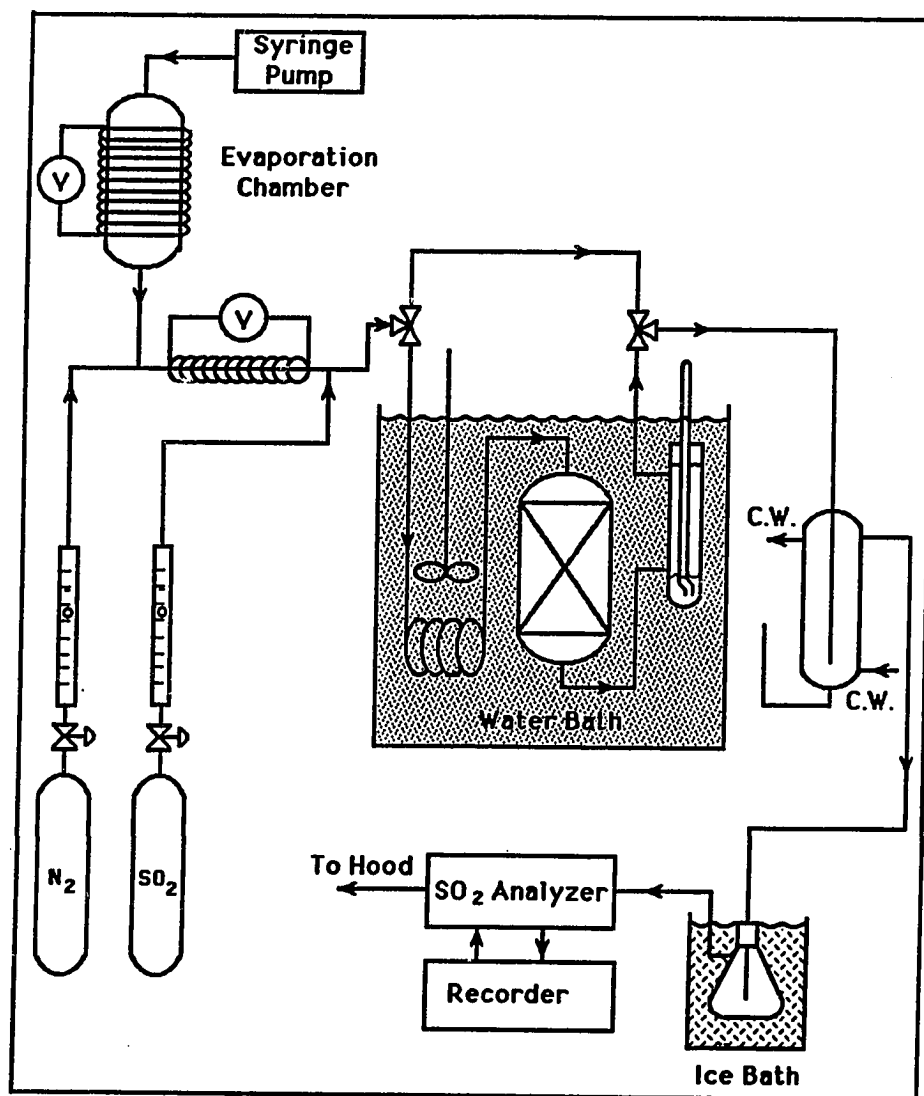
The present study was carried out in a bench scale fixed bed reactor, operated at conditions similar to those found in bag filters of commercial spray drying systems, and using powder reagent Ca(OH)<sub>2</sub> as the sorbent. The effect of Ca(OH)<sub>2</sub> loading, temperature, SO<sub>2</sub> concentration, and relative humidity was studied. Also, additives that improve the lime reactivity towards SO<sub>2</sub> were identified.

### **1.3 Experimental Methods**

#### **1.3.1 Apparatus**

The general design of the experimental apparatus is given in Figure 1-1. A simulated flue gas was synthesized by combining nitrogen and sulfur dioxide from gas cylinders. The gas flow rates were measured using rotameters. Water was added to the system by means of a syringe pump (Sage Instruments, Model 341A) and evaporated at 120°C in a stainless steel evaporation chamber before mixing with the gas stream.

The reactor was made of glass, and it had a diameter of 4 cm and 12 cm height. The reactor was packed with a mixture of silica sand and  $\text{Ca}(\text{OH})_2$  reactant in a weight ratio of 40:1. The addition of sand is necessary to avoid channeling caused by lime agglomeration (Karlsson et al., 1983). The silica sand (between 80 and 115 mesh) was obtained from Martin Marietta Aggregates.



**Figure 1-1: Experimental Apparatus**

The reactor was immersed in a water bath that maintained the system temperature within 0.1°C. Tubing upstream from the reactor was heated to prevent the condensation of moisture on the walls. Before going to analysis the gas was cooled and the water then condensed out by cooling water and an ice bath. The gas was analyzed for SO<sub>2</sub> using a pulsed fluorescent SO<sub>2</sub> analyzer (Thermoelectron Corporation model 40) and the concentration was continuously recorded. The SO<sub>2</sub> analyzer was calibrated using a calibration standard (a mixture of 2000 ppm SO<sub>2</sub> and N<sub>2</sub>). The reactor was equipped with a bypass, to allow the bed to be preconditioned and to allow the gas flow to be stabilized at the desired SO<sub>2</sub> concentration before beginning the experimental run. Prior to each experimental run the bed was humidified by flushing with pure nitrogen at a relative humidity of about 98% for 10 minutes then later with pure nitrogen at the relative humidity at which the experiment was to be performed for 8 minutes. This was done to simulate the moisture conditions encountered in the bag filters where the solids are originally slurry droplets.

The reaction time was normally 1 hour. The raw data from each experimental run was a curve of SO<sub>2</sub> concentration leaving the reactor versus time. This curve was given by the recorder of the SO<sub>2</sub> analyzer.

### 1.3.2 Analysis of the Experimental Data

The raw data from the experiments was SO<sub>2</sub> concentration from the reactor as a function of time. By integration of the SO<sub>2</sub> concentration over time and a mass balance on the reactor the average fraction of Ca(OH)<sub>2</sub> converted was calculated at each time. As a backup, the reacted solids are analyzed for sulfite and hydroxide using acid/base and iodine titrations.

### 1.3.3 Reagent Used

Most of the experimental work was done using reagent grade  $\text{Ca(OH)}_2$  as a reactant. Two batches of  $\text{Ca(OH)}_2$  that will be identified as lime 0 and lime A were used. These two batches of  $\text{Ca(OH)}_2$  differ slightly in particle size and BET surface area as shown in Table 1-1.

**Table 1-1: Particle Size and BET Surface Area of Reactant**

Reactant	Coulter Counter Median Particle Size ( $\mu\text{m}$ )	BET Surface Area ( $\text{m}^2/\text{g}$ )
lime 0	7.4	8.2
lime A	5.6	9.4
lime A (slurried)	-	8.8

The BET surface area of a sample of 1 g of  $\text{Ca(OH)}_2$  A, after slurrying with 5 ml of distilled water and drying at  $75^\circ\text{C}$  is also shown in Table 1-1. The slurrying and drying process caused a slight decrease in the surface area of  $\text{Ca(OH)}_2$ .

### 1.3.4 Preparation of the Samples with Additives

An aqueous solution containing the desired additive was prepared. Five ml of this solution were then added to 1 g of  $\text{Ca(OH)}_2$  and slurried. The sample was placed in an oven to dry at  $75^\circ\text{C}$  for about 14 hours then later sieved to separate the individual  $\text{Ca(OH)}_2$  particles prior to mixing with the silica sand and being placed in the reactor.

### 1.4 Model

The equations that describe the absorption of a component from a moving gas stream by a fixed solid in a packed bed consist of two partial differential equations obtained from material balances in the gaseous and solid phases. Assuming that the concentration of  $\text{SO}_2$  in the gas phase does not change rapidly with time at a given point (von Rosenberg et al., 1977), the time derivative of the  $\text{SO}_2$  concentration can be neglected and the mass balances lead to the following equations:

$$\frac{V_m dC_{\text{SO}_2}}{A dz} = r_{\text{SO}_2} \quad (1.1)$$

$$\frac{dC_{\text{lime}}}{dt} = r_{\text{SO}_2} \quad (1.2)$$

with boundary and initial conditions:

$$\text{At } z = 0 \quad C_{\text{SO}_2} = C_{\text{SO}_2}^o \quad (1.3)$$

$$\text{At } t = 0 \quad C_{\text{lime}} = C_{\text{lime}}^o$$

Where:

$C_{\text{SO}_2}$  = concentration of  $\text{SO}_2$  in the gas phase ( $\text{gmol}/\text{cm}^3$ )

$V_m$  = volumetric flow rate of gas ( $\text{cm}^3/\text{sec}$ )

$A$  = cross sectional area of the reactor ( $\text{cm}^2$ )

$z$  = length of the reactor (cm)

$C_{\text{lime}}$  =  $\text{Ca}(\text{OH})_2$  concentration ( $\text{gmol}/\text{cm}^3$ )

$t$  = time (sec)

$r_{\text{SO}_2}$  = rate of disappearance of  $\text{SO}_2$  ( $\text{gmol}/\text{cm}^3 \text{ sec}$ )

the rate expression  $r_{\text{SO}_2}$  will depend on the model selected to represent the kinetics of the reaction.

A shrinking core model with kinetics of zero order in  $\text{SO}_2$  was chosen to fit the experimental data. The shrinking core model or unreacted core model assumes that the reaction takes place at the exterior surface of the particle. As the reaction proceeds the surface of reaction will move into the interior of the solid leaving behind a layer of inert product. The external radius of the particle remains the same, this assumes no shrinkage or swelling of the product layer.

The shrinking core model was originally developed by Yagi and Kunii (1961) for the isothermal reaction of spherical solid particles. The  $\text{Ca}(\text{OH})_2$  particles are non-spherical and have a rough surface, so their surface area is much higher than that of spherical particles of the same volume. An empirical expression was introduced to account for the decrease in roughness as the reaction progress. A roughness parameter was defined as:

$$\sigma = \frac{A}{A_\phi} \quad (1.4)$$

Where:

$A$  = actual surface area of the lime

$A_\phi$  = surface area of spherical particles of equal volume

When the lime is unreacted,  $\sigma$  can be estimated as the ratio of the BET surface area of the lime and the surface area calculated from the Coulter Counter particle size distribution assuming spherical particles. As

the reaction progresses  $\sigma$  should decrease and approach the limit  $\sigma = 1.0$  when all the lime has reacted.

An empirical expression of the form:

$$\sigma = 1.0 + \exp(aX_{\text{lime}} + b) \quad (1.5)$$

where  $X_{\text{lime}}$  is the fraction of lime unreacted, was used to describe the change of roughness with the reaction. Equation (1.5) must satisfy the condition:

$$\text{at } X_{\text{lime}} = 1.0 \quad \sigma = \sigma_o = \text{BET area}/A_\phi \quad (1.6)$$

To force  $\sigma$  to decrease more rapidly at high values of  $X_{\text{lime}}$  and to simulate the experimental results, an additional condition was incorporated:

$$\text{at } X_{\text{lime}} = 0.8 \quad \sigma = 2.0 \quad (1.7)$$

For the two batches of  $\text{Ca}(\text{OH})_2$  used in the experiments, namely lime 0 and lime A which differ slightly in surface area and particle size, the constants  $a$  and  $b$  in equation (1.5) took slightly different values.

After introducing the roughness parameter  $\sigma$  the following equations can be obtained for the cases when chemical reaction, or  $\text{SO}_2$  diffusion through the gas film and product layer are the controlling steps.

$$r_{\text{SO}_2} = \frac{1}{V} 4\pi R^2 N \sigma \rho_{\text{lime}} k_s X_{\text{lime}}^{2/3} \quad (1.8)$$

$$r_{\text{SO}_2} = \frac{1}{V} \frac{C_{\text{SO}_2}^g}{\frac{X_{\text{lime}}^{-1/3} - 1}{4\pi D_e N R (\sigma\sigma_o)^{1/2}} + \frac{1}{4\pi R^2 k_s N \sigma_o}} \quad (1.9)$$

where:

$k_g$  = mass transfer coefficient (cm/sec)

$D_e$  = diffusivity of  $\text{SO}_2$  through product ( $\text{cm}^2/\text{sec}$ )

$k_s$  = kinetic rate constant ( $\text{cm}^4/\text{gmol sec}$ )

$\rho_{\text{lime}}$  =  $\text{Ca}(\text{OH})_2$  molar density ( $\text{gmol}/\text{cm}^3$ )

$N$  = number of  $\text{Ca}(\text{OH})_2$  particles

$R$  = Radius of the particle (cm)

$V$  = reactor volume ( $\text{cm}^3$ )

$C_{\text{SO}_2}^g$  =  $\text{SO}_2$  concentration at the gas bulk ( $\text{gmol}/\text{cm}^3$ )

If the chemical reaction is slow, the rate of disappearance of  $\text{SO}_2$  will be given by equation (1.8). If the chemical reaction is fast, all of the  $\text{SO}_2$  that reaches the surface of the core will be immediately consumed and the concentration of the  $\text{SO}_2$  at the surface of the unreacted core will become zero. At these conditions the rate of diffusion of the  $\text{SO}_2$  through the gas film and product layer will become the limiting steps, and equation (1.9) will become important.

Of equations (1.8) and (1.9), the one that gives the lowest rate of  $\text{SO}_2$  disappearance will determine the overall kinetic rate. The

parameters of the model are  $k_g$ ,  $D_e$ , and  $k_s$ . The integration assumed an average particle size which gave the same surface area as the measured particle size distribution assuming spherical particles. The mass transfer coefficient,  $k_g$  was not used as an adjustable parameter because at the conditions at which the experiments were performed, gas film diffusion is not likely to be important. The only effect of gas film diffusion is that it provides a limit to the rate expression (1.9) at the beginning of the reaction where product layer resistance is zero as there is no product formed. The value of  $k_g$  (544 cm/sec) was estimated using a Sherwood number of 2 corresponding to mass transfer from spherical particles in a stagnant fluid (Sherwood et al., 1975).

Thus  $D_e$  and  $k_s$  were the only parameters used to fit the experimental data. Depending on whether mass transfer or chemical reaction is the controlling step, only one of these parameters may be important.

A computer program with variable step size in time and in distance along the reactor was written to model the reaction. This computer program uses the IMSL integration routine DGEAR to carry out the integration, and the IMSL interpolation routine ICSCCU to provide interpolated values of lime conversion needed for each time integration step.

## 1.5 Results

The effects of relative humidity, temperature, inlet  $\text{SO}_2$  concentration, and amount of lime in the reactor on the reaction of  $\text{SO}_2$  with powdered reagent  $\text{Ca}(\text{OH})_2$  were studied. The experimental conditions are listed in Table 1-2.

**Table 1-2: Experimental Conditions**

Relative Humidity:	17 - 90%
$\text{SO}_2$ Inlet Concentration:	500 - 4000 ppm
Reactor Temperature:	30.5 - 95°C
Nitrogen Flow Rate:	4600 $\text{cm}^3/\text{min}$ (0°C, 1 atm)
Amount of Lime:	1.0 - 4.0 g

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### 1.5.1 Effect of Relative Humidity

Relative humidity was found to have a dramatic effect on the rate of reaction of  $\text{SO}_2$  with  $\text{Ca}(\text{OH})_2$  as illustrated by Figure 1-2. The full lines correspond to experimental results at 2000 ppm inlet  $\text{SO}_2$  and 66°C using 4 g of lime 0. Figure 1-2 shows that for all relative humidities, 100% of the  $\text{SO}_2$  is removed during the first one or two minutes of reaction, then the reaction rate decreases quickly at low relative humidities but slower at high relative humidities.

The broken lines in Figure 1-2 correspond to the model prediction for these experiments. Figure 1-3 shows the dependence of the rate constant and solid diffusion coefficient on relative humidity. At

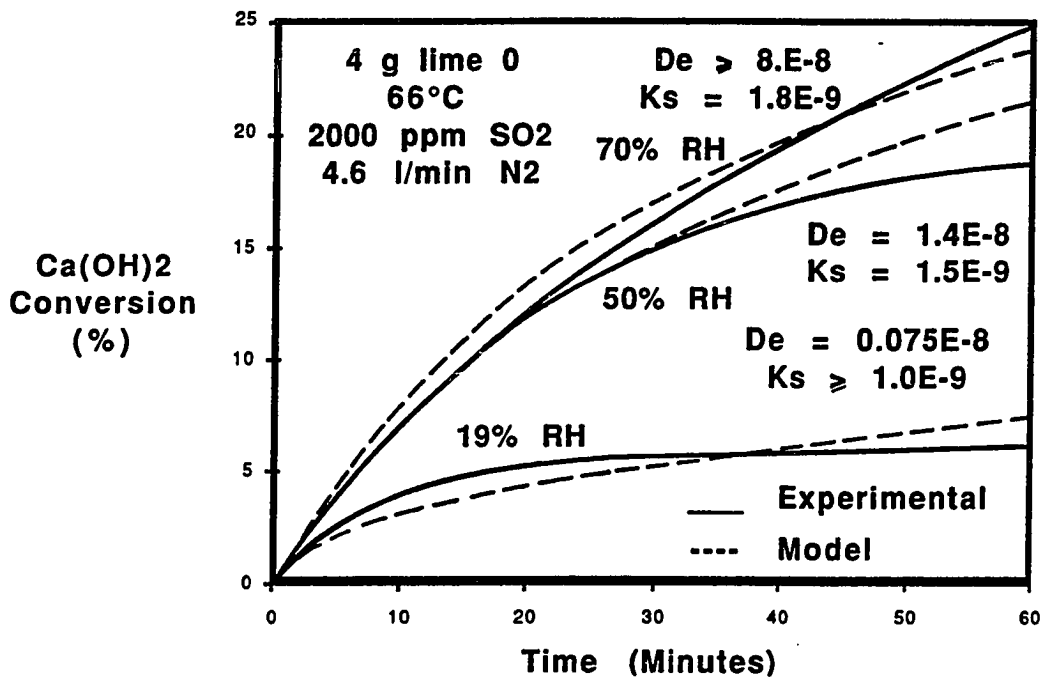


Figure 1-2: Effect of Relative Humidity on Reaction Rate, Lime 0

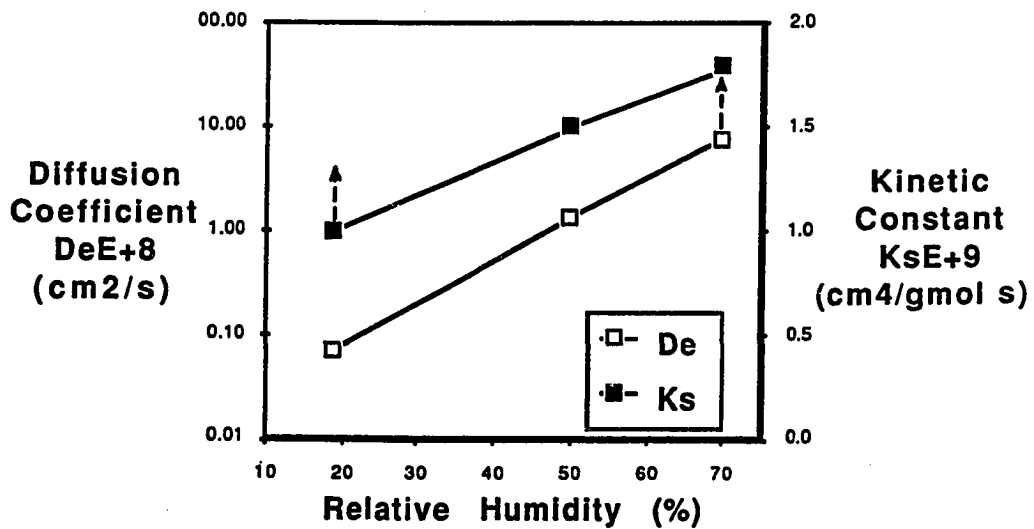


Figure 1-3: Effect of Relative Humidity on Model Parameters

high relative humidity the chemical reaction is the controlling step and  $k_s$  is the parameter that determines the rate of reaction. Any value of  $D_e$  greater than  $8.0E-8$   $\text{cm}^2/\text{sec}$  will give essentially the same result.  $\text{SO}_2$  diffusion through the product layer becomes more important as the relative humidity decreases. At 19% relative humidity  $D_e$  is the parameter that determines the rate of adsorption of  $\text{SO}_2$ . At 19% relative humidity any value of  $k_s$  greater than  $1.0E-9$   $\text{cm}^4/(\text{gmol sec})$  will give essentially the same results. Both  $D_e$  and  $k_s$  are affected by the relative humidity, but in the range of relative humidities studied  $k_s$  increases approximately linearly while  $D_e$  increases exponentially. Because the  $\text{SO}_2$  diffusion coefficient changes more rapidly than the kinetic constant, a change in the controlling mechanism occurs when the relative humidity is increased. The strong effect of relative humidity on reaction rate has also been reported by other researchers (Klingspor et al., 1984, Jorgensen et al., 1986).

### 1.5.2 Effect of Inlet $\text{SO}_2$ concentration

The effect of the inlet  $\text{SO}_2$  concentration on the reaction rate was found to depend on the relative humidity. Figures 1-4 and 1-5 illustrate the effect of inlet  $\text{SO}_2$  concentration at 70 and 50% relative humidity respectively. The full lines in these figures correspond to experimental results, and the broken lines to the model predictions. At 70% relative humidity the  $\text{Ca}(\text{OH})_2$  conversion was practically independent of the inlet  $\text{SO}_2$  concentration as can be seen in Figure 1-4. At lower relative humidity the reaction rate is not affected by the  $\text{SO}_2$  concentration if the  $\text{SO}_2$  concentration is high. However, at lower levels of  $\text{SO}_2$  the reaction rate is affected by the  $\text{SO}_2$  concentration as illustrated by Figure 1-5. The observed effect of  $\text{SO}_2$  concentration can be explained by assuming that the reaction rate has zero order kinetics

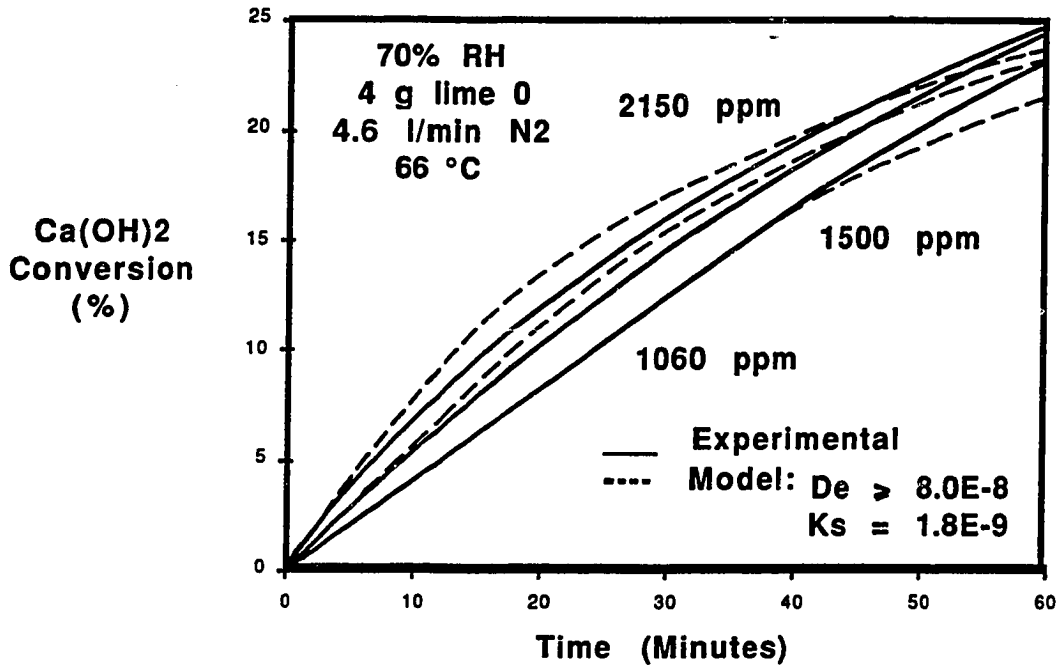


Figure 1-4: Effect of SO<sub>2</sub> Concentration, High Relative Humidity

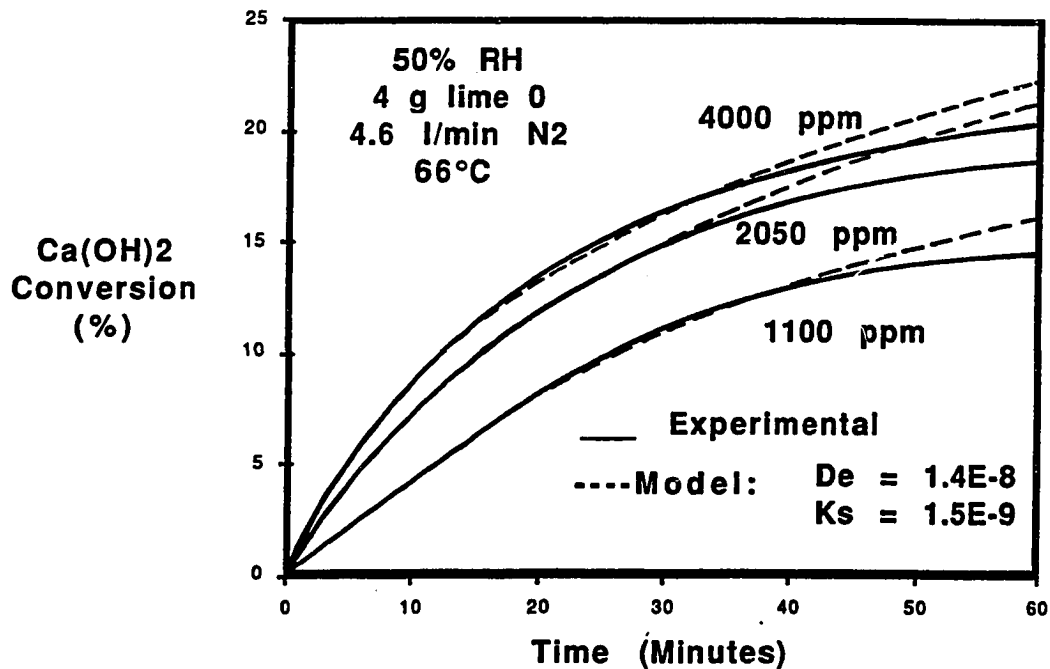


Figure 1-5: Effect of SO<sub>2</sub> concentration, Low Relative Humidity

in  $\text{SO}_2$ , but at low relative humidity and/or low  $\text{SO}_2$  concentrations,  $\text{SO}_2$  diffusion becomes the controlling step instead of chemical reaction. As can be seen from Figures 1-4 and 1-5, the model is able to predict the  $\text{SO}_2$  effect with reasonable accuracy.

### 1.5.3 Effect of Amount of $\text{Ca}(\text{OH})_2$ in the Reactor

The effect on the average  $\text{Ca}(\text{OH})_2$  conversion of changing the amount of  $\text{Ca}(\text{OH})_2$  in the reactor is illustrated by the full lines in Figure 1-6 which show the experimental  $\text{Ca}(\text{OH})_2$  conversion when the amount of lime 0 in the reactor was reduced from 4 to 1 g at 1000 ppm  $\text{SO}_2$ , 50% relative humidity. From the figure it can be seen that the amount of  $\text{Ca}(\text{OH})_2$  present in the reactor makes a difference during the first minutes of reaction, but the effect is less marked at later times. These results are consistent with the effect of  $\text{SO}_2$  concentration discussed in the previous section. When more  $\text{Ca}(\text{OH})_2$  is present in the reactor, more  $\text{SO}_2$  is removed at the entrance of the reactor, so the  $\text{Ca}(\text{OH})_2$  present farther down in the reactor "sees" a lower concentration of  $\text{SO}_2$ , and the reaction rate is slower. At later times when the  $\text{SO}_2$  removal is lower the amount of  $\text{Ca}(\text{OH})_2$  present will not be as important.

### 1.5.4 Effect of Reactor Temperature

Reactor temperature has a very moderate effect on  $\text{Ca}(\text{OH})_2$  reactivity, as illustrated by the full line in Figure 1-7, which shows the effect on  $\text{Ca}(\text{OH})_2$  conversion when the reactor temperature was increased from 30.4 to 64.4°C while keeping all other variables constant. The relative humidity was 74%, so in this region the reaction is expected to be kinetically controlled.

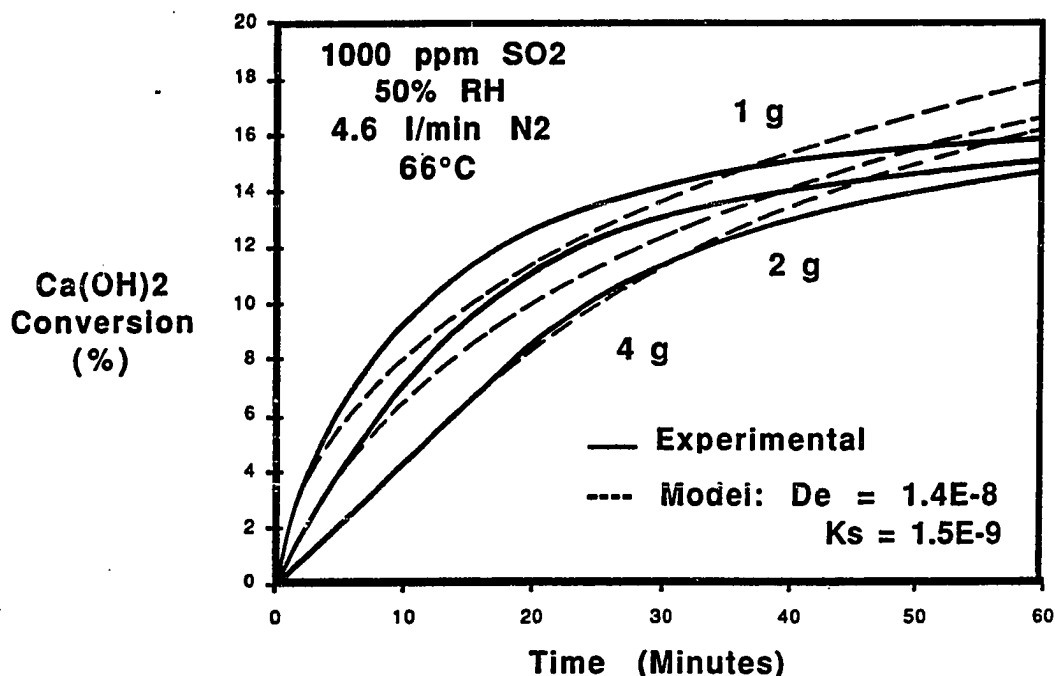


Figure 1-6: Effect of Ca(OH)<sub>2</sub> loading, 1000 ppm SO<sub>2</sub>

The broken lines in Figure 1-7 are the model prediction for the experiments run at the two different temperatures. At the conditions at which the experiments were performed the reaction rate is kinetically controlled, so  $k_s$  is the only important adjustable parameter in the model. By using the values of  $k_s$  given by the model an apparent activation energy of 2.9 kcal/gmol can be estimated for Ca(OH)<sub>2</sub>. This value of activation energy is somewhat lower than the value of 6 kcal/gmol reported by other sources for this reaction (Acurex, 1985).

A very weak dependence of the reaction rate with temperature was also reported by other researchers (Klingspor et al., 1984, Jorgensen et al., 1986).

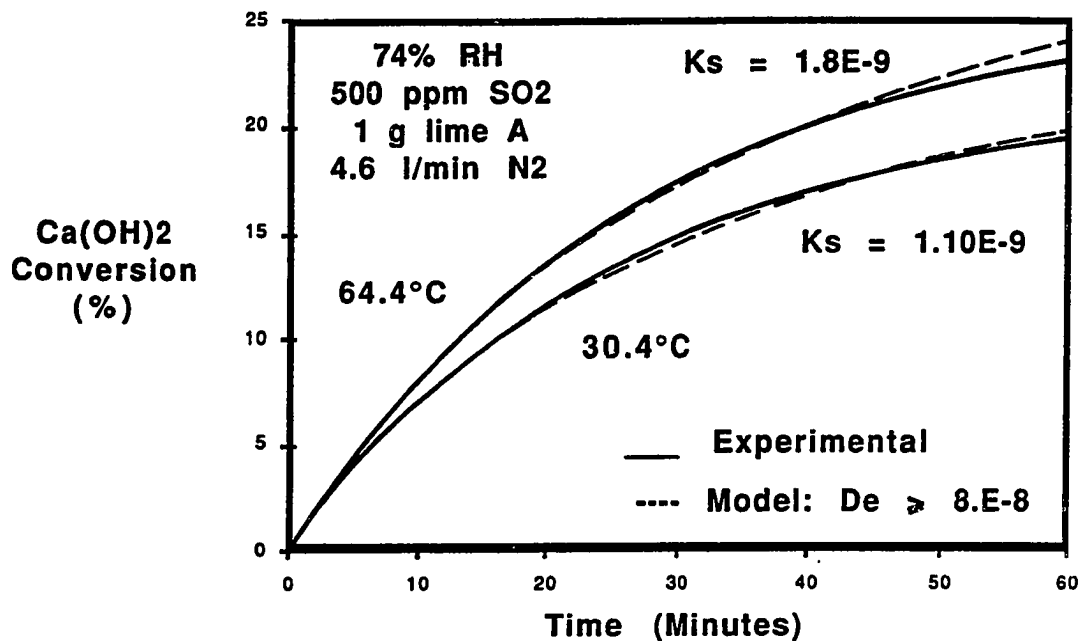


Figure 1-7: Effect of Reactor Temperature, Lime A

### 1.5.5 Effect of Additives

Two organic acids (adipic acid, and glycolic acid), and three organic deliquescents (ethylene glycol, tri-ethylene glycol, and mono-ethanolamine) were selected as test additives for Ca(OH)<sub>2</sub>. All of them proved to be detrimental to the reaction of SO<sub>2</sub> with Ca(OH)<sub>2</sub>.

A number of deliquescent salts were also tested as additives at 74 and 54% RH (Table 1-3). The beneficial effect of the salts depends on the type and amount of salt and the relative humidity. At high relative humidity (74%) all the deliquescent salts tried were successful in increasing the reactivity of the Ca(OH)<sub>2</sub> towards SO<sub>2</sub>. At a lower relative humidity (54%) some of the salts do not perform as well, and some, such as Ca(NO<sub>3</sub>)<sub>2</sub>, do not have any beneficial effect at all.

**Table 1-3: Effect of Deliquescent Salts in Ca(OH)<sub>2</sub> Reactivity and Deliquescent Properties of the Salts**

500 ppm SO <sub>2</sub> , 1.0 g lime A, 4.6 l/min N <sub>2</sub> (0°C, 1 atm)							
Additive (Mole%)	Ca(OH) <sub>2</sub> Conversion at 60 minutes (%)			Model Constants			
	74% RH	54% RH	a <sub>w</sub> (#)	at 74% RH		at 54% RH	
	64.4°C	66°C	at 70°C	D <sub>c</sub> E+8 (cm <sup>2</sup> /s)	k <sub>s</sub> E+9 (cm <sup>4</sup> /mol s)	D <sub>c</sub> E+8 (cm <sup>2</sup> /s)	k <sub>s</sub> E+9 (cm <sup>4</sup> /mol s)
None	22.4	11.8	-	≥ 8.0	1.8	1.5	≥ 1.5
5% Na <sub>2</sub> SO <sub>4</sub>	28.3	-	.887(1)	≥ 18.0	2.7	-	-
5% Na <sub>2</sub> SO <sub>3</sub>	29.8	16.1	-	≥ 17.0	2.6	3.3	≥ 1.7
5% CaCl <sub>2</sub> (**)	34.6	16.4	.69(1)	≥ 73.0	5.4	2.9	≥ 1.6
10% NaCl	38.5	27.0	.751 (2)	≥ 85.0	6.1	≥ 18.0	2.75
5% Ca(NO <sub>3</sub> ) <sub>2</sub> (**)	39.4	12.3	.553(*,1)	≥ 85.0	7.0	1.6	≥ 1.5
5% Co(NO <sub>3</sub> ) <sub>2</sub>	-	13.2	-	-	-	1.9	≥ 1.5
10% NaNO <sub>2</sub>	40.0	-	.593 (2)	≥ 80.0	7.0	-	-
10% NaNO <sub>3</sub>	41.5	27.2	.657 (2)	≥ 95.0	7.6	≥ 18.0	2.75
5% BaCl <sub>2</sub>	-	19.4	.876(1)	-	-	4.5	≥ 1.9
5% Na <sub>2</sub> S <sub>2</sub> O <sub>3</sub>	-	21.6	.298(1)	-	-	6.6	2.15
10% KCl	-	37.3	.80 (2)	-	-	≥ 80.0	4.8
10% NaBr	-	42.0	.507 (2)	-	-	≥ 90.0	7.7
10% LiCl	-	43.9	.099(1)	-	-	≥ 120.	8.23
100% SO <sub>2</sub> Removal	48.2	48.2					

(\*) data at 100°C.

(\*\*) Solid phases were CaCl<sub>2</sub>·Ca(OH)<sub>2</sub>·H<sub>2</sub>O and Ca<sub>2</sub>N<sub>2</sub>O<sub>7</sub>·2H<sub>2</sub>O respectively.

(1) Source (National Research Council, 1930)

(2) Source (Lange, 1961)

(#) Activity of water over saturated solutions of the salt

Also presented in Table 1-3 is the water activity over saturated solutions of the salts at 70°C and 1 atm. The water activity is approximately equal to the relative humidity of the gaseous phase that would be in equilibrium with a saturated solution of the salt at that temperature. If one of these deliquescent salts is contacted with a gaseous phase of relative humidity greater than the water activity, the salt will capture water from the gas phase and become a solution. This tendency to capture water has been extensively documented in the literature by studies of the growth of salt containing aerosols as a function of the atmospheric relative humidity (Winkler, 1973, Ferron, 1977, Tang, 1976, Tang et al., 1977, Tang and Munkelwitz, 1977, Tang et al., 1978). From the data presented in Table 1-3 is clear that based in deliquescence alone most of the salts tested, specifically  $\text{NaNO}_3$  and all the chlorides with exception of  $\text{LiCl}$ , should not have any beneficial effect at 54% relative humidity. Nevertheless, these salts are among the ones that behave the best at that low relative humidity. A possible explanation for this findings would be an hysteresis phenomenon, and this will be discussed later.

Table 1-3 also shows the values of the diffusion coefficient of  $\text{SO}_2$  through the product layer ( $D_e$ ), and the kinetic constant ( $k_g$ ) that can be used to simulate the experimental runs using salt additives.  $D_e$  values ranging from  $1.5\text{E-}8$  to  $120\text{E-}8$  ( $\text{cm}^2/\text{s}$ ) and  $k_g$  values from  $1.5\text{E-}9$  to  $8.23\text{E-}9$  ( $\text{cm}^4/\text{gmol s}$ ) were used in the simulation of the salt experiments. Depending on the amount and type of salt added, chemical reaction or  $\text{SO}_2$  diffusion can become the controlling step. A reasonably good agreement was found between the predictions of the model and the experimental results. The maximum percentage of error between the experimental data and predicted values was below 10% in most cases with a few exceptions where it was below 20%.

### 1.5.5.1. Influence of Salt Concentration

The influence of the salt concentration on the  $\text{SO}_2$  reaction rate is illustrated by Figure 1-8. The salts used were  $\text{NaCl}$  and  $\text{NaNO}_3$  in concentrations ranging from 1 to 15 mole%. The experiments were carried out at a relative humidity of 54%, and a reactor temperature of  $66^\circ\text{C}$ . As can be seen from the figure, the conversion increases with increasing concentration of additive until about 10 mole%. After this the curve levels off. The optimum concentration of additive is then about 10 mole% for 1:1 electrolytes like  $\text{NaCl}$  and  $\text{NaNO}_3$ .

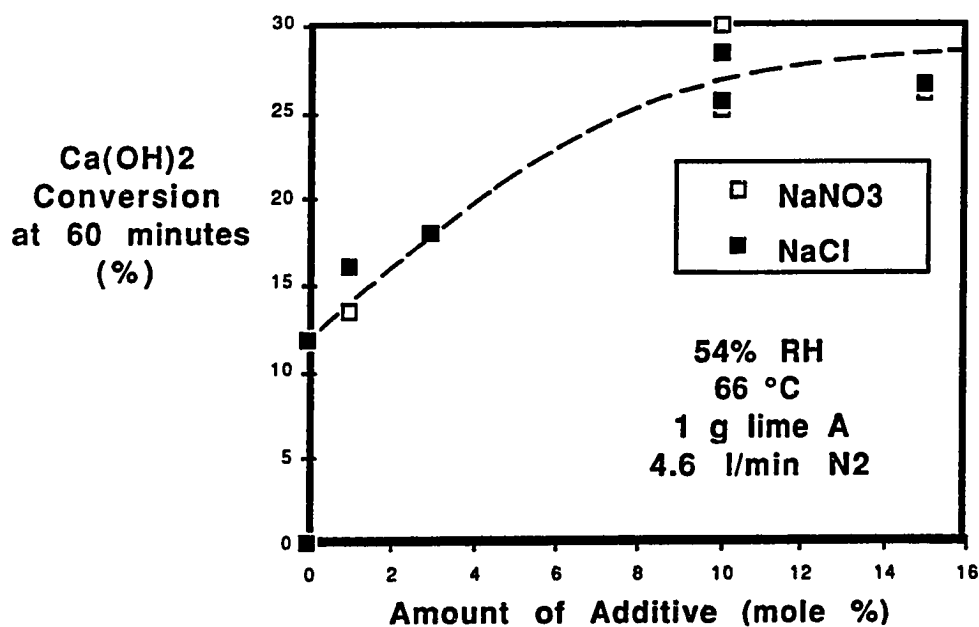


Figure 1-8: Effect of Amount of Additive

The deliquescent salts affected the model parameters in a similar way to the relative humidity, the diffusion coefficient increasing more rapidly than the kinetic constant. Figure 1-9 illustrates the effect

of NaCl on the model parameters. The kinetic constant increased linearly when NaCl concentration was increased from 0 to 10 mole%, while the diffusion coefficient increased exponentially after a sharp increase from 0 to 1 mole% NaCl.

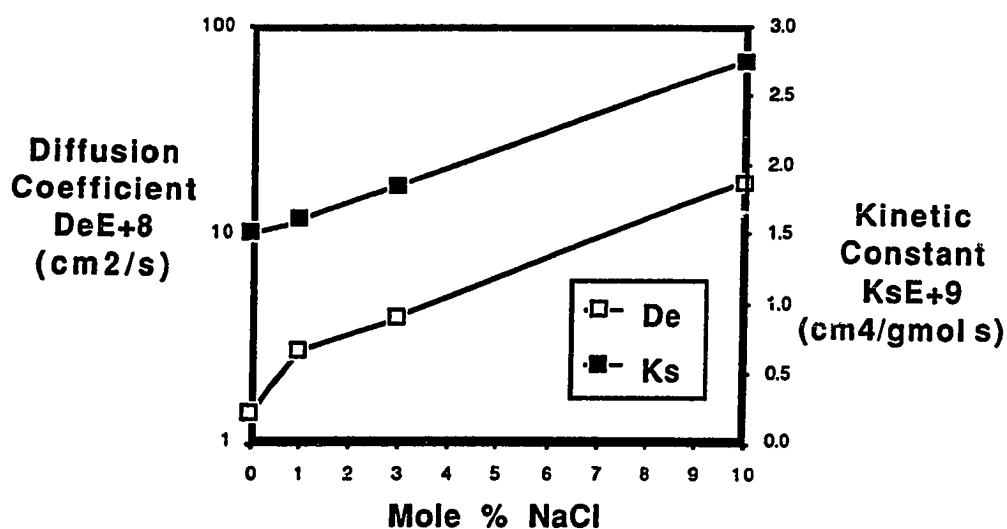


Figure 1-9: Effect of NaCl on the Model Parameters

#### 1.5.5.2. Effect of Prehumidification of Bed

As was mentioned in the Experimental Apparatus Section, before each experimental run the fixed bed was prehumidified by flushing with pure nitrogen a relative humidity of about 98% for 10 minutes before flushing with nitrogen at the relative humidity at which the experiment was to be performed.

This prehumidification step could be the reason why some of the salts are still effective at a relative humidity lower than the one predicted from equilibrium considerations. Due to hysteresis it is possible

that when the relative humidity was lowered to the experimental conditions after the prehumidification, some excess water remains in the solids. Strong hysteresis effects have been reported in NaCl aerosols (Tang and Munkelwitz, 1977).

To check if hysteresis was responsible for the beneficial effect of some salts at low relative humidities, experimental runs were made omitting this step. Table 1-4 shows the results obtained at 54 and 17.4% relative humidity with and without prehumidification of the bed at 98% relative humidity.

**Table 1-4: Effect of Prehumidification of the bed at 98% RH on Ca(OH)<sub>2</sub> Reactivity**

500 ppm SO<sub>2</sub>, 1.0 g Ca(OH)<sub>2</sub>, A, 4.6 l/min (0°C, 1 atm) N<sub>2</sub>

Average Ca(OH)<sub>2</sub> Conversion after 1 hr (%)

Additive (Mole%)	54% RH 66°C		17.4% RH 95°C	
	Prehumidified		Prehumidified	
	Yes	No	Yes	No
None	11.2	-	4.0	-
10% NaCl	27.0	23.2	9.7	4.0
10% NaNO <sub>3</sub>	27.2	23.7	11.9	-
10% KCl	37.3	19.3	3.4	-

The additives used were NaCl, NaNO<sub>3</sub> and KCl. At 54% relative humidity even when some decrease of the Ca(OH)<sub>2</sub> conversion was found without the prehumidification, the results are still far superior to the pure Ca(OH)<sub>2</sub> case. Hysteresis then, can not explain all the beneficial effect observed at 54% relative humidity. At 17.4% relative humidity all the beneficial effect in the case of the NaCl appears to be due to the prehumidification of the bed i.e. due to a hysteresis phenomenon.

## 1.6 Conclusions

As shown in the results section, the relative humidity of the gaseous phase is the most important variable in the reaction of  $\text{SO}_2$  with  $\text{Ca}(\text{OH})_2$  solids. These results are in agreement with results reported in the literature for  $\text{SO}_2$  removal in the bag filters of spray dryer pilot and commercial plants (Blythe and Rhudy, 1984, Bresowar et al., 1981, Robards et al., 1985, Samuel et al., 1983, Stevens, 1981, Stevens et al., 1982), and bench scale studies (Klingspor et al., 1983, Klingspor et al., 1984, Acurex, 1985, Jorgensen et al., 1986). The other variables tested, i.e. temperature, amount of  $\text{Ca}(\text{OH})_2$ , and  $\text{SO}_2$  concentration have a lower impact on the reaction rate. The different effect of  $\text{SO}_2$  concentration at low and high relative humidity can be explained by assuming that the reaction has zero order kinetics in  $\text{SO}_2$  and that at low relative humidity the reaction rate is mass transfer controlled while at high relative humidities the reaction is controlled by reaction kinetics.

Most of the deliquescent salts tried were effective in increasing  $\text{Ca}(\text{OH})_2$  reactivity towards  $\text{SO}_2$ . The extent of the beneficial effect being a function of the type of salt, the salt concentration, and the relative humidity. Some salts are effective at a lower relative humidity than would be predicted from their deliquescent properties. Hysteresis due to the prehumification of the bed appears to be partially responsible for this behavior, but it can not explain all the improvement observed at 54% relative humidity. An alternate explanation proposed is that the chlorides and  $\text{NaNO}_3$  modify the properties of the product  $\text{CaSO}_3 \cdot 1/2\text{H}_2\text{O}$  layer that is formed as the reaction takes place thereby facilitating the access of the  $\text{SO}_2$  to the unreacted  $\text{Ca}(\text{OH})_2$  which remains in the interior of the particle.  $\text{NaCl}$  and  $\text{CaCl}_2$  have been

reported to enhance the sulfur dioxide reactivity of limestones in fluidized bed combustion by affecting the the pore structure of the lime during calcination, which then increases the extent of sulfation of the limestone (Chopra et al., 1980).

The only previous modelling effort for this reaction was the work of Klingspor et al. (1983, 1984). Their work used an integral shrinking core model with only reaction kinetics to explain the dependence of reaction rate on lime conversion. Their experimental data fit this integral shrinking core model only after a certain lime conversion had been reached. They attributed the sharp decrease on reaction rate observed at initial times to a decrease in surface roughness, but did not attempt to correlate this decrease in surface roughness with lime conversion. Their model neglects the effects of  $\text{SO}_2$  diffusion through the product layer and their model also neglected the  $\text{SO}_2$  concentration and lime concentration profiles in the fixed bed reactor. All of these factors will be more important at initial times, when the  $\text{SO}_2$  removal is higher, so it is not surprising that they were able to fit the the experimental data only at later times.

The simple model presented here seems able to predict with reasonable accuracy the effect of all the process variables tested and explain the trends observed in the experimental data. The experimental data are estimated to have  $\pm 10\%$  experimental error, so the predictions of the model are well within the range of experimental error in most cases. The values of the diffusion coefficient used in the modelling (from  $0.75\text{E-}9$  to  $1.20\text{E-}6$ ) seem reasonable for diffusion of  $\text{SO}_2$  in a solid, as they are of the same order of magnitude of the diffusivities of gases in polymers (Vieth and Amini, 1974, Brzozowski and Kumins, 1974,

MacDonald and Haung, 1981, McBride et al., 1979, Minoura et al., 1981).

The relative humidity affects both the diffusion coefficient of  $\text{SO}_2$  and the kinetic constant. In the range of relative humidity studied (19 to 74%) the kinetic constant increased linearly with relative humidity while the diffusion coefficient increased exponentially. This dependence of the parameters on the relative humidity leads to a change in controlling mechanism as the relative humidity decreases. At high relative humidity and/or high  $\text{SO}_2$  concentration the reaction rate is kinetically controlled and the reaction rate is independent on the  $\text{SO}_2$  level. At low relative humidity and/or low  $\text{SO}_2$  concentration the controlling step is the diffusion of the  $\text{SO}_2$  through the  $\text{CaSO}_3 \cdot 1/2\text{H}_2\text{O}$  product layer. At these conditions the overall reaction rate becomes affected by the  $\text{SO}_2$  concentration which is the driving force for diffusion.

The addition of deliquescent salts increases the diffusion coefficient and the kinetic constant in a similar way to the relative humidity, the diffusion coefficient increasing more rapidly than the rate constant. When increasing amounts of the same salt (NaCl) were added,  $k_s$  increased linearly and  $D_e$  nearly exponentially. Depending on the amount and type of salt additive, chemical reaction or gas diffusion can be the controlling mechanism.

The kinetic constant was a very weak function of temperature. The estimated activation energy was 2.9 kcal/gmol.

## Chapter 2

### Background of Research

#### 2.1 Introduction

Sulfur dioxide is one of the most abundant pollutants in the United States. The estimated yearly emissions of sulfur dioxide for the years 1972, 1975, 1977, 1979 and 1981 are presented in Table 2-1. Most of the SO<sub>2</sub> emissions originate from the combustion of fossil fuels, the electric utilities being the most important source (over 50%). Over 90% of the SO<sub>2</sub> emissions due to electric utilities are from coal-fired boilers. Table 2-2 shows the contribution of different sources to the power generation in the United States during 1982, and the prediction for 1991.

Sulfur is a component of all natural oil and coal, with compositions varying from 0.1 to over 5%. The total SO<sub>2</sub> emissions will vary considerably depending on the nature and origin of the fuel. Power plant gases generally contain low concentrations of SO<sub>2</sub>, but they are emitted at large volumetric rates. Typical concentrations of SO<sub>2</sub> in power plant gases with 15% excess air range from 0.11 to 0.35% SO<sub>2</sub> by volume, depending on the type of fuel (Seinfeld, 1975, Clarke, 1980).

Once in the atmosphere, SO<sub>2</sub> is partly oxidized to sulfur

**Table 2-1: National Estimates of Sulfur Dioxide Emissions  
Teragrams/year**

Source	1972	1975	1977	1979	1981
Transportation	0.6	0.6	0.8	0.9	0.8
<b>Stationary Fuel Combustion</b>					
Electric Utilities	15.8	16.5	16.9	15.8	14.8
Industrial	3.5	2.7	2.8	2.7	2.3
Residential, Commercial	1.2	1.0	1.1	0.8	0.7
Industrial Processes	6.4	4.8	4.4	4.3	3.9
Others	0.2	0.0	0.0	0.0	0.0
<b>TOTAL</b>	<b>27.7</b>	<b>25.6</b>	<b>26.0</b>	<b>24.5</b>	<b>22.5</b>

Source: (EPA Report 450/4-82-012, 1982)

**Table 2-2: Power Generation Sources: Present and Future**

	Percentage of Generation Power						Total Generating Capacity (GW)
	Coal	Nuclear	Oil	Hydro	Gas	Other	
Dec. 1982	42	11	23	12	11	1	656
Dec. 1991	44	16	19	11	9	1	799

Source: (Melia et al., 1983)

trioxide or sulfuric acid and its salts by photochemical or catalytic reactions (Seinfeld, 1975). It is difficult to isolate the environmental impacts of sulfur compounds alone, as they are often associated with other pollutants. The most damaging effects attributed to atmospheric air pollution are produced by oxides of sulfur in combination with particulate matter and moisture.

Sulfur compounds are held responsible for damage to a number of building materials including limestone, marble, roofing slate, and mortar. Textiles, especially nylon, can be weakened by  $\text{SO}_2$  or sulfuric acid (Wark and Warner, 1981). Finally, sulfuric acid accounts for 60 to 70% of the acidity of acid rain (Wark and Warner, 1981), so  $\text{SO}_2$  emissions are undoubtedly linked with this phenomena. Several detrimental environmental effects have been attributed to acid rain such as acidification of natural water sources, leaching of nutrients from the soil, direct damage to vegetation, and increase in the corrosion of building materials. The severity of the damage caused by acid rain depends on the type of minerals present in a given region. Regions that contain rocks such as limestone or similar minerals are buffered against the onslaught of acid rain. Since it is very difficult to alter the effects of acid rain once it has occurred in a region, the best solution is to control the  $\text{SO}_2$  emissions at the source.

## **2.2 Reduction of $\text{SO}_2$ Emissions**

Four possible methods or alternatives may be used to reduce the effects of  $\text{SO}_2$  emissions from fossil fuels. These potential methods are:

**A. Switch to low-sulfur fuel**

- B. Desulfurize coal and oil
- C. Build tall stacks to increase atmospheric dispersion
- D. Desulfurize flue gas.

### **2.2.1 Change to low-sulfur fuel**

Shifting to low-sulfur fuel was a method widely used in the United States in the early 70's when air pollution regulations were established by the Environmental Protection Agency (EPA) limiting sulfur dioxide emissions (Marchello, 1976). Nevertheless, the substitution of low sulfur fuel is only a short term solution because of the limited supply, especially of natural gas and low sulfur oil (Zareski, 1973, Morrell et al., 1973). The United States does have large reserves of low sulfur coal, but their geographical location is not ideal. Most of the coal consuming utilities are in the East and Midwest, while 90% of the low sulfur coal reserves (less than 1% sulfur) are in the West (Hunter, 1973, Wark and Warner, 1981). This means high transportation cost for this low sulfur coal. The technical factors and power plant modifications needed for low sulfur coal have been discussed in detail by Schwartz (1984).

An intermediate solution, the blending of low-sulfur Western coal with local high sulfur coal has been long been practiced by some Midwestern Utilities. Another form of fuel blending that can be accomplished more easily with little capital expenditure is the augmentation of pulverized coal with natural gas, a procedure which has been termed the "select use" of gas (Green, 1984).

### 2.2.2 Use of Desulfurized Coal and Oil

Sulfur is contained in coal in organic and inorganic forms. Inorganic sulfur, in the form of iron pyrite ( $\text{FeS}_2$ ), is present in discrete lumps through the coal and due to its greater density can be separated from the coal by gravity washing. About 40 to 60% of a given coal's sulfur is in the form of pyrites (Moriber, 1974), and up to 84% of the pyritic sulfur can be eliminated by crushing and gravity washing (Cavallaro et al., 1974). Sulfur in the organic form is chemically bound to the coal and it can not be removed without chemically changing the nature of the coal. Consequently, more costly and complex processes are required to remove the organic sulfur from the coal. Examples of such processes are coal gasification, or coal liquefaction. Several coal gasification and coal liquefaction techniques are under development (Belt and Roder, 1973, Qader and Hill, 1973, Yavorsky et al., 1974, Akhtar et al., 1974), and the technical feasibility of these processes has been established. Their economic feasibility remains yet to be proven.

The desulfurization of natural oil can be accomplished by several commercially available processes (Johnson et al., 1973, Gregoli and Hartos, 1973), and although desulfurization is expensive, there is no technological deterrent (Barthel et al., 1974).

### 2.2.3 Tall Stack Dispersion

This control method is based on natural dispersion at high elevation so that ground level concentrations are acceptable at all times. The usefulness of this method is limited, because it reduces the air pollution in a local area but does not eliminate the problem. The  $\text{SO}_2$  remains in the atmosphere where it is slowly oxidized to  $\text{SO}_3$  and reacts

with water droplets to form sulfuric acid. Thus, the  $\text{SO}_2$  may manifest itself as acid rain in places hundreds of miles away from the source.

#### **2.2.4 Removal of $\text{SO}_2$ from Flue Gases**

The removal of  $\text{SO}_2$  from flue gases has probably been subject to more research than any other gas-purification operation, and a variety of processes has been developed. Flue gas desulfurization (FGD) processes can be grouped according to two classifications: 1) throwaway or regenerative and 2) wet or dry. Throwaway processes are those in which a waste product is formed which must be discarded. As a result, fresh chemicals must be continuously added. In regenerative processes, as the name indicates, the removal agents are continuously regenerated in a close-loop system. Wet or dry processes differ simply by whether or not the active removal agent is contained in a liquid solution. Table 2-3 lists the most important flue gas desulfurization processes. Dry flue gas desulfurization processes will be reviewed in detail in the following sections.

### **2.3 Throwaway Dry FGD Processes**

#### **2.3.1 Dry Injection**

Dry injection processes involve pneumatically introducing a dry powdery alkaline material into the flue gas stream, followed by particulate collection either using bag filters or electrostatic precipitators. The injection point can vary from the boiler furnace area all the way to the entrance to the solids collection equipment (Kelly and Dickerman, 1981, Kelly and Shareef, 1981, Kelly et al., 1983, Blythe et al., 1980). The most commonly used sorbents are nahcolite, trona and refined trona

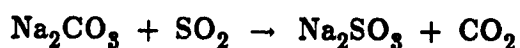
**Table 2-3: Flue Gas Desulfurization Processes**

Process Generics	Process Operations	Key Sulfur Product
<b>A. Throwaway Scrubbing</b>		
1. Lime or limestone	Slurry scrubbing	$\text{CaSO}_3/\text{CaSO}_4$
2. Sodium Carbonate	$\text{Na}_2\text{SO}_3$ solution	$\text{Na}_2\text{SO}_4$
3. Double Alkali	$\text{Na}_2\text{SO}_3$ solution, regenerated by CaO or $\text{CaCO}_3$	$\text{CaSO}_3/\text{CaSO}_4$
4. Magnesium-promoted lime/limestone	$\text{MgSO}_3$ solution, regenerated by CaO or $\text{CaCO}_3$	$\text{CaSO}_3/\text{CaSO}_4$
<b>B. Regenerative scrubbing</b>		
1. Magnesium Oxide	$\text{Mg}(\text{OH})_2$ slurry	15% $\text{SO}_2$
2. Wellman-Lord	$\text{Na}_2\text{SO}_3$ solution	S, $\text{H}_2\text{SO}_4$
3. Citrate	Sodium Citrate solution	Sulfur
4. Ammonia	Ammonia solution, conversion to $\text{SO}_2$	Sulfur (99.9%)
<b>C. Dry throwaway</b>		
1. Dry injection	Alkali injection in flue gas	$\text{Na}_2\text{SO}_3$
2. Coal/Alkali combustion	Burning Coal/limestone	$\text{CaSO}_3/\text{CaSO}_4$ mixture
3. Injection/humidification	Alkali injection/gas humidification	$\text{CaSO}_3/\text{CaSO}_4$
4. Spray dryer	Absorption with slaked lime solutions	$\text{CaSO}_3/\text{CaSO}_4$
<b>D. Dry Regenerative</b>		
1. Aqueous carbonate	Absorption with $\text{Na}_2\text{CO}_3$ solution, reaction with C, $\text{CO}_2$	Sulfur
2. Molten carbonate	Absorption with molten carbonate, reaction with CO, $\text{H}_2$	Sulfur
3. Manganese oxide	Powder $\text{MnO}_2$ injection	$\text{NH}_4\text{SO}_4$

(Genco et al., 1975, Genco and Rosenberg, 1976, Bechtel Corporation, 1976, Lutz et al., 1979, Veazie and Kielmeier, 1970, Bagwell et al., 1969, Muzio et al., 1980, Muzio et al., 1983, Ablin, 1984). Pressure hydrated lime and dolomitic lime have also been tested, but they give a lower SO<sub>2</sub> removal than nahcolite and trona (Weber et al., 1984, Bobman et al., 1985).

Nahcolite is a naturally occurring mineral containing up to 90% sodium bicarbonate. Large reserves of this mineral are found in Northwest Colorado and Southwest Wyoming (Samuel and Lapp, 1980). Trona is another natural mineral composed of sodium carbonate and bicarbonate, with 2 moles of hydration water (NaHCO<sub>3</sub>·Na<sub>2</sub>CO<sub>3</sub>·2H<sub>2</sub>O). Trona is also found in relative abundance in Southwestern Wyoming and Owens Lake, California. Refined trona is bicarbonate-enriched trona.

The overall reactions for the removal of SO<sub>2</sub> using nahcolite or trona are:



Sodium bicarbonate is more reactive than sodium carbonate, so at comparable sodium injection ratios trona is less effective in removing SO<sub>2</sub> than nahcolite. The higher reactivity of NaHCO<sub>3</sub> has been attributed to thermal decomposition of the NaHCO<sub>3</sub> into highly reactive Na<sub>2</sub>CO<sub>3</sub> which simultaneously reacts with SO<sub>2</sub>. As the sodium bicarbonate decomposes new surface continually becomes available for reaction with SO<sub>2</sub>. The decomposition of the NaHCO<sub>3</sub> may also provide a moisture layer which serves as a reaction media and increases the reaction rate (Mueller and Winston, 1985). 70% SO<sub>2</sub> removal has been

achieved with nahcolite at a stoichiometric ratio of 1.05 (2 moles of total Na/mol SO<sub>2</sub>), while a refined trona stoichiometric ratio of 1.6 was required to reach the same removal. The maximum SO<sub>2</sub> removal observed with trona has been 50% (Samuel and Lapp, 1982).

Both baghouse and electrostatic precipitators have been tested for collection of solids in dry injection processes. Bag filters are better than electrostatic precipitators because additional reaction can take place between unspent sorbent collecting on the bag surface and the SO<sub>2</sub> remaining in the flue gas, thus increasing overall SO<sub>2</sub> removal (Kelly and Shareef, 1981).

Data collected in bench-scale and pilot-scale experiments support the technical feasibility of dry injection as an SO<sub>2</sub> control alternative, and the process appears to have economic advantages over other currently available FGD technologies when applied to western power plants burning low sulfur coal (Lutz et al., 1979, Samuel and Lapp, 1982). There are, nevertheless, two major restraints to development of commercial dry injection systems. First, the uncertainty in sorbent availability, and second and most important, the difficulty of disposal of the solid wastes. The waste products in the case of nahcolite and trona are water soluble sodium sulfate and sodium sulfite which if disposed without stabilization or insolubilization present the environmental danger of leaching and contamination of underground water reserves. These two problems must be solved before dry injection can be commercialized.

### 2.3.2 Coal/Alkali Combustion

Two processes based on the combustion of coal/alkali fuel mixtures to control  $\text{SO}_2$  emissions are under development. Combustion of coal/limestone pellets in an industrial stoker fired boiler, and combustion of pulverized coal/limestone mixture in a low  $\text{NO}_x$  burner (limestone injection multistage burner or LIMB process). Tests at the pilot scale have demonstrated that both of these processes are able to achieve at least 50%  $\text{SO}_2$  removal (Kelly and Shareef, 1981 and 1981a, Kelly et al., 1983, Lisauskas et al., 1985). Coal/alkali combustion is a low cost alternative to other FGD processes, but before these two processes can be applied at a commercial scale, work remains to be done to fully characterize the impact of these technologies on boiler operation and particulate control design and operation. A review of these technologies has been given by Maloney (1980), and some kinetic studies of the reactions in the LIMB burner by Borgwardt (1984).

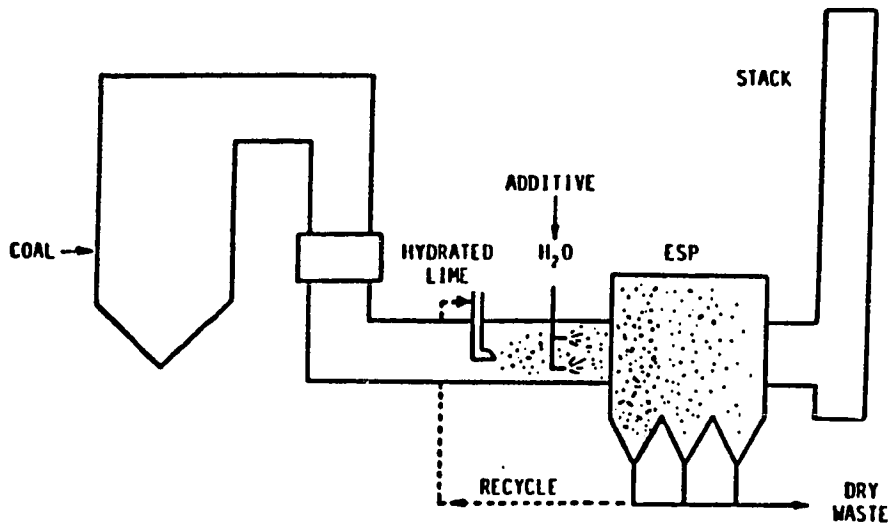
### 2.3.3 Injection/Humidification

Injection/humidification techniques involve humidification of the flue gas and capture of the  $\text{SO}_2$  by a dry sorbent injected in the ductwork downstream of the air preheater, followed by removal of the spent sorbent along with coal fly ash in the particulate collection system (bag filters or ESP) of a coal fired power plant. The  $\text{SO}_2$  reacts with the entrained sorbent particles in the ductwork and with the dense sorbent bed collected in the particulate removal system. Injection/humidification differs from dry injection processes in that it involves humidification of the gas by water spraying. This humidification lowers the temperature of the flue gas so the  $\text{SO}_2$  absorption takes place at a much lower temperature and higher relative humidity than in the dry injection case.

Two injection/humidification processes have been reported in the literature, the coolside process (Stouffer et al., 1985) and hydrate addition at low temperature (Forsythe and Kaiser, 1986).

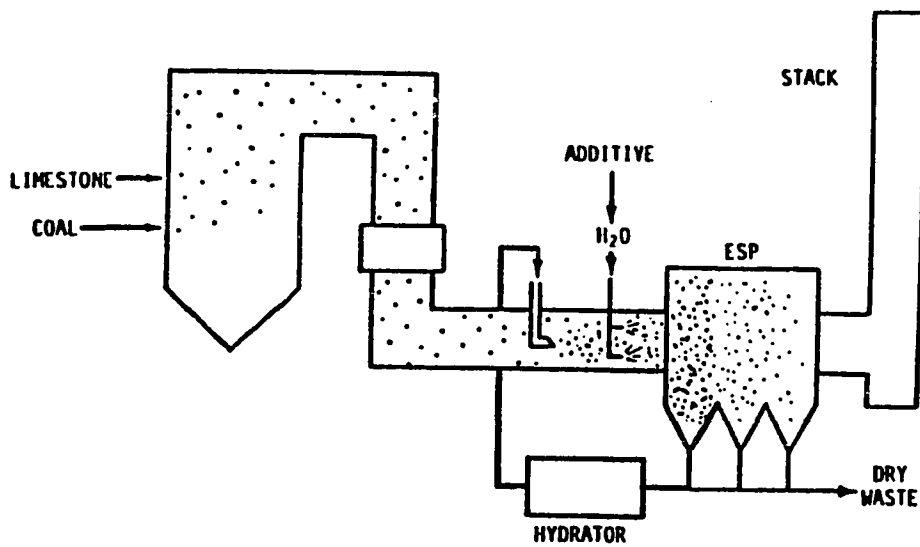
In the coolside process the proposed sorbent is high surface area hydrated lime promoted by the addition of a sodium compound such as sodium hydroxide or sodium carbonate. Boiler Limestone Injection flyash has also been demonstrated to be an effective coolside sorbent after a simple activation step and/or flue gas humidification. This possibility may allow the use of the coolside technique in combination with Boiler Limestone Injection to minimize overall SO<sub>2</sub> control cost.

Diagrams of the straight coolside process using hydrated lime as the sorbent, as well as the Boiler Limestone Injection recycle option are depicted in Figure 2-1. Conoco Coal Research Division made a one MW field trial of this process using a 3000-4000 ACFM flue gas slipstream from a coal fired industrial boiler at Du Pont's Martinsville Nylon Plant. The slipstream was diverted through a pilot scale humidifier and ESP provided by Research Cottrell. Injection of a commercial hydrated lime with sodium based additives (selected based on laboratory work), gave SO<sub>2</sub> removal up to 80% with up to 40% sorbent utilization on a once through basis. The water droplets sprayed into the humidifier played a key role in the observed high SO<sub>2</sub> removal. Additionally humidification was an effective method of conditioning the flue gas for efficient ESP operation, allowing removal of the higher loadings of high resistivity solids caused by the sorbent injection. The combination of coolside and limestone injection technologies also showed significant SO<sub>2</sub> removal across the humidifier and ESP.



A. Hydrated Lime as sorbent.

Source: (Stouffer et al., 1985)



B. Boiler Limestone Injection Recycle Option

Source: (Stouffer et al., 1985)

Figure 2-1: Diagram of the Coalside process

The hydrate addition at low temperature (HALT) technology uses prepared  $\text{Ca}(\text{OH})_2$  particles as the injected sorbent. Additives such as  $\text{CaCl}_2$ , calcium silicate, di-calcium silicate, and calcium aluminate in the water used produce the hydrate, together with careful selection of hydration conditions combine to give the particles a surface chemistry and morphology designed to enhance  $\text{SO}_2$  capture. Preliminary tests conducted on a 255 ACFM test system at the Sammis Plant of the Ohio Edison Co., showed that up to 85%  $\text{SO}_2$  removal could be achieved by optimizing the process parameters (Forsythe and Kaiser, 1986). Further work is necessary to demonstrate the full capabilities of the process.

Injection/humidification techniques have the potential of providing low cost control options attractive for retrofit applications under more stringent  $\text{SO}_2$  regulation. They would require significantly lower capital investment and space than the conventional wet limestone slurry or lime spray dryer processes (Stouffer et al., 1985, Forsythe and Kaiser, 1986). The  $\text{SO}_2$  removal that can be achieved though, is lower than in either of these processes, and they seem to require higher sorbent stoichiometries.

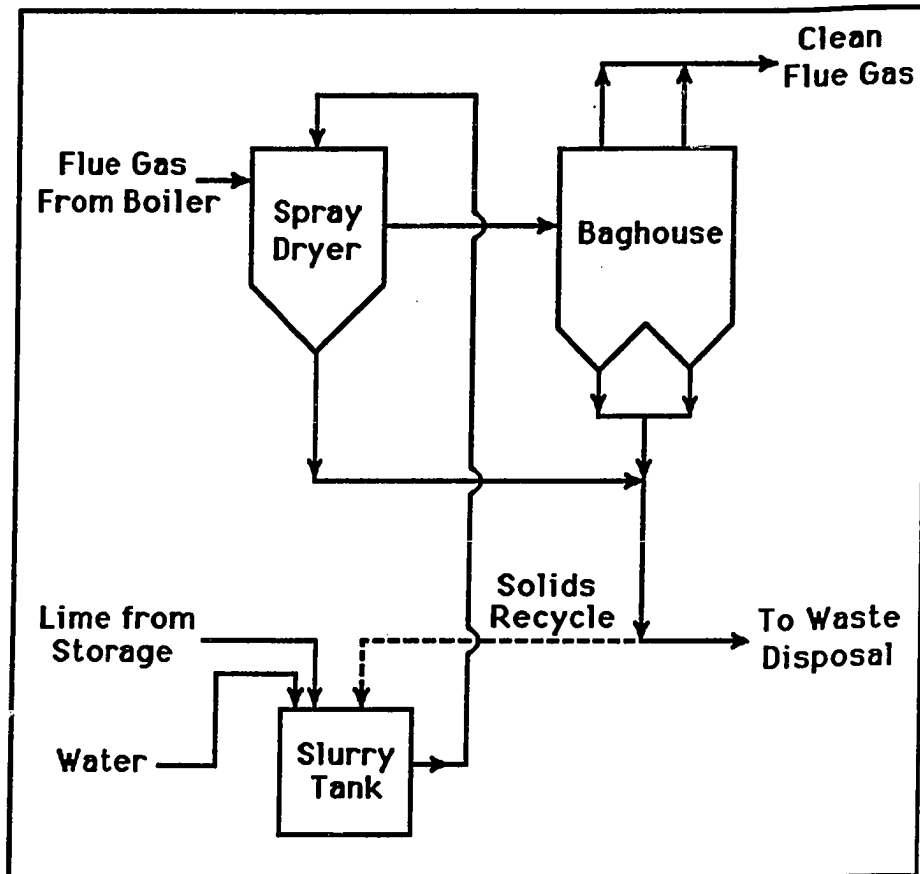
#### **2.3.4 Spray dryer based processes**

Figure 2-2 is a schematic diagram of a typical spray drying FGD system. The flue gas containing fly ash and  $\text{SO}_2$  enters the spray dryer where it is contacted with a finely atomized aqueous solution or slurry of an alkali (typically lime or soda ash). During the approximately 10 seconds of residence time in the dryer the sulfur dioxide is absorbed in the slurry droplets and neutralized by the alkali. Simultaneously, the thermal energy of the gas evaporates the water in

the slurry droplets, adiabatically humidifying the flue gas. The product leaving the spray dryer (a mixture of sulfite, sulfate, carbonate, and some unreacted lime) together with the fly ash is removed in collection equipment such as a bag filter or electrostatic precipitator (ESP). Since not all the water is removed from the solids in the spray dryer, the remaining moisture promotes further reaction with  $\text{SO}_2$  in the ducts leading to the bag filters and in the bag filters. Due to this additional  $\text{SO}_2$  removal, bag filters are the preferred collection equipment.

In a straight-through process, the solids collected in the bag filters will go directly to solid waste disposal while the clean flue gas is released to the atmosphere through the stack.

Parametric studies in a number of pilot and demonstration plants indicated that the main variables affecting  $\text{SO}_2$  removal in a spray drying system are the sorbent stoichiometric ratio and the approach to the adiabatic saturation temperature at the spray absorber outlet (Blythe and Rhudy, 1984, Bresowar et al., 1981, Samuel et al., 1984, Yeh et al., 1983, Jankura et al., 1984). Degree of atomization, gas flow rate, inlet  $\text{SO}_2$  concentration, temperature, and gas retention time in the spray absorber also affect  $\text{SO}_2$  removal, but to a lesser degree (Gustke et al., 1984, Bresowar et al., 1981, Lewis and Gehri, 1983, Samuel et al., 1984). Finally, partial recycle of spray dryer absorber and/or bag house solids has been found to have a significant beneficial effect on  $\text{SO}_2$  removal (Jankura et al., 1984, Parsons et al., 1981, Robards et al., 1985, Blythe and Rhudy, 1984, Kelly et al., 1983, Gustke et al., 1984, Donnelly et al., 1985). The dry waste recycle is added to the fresh lime slurry delivered from the slaker.



**Figure 2-2:** Typical Spray Dryer System for FGD

Spray drying with partial recycle of solid products has been patented by Niro Atomizer (Felsvang, Hansen and Rasmussen, 1981). The beneficial effect of solids recycle has been attributed to several factors (Kaplan and Felsvang, 1980). First, the recycled material contains unreacted lime which can be further utilized when introduced into the spray drying system more than once. Secondly, the spray dried products provide a surface on which slaked particles can agglomerate, thereby exposing more surface area of the fresh lime and enhancing the absorption reaction. A third benefit is from the recirculated fly ash, which, depending on its alkalinity, can allow a reduction of the system stoichiometry resulting in a decrease in the amount of fresh lime required. Jozewicz and Rochelle (1985 and 1985a) have also shown that fly ash can react with  $\text{Ca(OH)}_2$  during slurring of recycle solids with fresh lime, producing high surface area calcium silicates, which are more reactive towards  $\text{SO}_2$  than  $\text{Ca(OH)}_2$ .

Spray dryer flue gas desulfurization systems have received much attention during the last decade, especially for low sulfur coal applications. They present several advantages over conventional lime and limestone wet scrubbing methods that have dominated the market for flue gas desulfurization during past years (Felsvang et al., 1978, Hollett, 1979, Masters, 1980, Shah, 1982, Kaplan and Felsvang, 1980):

- Spray drying systems produce a dry, solid waste that can be handled by conventional fly ash handling systems eliminating the need for sludge handling systems.
- Dry systems should have lower maintenance costs, because they require less equipment (Thickeners, centrifuges, vacuum filters and mixers required to handle the wet sludge waste are not longer required). Also, the slurry pumping requirements are much lower for spray drying. Finally keeping the gas warm minimizes risk of erosion, corrosion, and scaling, thus

allowing the use of carbon steel as the construction material in most equipment.

- The spray dryer absorber is flexible in operation with regard to varying boiler load. Feed rates can be adjusted immediately to maintain a constant emission load.
- A typical spray dryer absorber can be installed in an area where space is limited.

Pilot and demonstration plants have been tested by various FGD system vendors (Stevens, 1981, Stevens et al., 1982, Martin et al., 1980, Grutle and Gehri, 1981, Hurst and Bielawski, 1981, Gunther et al., 1981, Samuel et al., 1983, Blythe and Rhudy, 1984, Blythe et al., 1983, Yeh et al., 1983, Bresowar et al., 1981, Kaplan and Felsvang, 1980), and several economic studies have indicated the potential of dry scrubbing to compete economically with wet sulfur dioxide removal systems for low and medium sulfur coals (Burnett and O'Brien, 1980, Burnett et al., 1981 and 1981a).

In the past years a number of companies and consortia have been contracted to build commercial units. By June 1983 sixteen utility and eight industrial spray dryer system units had been sold. A few of these commercial units are now in operation and have demonstrated the capability of spray dryer systems of competing with wet scrubbing as an alternative for FGD (Gustke et al., 1984, Kaplan et al., 1983, Lewis and Gehri, 1983, Roop and Pflug, 1984, Horn and Bent, 1984, Reinauer et al., 1983, Farber, 1984).

Dry scrubbing was originally developed for low and medium sulfur coal applications, although some reports have appeared recently which deal with the adaptation of the system to utility steam generators burning high sulfur coal (Jankura et al., 1984)

## **2.4 Regenerative Dry FGD Processes**

### **2.4.1 Aqueous Carbonate**

This spray dryer based regenerative process was developed by Atomics International. A sodium carbonate solution is sprayed into the flue gas in a spray dryer type of absorber where the solution absorbs  $\text{SO}_2$  while the water is evaporated from the solution leaving a dry product. After being collected in cyclones and electrostatic precipitators the solids are taken to the reducer where they are reacted with coke and  $\text{CO}_2$  to regenerate the  $\text{Na}_2\text{CO}_3$  and evolve  $\text{H}_2\text{S}$ . The  $\text{H}_2\text{S}$  can be used to produce sulfur in a conventional Claus plant (Slack, 1974, Gehri and Oldenkamp, 1976). Aqueous carbonate is the only regenerative dry FGD process that has been tested at commercial scale. Niagara Mohawk Power owns a 100 MW plant using this process (Melia et al., 1983).

### **2.4.2 Molten Carbonate**

This process, also developed by Atomics International, adsorbs  $\text{SO}_2$  in an eutectic melt of sodium, potassium and lithium carbonate, at a temperature of about  $450^\circ\text{C}$ . The resulting molten solution of alkali metal sulfites, sulfates and unreacted carbonate is regenerated in a two step process with  $\text{CO}$  and  $\text{H}_2$  to the alkali carbonate for recycling.  $\text{H}_2\text{S}$  evolved in the regeneration step is converted to sulfur in a conventional Claus plant (Yosim et al., 1973).

### 2.4.3 Manganese Dioxide

This process developed by Mitsubishi Heavy Industries injects powder  $\text{MnO}_2$  into an entrainment reactor. The  $\text{SO}_2$  is oxidized to metal sulfate, followed by regeneration of the  $\text{MnO}_2$  and production of ammonium sulfate (Seinfeld, 1975).

### 2.5 Scope of Investigation

Dry systems are going to have a larger share of the FGD market in the coming years. By October 1983 spray dryer based systems constituted 4% of the total operating scrubbing capacity, but they constituted 18.6% of the scrubbing capacity under construction, and 21.4% of the planned scrubbing capacity (Melia et al., 1983). All of the spray drying systems in operation with the exception of one are lime throwaway systems. In addition to spray drying based systems some of the other dry processes discussed may reach commercial scale in the future.

The overall reaction in a spray dryer system using lime as the active agent is:



the oxygen in the flue gas oxidizing some of the sulfite to sulfate.

Because of the dependence of spray dryer absorption FGD on water, the stages of the reaction are intimately linked to the drying stages of the slurry droplets. Three drying stages have been described for evaporation of slurry droplets, namely, the constant rate, the falling rate, and the pseudo-equilibrium rate periods (Getler and Furlong, 1979).

The constant rate period lasts until the droplet shrinks to the extent that the alkali particles touch each other. The length of this period will depend on droplet size, initial gas temperature, and solids concentration in the slurry. Under typical dry scrubber conditions the constant rate period would last about 0.12 seconds for a 25 micron droplet at 5% solids, and 0.06 seconds for a 25 micron droplet at 25% solids. The time for a 100 micron droplet will be about 1.6 times more (Downs et al., 1980).

During the falling rate period, the remaining moisture becomes more difficult to remove because the water needs to diffuse through the pores of the agglomerate. Diffusion through and around the particles becomes the limiting step for further moisture removal. If the droplets were evaporated to complete dryness, the time for the falling rate period could be estimated using a correlation suggested by Ranz and Marshall (1952).

The solids, however, do not dry completely but instead establish a pseudo-equilibrium with the cool and humid environment of the spray dryer. The "pseudo-equilibrium stage" or "dry stage" (Downs et al., 1980), does not occur to a major extent within the spray dryer itself but represents the properties of the spray dried solids. Due to the moisture remaining in the solids, they continue to react with  $\text{SO}_2$  in the ducts leaving the spray dryer and in the bag filters used for solid collection.

Reported results from pilot and demonstration spray drying plants indicate that depending on the experimental conditions 10 to 20% of the overall  $\text{SO}_2$  removal takes place in the bag filters (Stevens, 1981,

Samuel et al., 1983, Samuel et al., 1984, Bresowar et al., 1981, Blythe and Rhudy, 1984). These results are misleading because the SO<sub>2</sub> removal is calculated based on the SO<sub>2</sub> concentration entering the spray dryer. If the baghouse removal is calculated based on the SO<sub>2</sub> concentration entering the bag filters it can be seen more clearly that the bag house alone is an efficient SO<sub>2</sub> removal device, especially at higher stoichiometric ratios. At an approach to adiabatic saturation temperature of 15°F and lime stoichiometries from 1.0 to 1.6, SO<sub>2</sub> removal efficiencies between 35 and 68% have been reported (Robards et al., 1985). Baghouse SO<sub>2</sub> removal would be especially important if spray drying were to be extended to high-sulfur coal applications.

The reaction between moist lime solids and SO<sub>2</sub> taking place in the ducts and bag filters of a spray dryer system is the subject of the present research. This reaction also occurs during SO<sub>2</sub> removal using the coolside process described in Section 2.3.3. A better understanding of this reaction and the parameters affecting the reaction rate is crucial to optimize SO<sub>2</sub> removal efficiency and/or decrease sorbent stoichiometric ratios in both spray dryer and coolside processes. Most of the information available in the literature for this reaction is reported results of SO<sub>2</sub> removal across the bag filters of pilot and demonstration spray dryer plants. These results are difficult to interpret, because the conditions of the flue gas entering the bag filters will be dependent on the spray absorber behavior. Any variable changes that affect the SO<sub>2</sub> removal across the spray absorber will change the concentration of SO<sub>2</sub> entering the bag filters. So, two variables will have effectively been changed in the bag filters and the contribution of each one can not be isolated.

Two bench scale studies regarding the reaction of interest have been reported (Klingspor et al., 1983, Klingspor et al., 1984, Acurex, 1985, Jorgensen et al., 1986). However, the characterization of this reaction is far from complete. The bench scale studies as well as spray drying results from pilot and demonstration plants will be discussed in detail in the next chapter.

The present study will be carried out in a bench scale fixed bed reactor, operated at conditions similar to those found in bag filters of commercial spray drying systems, and using powder reagent  $\text{Ca}(\text{OH})_2$  as the sorbent. The effect of  $\text{Ca}(\text{OH})_2$  loading, temperature,  $\text{SO}_2$  concentration, and relative humidity will be studied. Also, additives that improve the lime reactivity towards  $\text{SO}_2$  will be identified.

## Chapter 3

### Reaction of $\text{Ca}(\text{OH})_2$ with $\text{SO}_2$

#### 3.1 Introduction

In a spray drying flue gas desulfurization system, the solids leaving the spray dryer are removed in collection equipment such as bag filters or electrostatic precipitators. Bag filters are the preferred collection equipment, because the unreacted  $\text{Ca}(\text{OH})_2$  present in the solids reacts with  $\text{SO}_2$  in the bag filters, thus producing additional  $\text{SO}_2$  removal (Kelly and Dickerman, 1981, Kelly et al., 1983). As was discussed in the previous chapter, the contribution of bag filters to the overall  $\text{SO}_2$  removal becomes especially important if spray drying is to be extended to high-sulfur coal (Robards et al., 1985). The study of the reaction between  $\text{Ca}(\text{OH})_2$  solids and  $\text{SO}_2$  that takes place in the bag filters and ducts leading to the bag filters is the subject of this Chapter.

The study was carried out in a bench scale fixed bed reactor, the bed consisting of powder reagent  $\text{Ca}(\text{OH})_2$  dispersed in silica sand. The experimental conditions were similar to those of commercial scale bag filters, the main differences being in the gas composition and type of reagent used. The gas phase used in the bench scale experiments consisted of a mixture of  $\text{N}_2$ ,  $\text{SO}_2$ , and water vapor.  $\text{O}_2$ ,  $\text{NO}_x$ , and  $\text{CO}_2$ ,

also components of flue gas, were not included. Powder reagent  $\text{Ca}(\text{OH})_2$  was used as reagent in the fixed bed reactor, while commercial dry scrubbing units use slaked lime.

The effects of  $\text{Ca}(\text{OH})_2$  loading, temperature, relative humidity, and inlet  $\text{SO}_2$  concentration were studied. Before discussing the results of the present research, a brief review of previous research done in bench scale reactors will be presented, as well as results that have been reported in the literature for  $\text{SO}_2$  removal in the bag filters of spray drying pilot and demonstration plants.

## **3.2 Previous Work on the Reaction of $\text{SO}_2$ with $\text{Ca}(\text{OH})_2$**

### **3.2.1 Previous work on fixed bed reactors**

Some work has been reported on the reaction of slaked lime and limestone with  $\text{SO}_2$  at low temperature using a fixed bed reactor similar to the one used in this research (Klingspor et al., 1983, Klingspor et al., 1984, Acurex, 1985, Jorgensen et al., 1986).

Klingspor and coworkers primarily studied limestone, but they found the conclusions to be applicable to lime as well. They used five different samples containing 90.0 to 93.7%  $\text{Ca}(\text{OH})_2$  with surface areas of 14.4 to 25.5  $\text{m}^2/\text{g}$ . Some of the conclusions of their research were:

- The initial reaction rate is an exponential function of the relative humidity of the gas stream.
- The initial reaction rate is a very weak function of the temperature.
- The initial reaction rate is zero order in  $\text{SO}_2$  for relative

humidities below 70%. For relative humidities greater than 70% the  $\text{SO}_2$  concentration becomes increasingly important.

- If the relative humidity is below 20%, the  $\text{SO}_2$  does not react with the lime.
- The lime- $\text{SO}_2$  reaction is not controlled by gas film diffusion at relative humidities of 92% or lower.
- The reaction controlled unreacted core model can be used to describe the dependence of the reaction rate on lime conversion after the conversion has reached a certain value  $X_B'$ . Before this lime conversion  $X_B'$ , the rate of reaction decreases much faster than can be predicted by a simple shrinking core model. The authors attributed this decrease in reaction rate to a decrease in surface roughness of the solid reactant.

Klingspor and coworkers obtained the initial reaction rate for the reaction of slaked lime and  $\text{SO}_2$  by extrapolating to time zero the data obtained in their fixed bed reactor. In the experiments run in the present research it was found that the reaction rate was extremely fast at initial times, so an extrapolation procedure was not considered reliable.

Acurex Corporation also conducted studies of the  $\text{Ca}(\text{OH})_2$ - $\text{SO}_2$  reaction in a bench-scale sand bed reactor (Acurex, 1985, Jorgensen et al., 1986). Some of their conclusions are:

- $\text{Ca}(\text{OH})_2$  conversion (mols  $\text{SO}_2$  removed/mol  $\text{Ca}(\text{OH})_2$ ) has a very strong dependence on relative humidity.
- There is no clear indication of increasing conversion rate with increasing  $\text{SO}_2$  concentration in the concentration range tested (500-1000 ppm) for relative humidity less than 70%.
- Conversion rate is increased moderately with temperature for a given relative humidity in the relative humidity range

tested (30-75%). An Arrhenius plot for measured reaction rates at 55% relative humidity gives an activation energy of 6000 cal/mol.

### 3.2.2 Results from Spray Drying Pilot Plants

The effect of process variables on SO<sub>2</sub> removal have been reported for a number of spray drying pilot and demonstration plants, but only a few of the reported results separate SO<sub>2</sub> removal in the bag filters from removal in the spray dryer (Stevens, 1981, Samuel et al., 1983, Samuel et al., 1984, Robards et al., 1985, Bresowar et al., 1981, Blythe and Rhudy, 1984) The most important variable affecting SO<sub>2</sub> removal in the bag filters is the stoichiometric ratio (or ratio of lime to SO<sub>2</sub> feed to the spray dryer). These results are not surprising because at low stoichiometric ratio (below 0.8) practically all the lime is consumed in the spray dryer, leaving no lime available for reaction with SO<sub>2</sub> in the bag filters. When the stoichiometric ratio increases, more unreacted lime leaves the spray dryer, because the SO<sub>2</sub> removal in the spray dryer does not increase significantly as the reagent ratio increases. This unreacted lime reacts with SO<sub>2</sub> in the bag filters, thus greatly increasing the bag filter contribution to the total SO<sub>2</sub> removal (Blythe and Rhudy, 1984).

The other variable that affects the SO<sub>2</sub> removal in the bag filters is the approach to the adiabatic saturation temperature at the spray dryer outlet, although this variable has been reported to have a smaller impact on the bag house performance than on the spray dryer removal efficiency (Robards et al., 1985). It must be noted though, that when the approach to the adiabatic saturation temperature is very low, the absorber efficiency is also improved, and there is little residual SO<sub>2</sub> in the flue gas left for the bag filters to remove (Bresowar et al., 1981).

Other process variables that affect the spray dryer removal efficiency, such as  $\text{SO}_2$  concentration in the inlet flue gas, liquid to gas (L/G) ratio in the spray dryer, or recycle ratio of solids have been reported to have a negligible effect on  $\text{SO}_2$  removal in the bag filters (Bresowar et al., 1981, Blythe and Rhudy, 1984).

### 3.3 Experimental Apparatus

The general design of the experimental apparatus is given in Figure 3-1. A simulated flue gas was synthesized by combining nitrogen and sulfur dioxide from gas cylinders. The gas flow rates were measured using rotameters (a Lab Crest Century for the nitrogen and a Gilmont micro-flow meter with a capillary valve for the sulfur dioxide). Water was added to the system by means of a syringe pump (Sage Instruments, Model 341A) and evaporated at  $120^\circ\text{C}$  in a stainless steel evaporation chamber before mixing with the gas stream.

The evaporation chamber was cylindrical, 5 cm diameter and 14 cm height. Heating was provided by electric wire wrapped around the chamber and insulated with asbestos tape. Heating was modulated by a voltage controller. The evaporation chamber was filled with 5 mm glass beads, to increase the contact surface. The temperature in the center of the evaporation chamber was measured using an Omega digital thermometer (Model 199) with a Chromel-Alumel thermocouple.

The reactor was made of glass, and it had a diameter of 4 cm and 12 cm height. The reactor was packed with a mixture of silica sand and  $\text{Ca}(\text{OH})_2$  reactant in a weight ratio of 40:1. The addition of sand is necessary to avoid channeling caused by lime agglomeration (Karlsson et al., 1983). The silica sand (between 80 and 115 mesh) was obtained from Martin Marietta Aggregates.

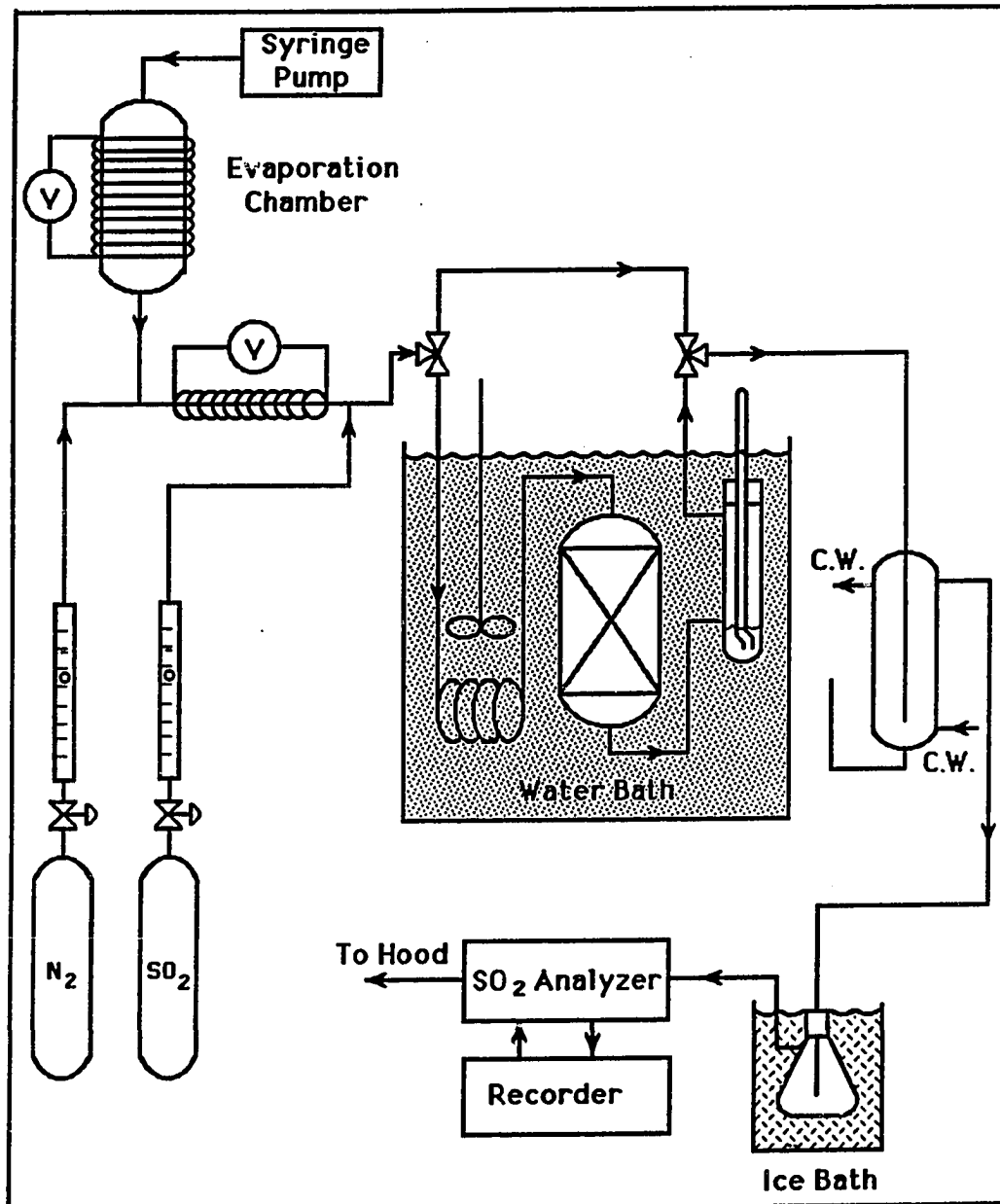


Figure 3-1: Experimental Apparatus

The reactor was immersed in a water bath that maintained the system temperature within  $0.1^{\circ}\text{C}$ . Tubing upstream from the reactor was heated to prevent the condensation of moisture on the walls. After leaving the reactor, the wet bulb temperature of the gas was measured using a mercury thermometer with a wet cloth at the tip. The mercury thermometer was placed in a small Dewar container. Before going to analysis the gas was cooled and the water then condensed out by cooling water and an ice bath. The gas was analyzed for  $\text{SO}_2$  using a pulsed fluorescent  $\text{SO}_2$  analyzer (Thermoelectron Corporation model 40) and the concentration was continuously recorded. The  $\text{SO}_2$  analyzer was calibrated using a calibration standard (a mixture of 2000 ppm  $\text{SO}_2$  and  $\text{N}_2$ ). The reactor was equipped with a bypass, to allow the bed to be preconditioned and to allow the gas flow to be stabilized at the desired  $\text{SO}_2$  concentration before beginning the experimental run. Prior to each experimental run the bed was humidified by flushing with pure nitrogen at a relative humidity of about 98% for 10 minutes then later with pure nitrogen at the relative humidity at which the experiment was to be performed for 8 minutes. This was done to simulate the moisture conditions encountered in the bag filters where the solids are originally slurry droplets.

The reaction time was normally 1 hour. The raw data from each experimental run was a curve of  $\text{SO}_2$  concentration leaving the reactor versus time. This curve was given by the recorder of the  $\text{SO}_2$  analyzer.

### 3.4 Analysis of the Experimental Data

The raw data from the experiments is  $\text{SO}_2$  concentration from the reactor as a function of time. By integration of the  $\text{SO}_2$  concentration over time and a mass balance on the reactor the average fraction of lime converted can be calculated at each time. A sample calculation can be found in Appendix D. As a backup, the reacted solids are analyzed for sulfite and hydroxide using acid/base and iodine titrations described in Appendix A.

The relative humidity of the gas stream was calculated from the amount of water injected by the syringe pump and the gas flow rate. The wet-bulb temperature measurement was not accurate enough to calculate relative humidity. Heat flow from the water bath was reduced by the use of a Dewar container but not eliminated. As a consequence, the wet-bulb temperature measured was systematically higher than the one corresponding to the relative humidity calculated from the injected water. Even with this systematic error the wet-bulb temperature was useful to check that the relative humidity remained constant during the experiment.

### 3.5 Reagent Used

Most of the experimental work was done using  $\text{Ca}(\text{OH})_2$  powder reagent A.C.S. (Matheson Coleman & Bell Manufacturing Chemist) as the reactant. The  $\text{Ca}(\text{OH})_2$  has maximum impurities of 1.213 wt%, the main impurity being magnesium and alkali salts (1% expressed as sulfates). Two batches of  $\text{Ca}(\text{OH})_2$  that will be identified as lime 0 and lime A were used. These two batches of  $\text{Ca}(\text{OH})_2$  differ slightly in particle size and BET surface area as shown in 3-1. The particle size

distribution was measured using a Coulter Counter model T<sub>AII</sub>, and the BET surface area by nitrogen adsorption isotherms in a Physical Adsorption Analyzer (Accusorb Model 2100E). The complete particle size distribution of the two Ca(OH)<sub>2</sub> used as well as details of the BET area measurement can be found in Appendix A, Sections A.1 and A.2. Also shown in Appendix A (Section A.3) are Scanning Electron Microscope pictures of lime 0 and lime A. The use of these two different batches of Ca(OH)<sub>2</sub> was not by choice, but rather forced by the depletion of the first batch of Ca(OH)<sub>2</sub> (lime 0).

A few experimental runs were also made using high surface area, pressure-hydrated dolomitic lime as the reactant. The chemical composition of the dolomitic lime is not exactly known but analysis made using Energy Dispersive Spectrometry (EDS) and X-Ray Powder Diffraction, as well as measured alkalinity (by acid/base titration) indicate it is composed mainly of Mg(OH)<sub>2</sub> and Ca(OH)<sub>2</sub> with small amounts of unhydrated MgO and CaO. The EDS and x-ray analysis results are discussed in detail in Appendix A (Sections A.4 and A-6). For the conversion calculation the dolomitic lime was assumed to consist of 40 mole% Mg(OH)<sub>2</sub> and 60 mole% Ca(OH)<sub>2</sub>. Three samples of pressure-hydrated dolomitic lime (provided by Dr John Chang, Acurex, 1984) differing in particle size and BET surface area were used. One sample was taken when the dolomitic lime left the hydrator (Hydrator lime), another when the dolomitic lime left the ball mill (Ball mill lime), and the last one corresponds to ball mill lime dry sieved through a 125 μm sieve. The BET surface areas of the dolomitic limes are given in Table 3-1.

**Table 3-1: Particle Size and BET Surface Area of Reactant**

Reactant	Coulter Counter Median Particle Size ( $\mu\text{m}$ )	BET Surface Area ( $\text{m}^2/\text{g}$ )
Reagent $\text{Ca}(\text{OH})_2$		
Lime 0	7.4	8.2
Lime A	5.6	9.4
Lime A (slurried)	-	8.8
Pressure Hydrated Dolomitic Lime		
after hydrator	-	20.1
after ball mill	-	21.1
sieved material after ball mill ( $< 125 \mu\text{m}$ )	-	18.4

### 3.6 Experimental Results

The effects of relative humidity, temperature, inlet  $\text{SO}_2$  concentration, and amount of lime in the reactor on the reaction of  $\text{SO}_2$  with powdered reagent  $\text{Ca}(\text{OH})_2$  were studied in the sand reactor described in Section 2.3. The experimental conditions were similar to the ones encountered in the bag filters during spray drying flue gas desulfurization. Table 3-2 shows the range of experimental conditions used in the experiments.

**Table 3-2: Experimental Conditions**

Relative Humidity:	17 - 90%
SO <sub>2</sub> Inlet Concentration:	500 - 4000 ppm
Reactor Temperature:	30.5 - 95°C
Nitrogen Flow Rate:	4600 cm <sup>3</sup> /min (0°C, 1 atm)
Amount of Lime:	1.0 - 4.0 g

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### 3.6.1 Effect of Relative Humidity

The relative humidity was found to have a dramatic effect on the rate of reaction of SO<sub>2</sub> with Ca(OH)<sub>2</sub>. Figure 3-2 shows lime conversion as a function of time at 19, 50 and 70% relative humidity. All three experiments were run at 2000 ppm inlet SO<sub>2</sub> and 66°C using 4 g of lime 0. The dashed line in the figure corresponds to the Ca(OH)<sub>2</sub> that would be converted if all the SO<sub>2</sub> were being removed. Figure 3-2 shows that for all relative humidities, 100% of the SO<sub>2</sub> is removed during the first one or two minutes of reaction, then the reaction rate decreases quickly at low relative humidities but slower at high relative humidities.

The same kind of behavior was observed with the other batch of Ca(OH)<sub>2</sub> (lime A) which differs slightly in particle size and BET surface area. Figure 3-3 shows the Ca(OH)<sub>2</sub> conversion versus time for 1 g of lime A, at relative humidities of 54 and 74%. The inlet SO<sub>2</sub> concentration was 500 ppm. Some "differential experiments" were also

performed at these two relative humidities. The differential experiments were run using a very small amount of  $\text{Ca(OH)}_2$  in the reactor (0.125 g) so that the  $\text{SO}_2$  concentration did not change significantly across the reactor. In these experiments, the integration of the  $\text{SO}_2$  removed was not accurate enough to determine the lime converted, so chemical analysis of the solids at different times was used instead. Figure 3-4 shows the results of these experiments, and even though there is some scattering of the data it is obvious that the relative humidity is strongly affecting the reaction rate.

The fact that the rate of reaction is a very strong function of the relative humidity of the gases agrees with the findings of Klingspor and coworkers (Klingspor et al., 1984), which reported the initial reaction rate to be an exponential function of the relative humidity. The Acurex results (Acurex, 1985, Jorgensen et al., 1986) also show an exponential type of dependence of the reaction rate with relative humidity.

### 3.6.2 Effect of Inlet $\text{SO}_2$ concentration

The effect of the inlet  $\text{SO}_2$  concentration on the reaction rate was found to depend on the relative humidity. At 70% relative humidity the  $\text{Ca(OH)}_2$  conversion was practically independent of the inlet  $\text{SO}_2$  concentration as illustrated by Figure 3-5. At lower relative humidity the reaction rate is not affected by the  $\text{SO}_2$  concentration if the  $\text{SO}_2$  concentration is high. However, at lower levels of  $\text{SO}_2$  the reaction rate is affected by the  $\text{SO}_2$  concentration as illustrated by Figure 3-6 which shows the  $\text{Ca(OH)}_2$  conversion at 50% relative humidity. These results are not in disagreement with the findings of Klingspor and coworkers (Klingspor et al., 1984) who reported the initial

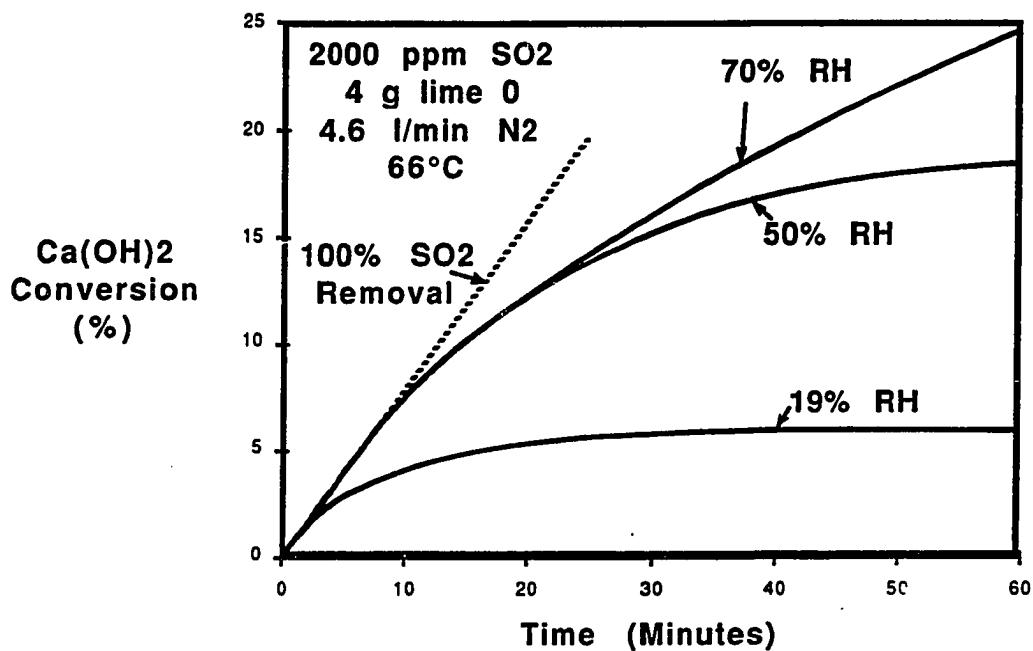


Figure 3-2: Lime 0, Effect of Relative Humidity

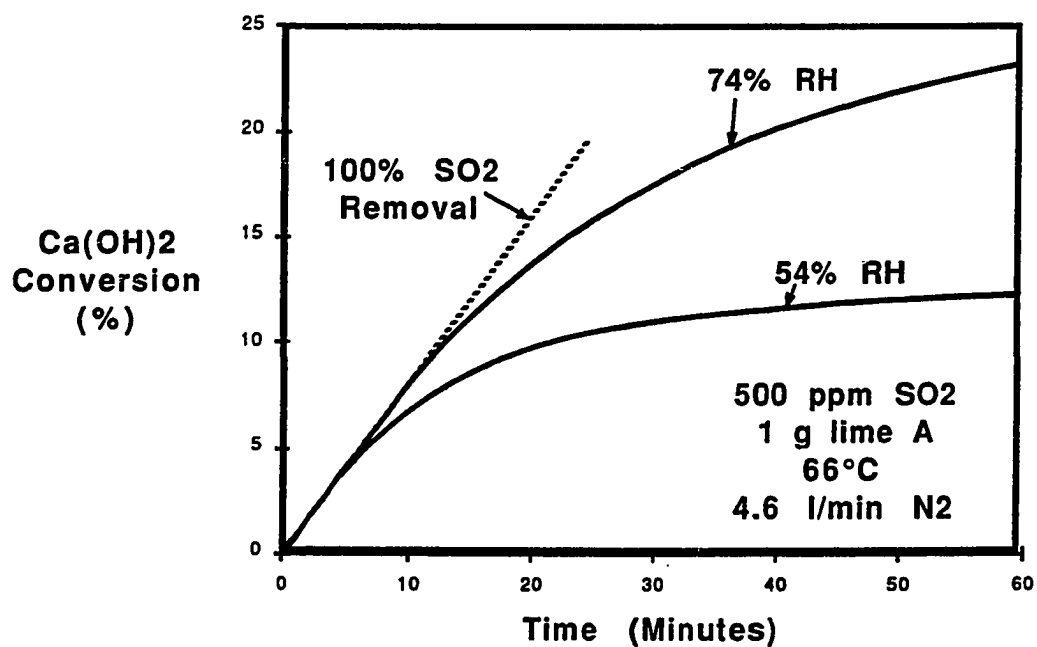
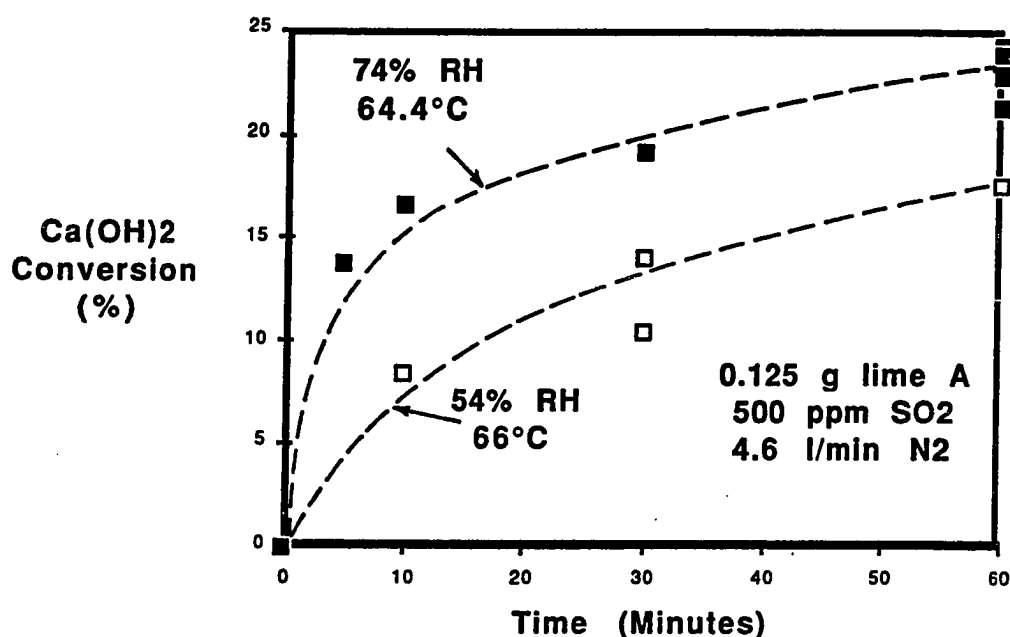


Figure 3-3: Lime A, Effect of Relative Humidity



**Figure 3-4:** Differential Experiments, Effect of Relative Humidity

reaction rate to be zero order in  $\text{SO}_2$  for relative humidities of 70% or lower. They measured initial reaction rate, that is reaction rate when no product has been formed. At this condition the reaction is kinetically controlled, because there is no diffusion through product layer or pore plugging to consider. In the present research the reaction was carried out for 1 hour, so that a considerable amount of product was produced. Under this condition, diffusion of the  $\text{SO}_2$  through the product layer can become important so the overall reaction rate may be dependent on the  $\text{SO}_2$  concentration even when the kinetic rate is zero order in  $\text{SO}_2$ . The fact that at low relative humidities and low  $\text{SO}_2$  levels the  $\text{SO}_2$  concentration affects the reaction rate could be explained by assuming that at these conditions mass transfer becomes the controlling step instead of chemical reaction.

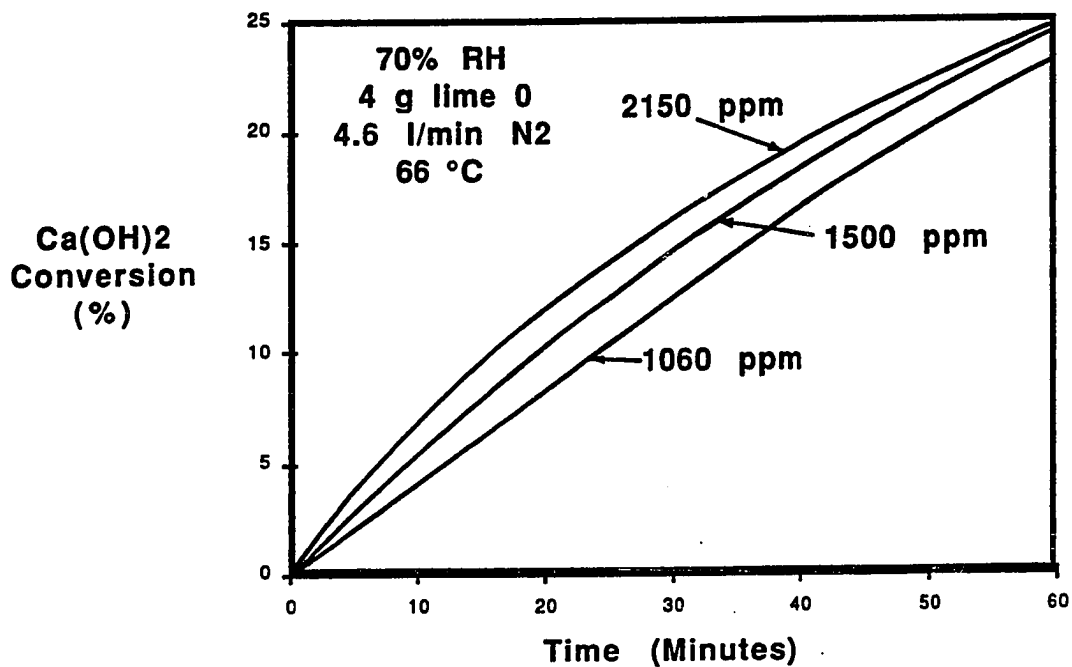


Figure 3-5: Effect of SO<sub>2</sub> Concentration, High Relative Humidity

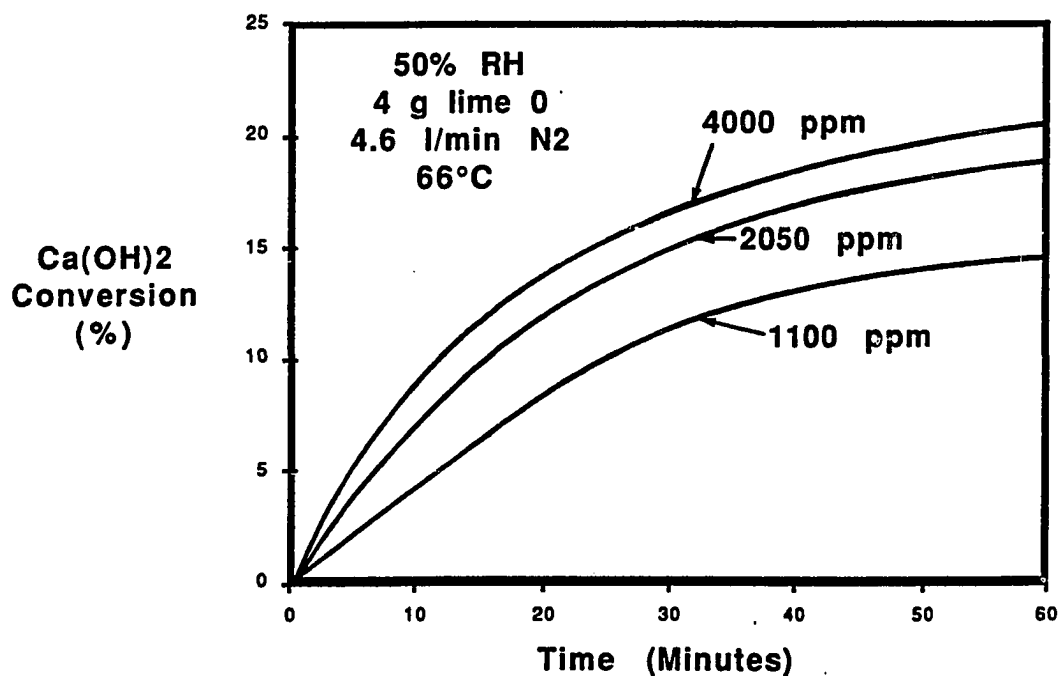


Figure 3-6: Effect of SO<sub>2</sub> concentration, Low Relative Humidity

### 3.6.3 Effect of Amount of $\text{Ca}(\text{OH})_2$ in the Reactor

The effect on the average  $\text{Ca}(\text{OH})_2$  conversion of changing the amount of  $\text{Ca}(\text{OH})_2$  in the reactor is illustrated by Figures 3-7 and 3-8 which show the  $\text{Ca}(\text{OH})_2$  conversion when the amount of lime 0 in the reactor was reduced from 4 to 1 g at  $\text{SO}_2$  levels of 1000 and 2000 ppm respectively. The relative humidity was 50% on these two sets of experiments. From Figure 3-7 it can be seen that the amount of  $\text{Ca}(\text{OH})_2$  present in the reactor makes a difference during the first minutes of reaction, but the effect is less marked at later times. These results are consistent with the effect of  $\text{SO}_2$  concentration discussed in the previous section. When more  $\text{Ca}(\text{OH})_2$  is present in the reactor, more  $\text{SO}_2$  is removed at the entrance of the reactor, so the  $\text{Ca}(\text{OH})_2$  present further down in the reactor "sees" a lower concentration of  $\text{SO}_2$ , and the reaction rate is slower. At later times when the  $\text{SO}_2$  removal is lower the amount of  $\text{Ca}(\text{OH})_2$  present will not be as important. When the  $\text{SO}_2$  concentration entering the reactor is higher, lime conversion should be less dependent on the amount of  $\text{Ca}(\text{OH})_2$  present as illustrated by Figure 3-8.

### 3.6.4 Effect of Reactor Temperature

Reactor temperature has a very moderate effect on  $\text{Ca}(\text{OH})_2$  reactivity, as illustrated by Figure 3-9, which shows the effect on  $\text{Ca}(\text{OH})_2$  conversion when the reactor temperature was increased from 30.4 to 64.4°C while keeping all other variables constant. The relative humidity was 74%, so in this region the reaction is expected to be kinetically controlled.

A very weak dependence of the reaction rate with temperature

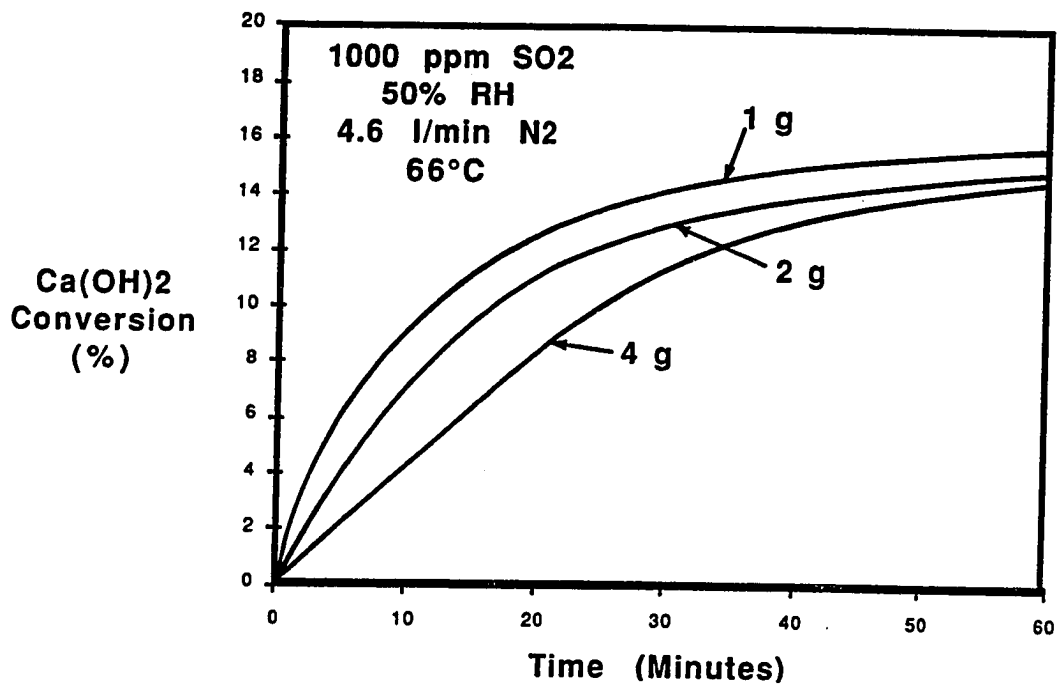


Figure 3-7: Effect of Ca(OH)<sub>2</sub> loading, 1000 ppm SO<sub>2</sub>

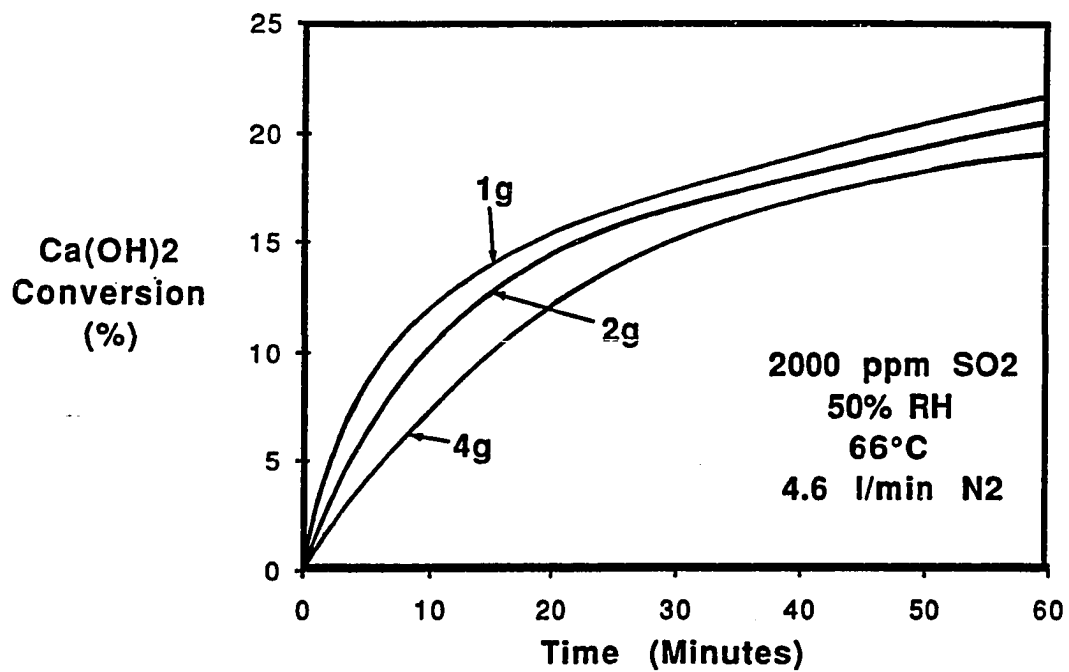


Figure 3-8: Effect of Ca(OH)<sub>2</sub> loading, 2000 ppm SO<sub>2</sub>

was also reported by Klingspor and coworkers (Klingspor et al., 1984) and by Acurex Corporation (Acurex, 1985, Jorgensen et al., 1986).

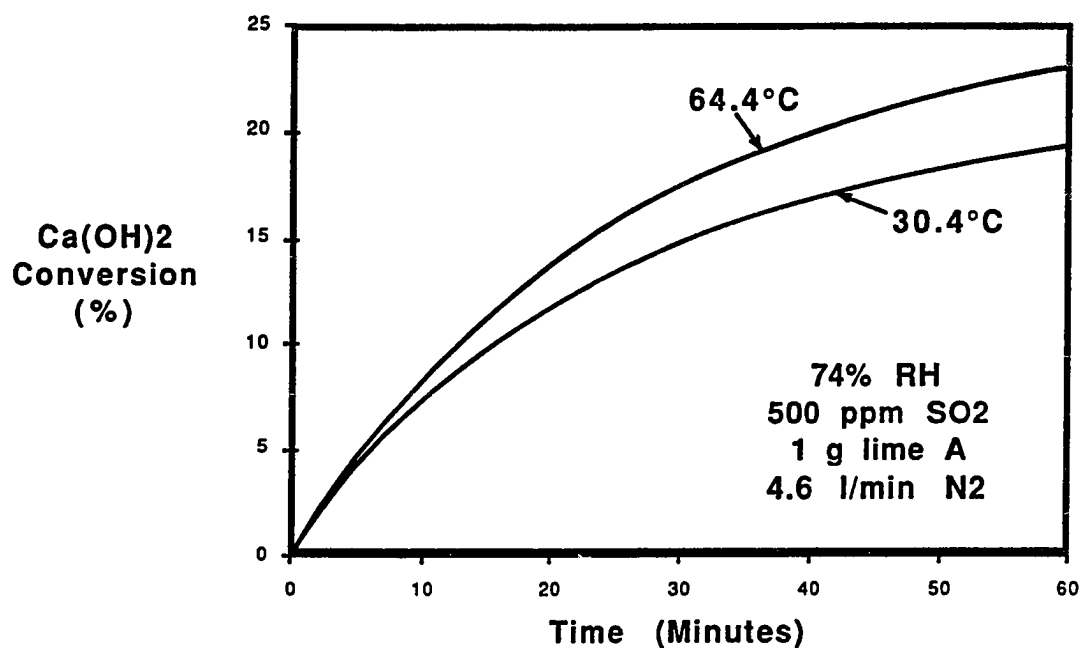


Figure 3-9: Effect of Reactor Temperature, Lime A

### 3.6.5 Other Types of Lime

A few experimental runs were made using samples of pressure hydrated dolomitic lime. The three samples differ in particle size and BET surface area.

Table 3-3 shows the average Ca(OH)<sub>2</sub> conversion after 60 minutes of reaction for the three different samples of hydrated dolomitic lime, together with the BET surface area. Also included in the table is the conversion of pure Ca(OH)<sub>2</sub> at the same experimental conditions.

The hydrator and ball mill lime are only slightly more reactive than the pure  $\text{Ca}(\text{OH})_2$ , despite having a much higher surface area (about 2 times that of pure  $\text{Ca}(\text{OH})_2$ ). When the ball mill lime was dry sieved using a  $125\ \mu\text{m}$  sieve, the reactivity of the hydrated dolomitic lime increased, even when its surface area decreased slightly.

**Table 3-3: Reactivity of Pressure Hydrated Dolomitic Lime**

74% R H, 64.4°C, 500 ppm  $\text{SO}_2$ , 1 g lime A

Type of Lime	Average Conversion after 60 Min (%)	BET Surface Area ( $\text{m}^2/\text{g}$ )
Pure $\text{Ca}(\text{OH})_2$ slurried	22	8.2
Pure $\text{Ca}(\text{OH})_2$ non-slurried	23	9.4
Hydrator Lime	24 *	20.1
Ball Mill Lime	25 *	21.1
Sieved Ball Mill Lime	31 *	18.4

\* Average hydroxide conversion assuming composition of dolomitic lime to be 40 mole%  $\text{Mg}(\text{OH})_2$  and 60 mole%  $\text{Ca}(\text{OH})_2$

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The pressure hydrated lime consisted of a few very large particles (some over  $100\ \mu\text{m}$ ), and a majority of small particles of  $1\ \mu\text{m}$  in size or lower, that tend to agglomerate (See Appendix A, Section A.3). The reactivity of the dolomitic lime may have improved after being sieved, because the large particles that were eliminated by sieving consisted mainly of dead-burned, unreactive or other unhydrated material

(MgO and CaO), that did not contribute significantly to the SO<sub>2</sub> absorption.

MgO has been reported to be usually "dead-burned" in the calcining process, and therefore will not explosively slake to form the highly reactive lime slurry needed for best results in spray absorption flue gas desulfurization (Parsons et al., 1981). Acurex Corporation (Acurex, 1985, Jorgensen et al., 1986) also tested some pressure hydrated dolomitic limes and found them to show somewhat lower conversion with SO<sub>2</sub> after 1 hr of reaction in comparison with reagent grade Ca(OH)<sub>2</sub>.

## Chapter 4

### Effect of Additives

#### 4.1 Introduction

The experimental results discussed in Chapter 3, as well as results from other sources (Klingspor et al., 1984, Acurex, 1985) indicate that the relative humidity of the gases has the greatest impact on the rate of absorption of  $\text{SO}_2$  by  $\text{Ca}(\text{OH})_2$ . The relative humidity is in turn correlated with the moisture content of the solids. Additives that will modify the moisture content of the  $\text{Ca}(\text{OH})_2$  solids in equilibrium with a gas phase of a given relative humidity would then be expected to change the reactivity of the  $\text{Ca}(\text{OH})_2$  towards  $\text{SO}_2$ . The present research was undertaken to investigate in a systematic manner the kind of additives that could be used to improve the  $\text{Ca}(\text{OH})_2$  reactivity. The small fixed bed reactor described in Section 3.3 was used to collect the data. Three different kind of additives were tried: buffer acids, organic deliquescents, and inorganic deliquescents.

## 4.2 Previous Research

### 4.2.1 Bench-Scale Fixed Bed Reactor

Some inorganic and organic compounds like sodium sulfite,  $\text{Fe}^{++}$  compounds, ethylene-diamine tetra-acetic acid (EDTA), and its disodium salt have been tested as additives for slaked lime during simultaneous  $\text{SO}_2/\text{NO}_x$  removal (Niro Process) (Felsvang et al., 1984) in a bench scale fixed bed reactor. The emphasis in the Niro process was to improve the  $\text{NO}_x$  removal rather than the  $\text{SO}_2$  removal.

Acurex Corporation tested  $\text{CaCl}_2$ ,  $\text{NaCl}$ , and  $\text{NaOH}$  as additives to improve the reactivity of hydrated lime towards  $\text{SO}_2$  in a fixed bed reactor (Acurex, 1985, Jorgensen et al., 1986). Increased reactivity was reported for  $\text{CaCl}_2$ ,  $\text{NaOH}$  and  $\text{NaNO}_3$ , but in the case of  $\text{NaCl}$  a slight decrease in the conversion was observed. The additives were added to the hydrated lime samples by dry mixing.

Karlsson et al. (1983), tried a number of deliquescent salts as additives for limestone in a small fixed bed reactor. Most of the halides tried (chlorides of Zn, Sn, Pd, Ca, Al, Ru, Fe, Ti, Te, and Pt,  $\text{CaBr}$ ,  $\text{CaI}_2$ , and  $\text{NiBr}$ ) were successful in promoting the reaction of limestone and  $\text{SO}_2$ , the exception being the chlorides of Mg, Mn, and Ce. None of the nitrates tried (nitrates of Ca, Mn, Cu, Fe, and Al) enhanced the reaction. After economic and secondary environmental considerations, the authors selected  $\text{CaCl}_2$  as the most promising candidate for use in a spray drying bag filter system. Based on their results for limestone Karlsson et al. then tried  $\text{CaCl}_2$  as an additive for  $\text{Ca}(\text{OH})_2$  in the same reactor. They found the  $\text{CaCl}_2$  to have some promoting effect on the reaction of  $\text{Ca}(\text{OH})_2$  with  $\text{SO}_2$ , but not to the same degree as in the limestone case.

Stouffer et al. (1985) reported some laboratory work in a glass tube differential reactor using slaked lime with a number of water soluble inorganic and organic additives, including  $\text{CaCl}_2$ ,  $\text{NaFeCl}_4$ ,  $\text{NaOH}$ ,  $\text{NaCl}$ ,  $\text{Na}_2\text{CO}_3$  and adipic acid. The objective of this laboratory work was to identify an active sorbent/additive system for use in the coolside desulfurization technique under development at Conoco Coal Research Division. They found  $\text{NaOH}$  and  $\text{Na}_2\text{CO}_3$  to be the most effective additives. At 60% relative humidity, 150°F and 1000 ppm  $\text{SO}_2$  the sorbent utilization at 60 minutes of reaction increased from 30 to 42% and 53% with the addition of 5 and 10 mole%  $\text{Na}_2\text{CO}_3$  respectively.

#### 4.2.2 Spray-Dryer Pilot Plants

Karlsson et al. (1983) performed tests in a 0.5 MW spray dryer with a slaked lime stoichiometry of one at 20 to 70% relative humidity. They found that the addition of 4 mole%  $\text{CaCl}_2$  increased  $\text{SO}_2$  removal by about 25% from 45-80% to 70-98%. Unfortunately, they did not indicate how much of the removal takes place in the spray dryer itself, and how much in the bag filters used for collection of the solid products. It is not then clear if the  $\text{CaCl}_2$  improves the rate of absorption during the wet phase that takes place in the spray dryer, or if the improvement occurs mainly in the "dry stage" that takes place in the bag filters.

Rhudy and Blythe (1985) presented results of  $\text{CaCl}_2$  addition tests conducted at the Arapahoe EPRI spray dryer/bag filter pilot scale test facility (21/2 MW). The tests were conducted at high  $\text{SO}_2$  levels (2000 and 3000 ppm), 20°F approach to the adiabatic saturation temperature at the spray dryer outlet (60% relative humidity), and with

chloride levels of 0.4 and 0.8 wt% in the fabric filter solids collected. With 2000 ppm inlet SO<sub>2</sub> and a reagent stoichiometric ratio of around 1.1 the overall SO<sub>2</sub> removal increased from 85 to 92% with the addition of 0.4 wt% of CaCl<sub>2</sub> and from 85 to 98% when 0.8% CaCl<sub>2</sub> was added. With 3000 ppm SO<sub>2</sub>, the SO<sub>2</sub> removal increased from 85 to 92% when 0.8 wt% CaCl<sub>2</sub> was added. At a reagent ratio of 1.1 the improvement in SO<sub>2</sub> removal was evenly split between the spray dryer and the fabric filters. When the reagent ratio was higher (1.3 to 1.4), the benefit appears to lie entirely in the spray dryer. This observation is misleading, though, because overall removal levels of essentially 100% were observed. So, even when the bag filter contribution to the overall removal is not increased, the bag filter is removing 100% of the SO<sub>2</sub> reaching the bags. Thus, CaCl<sub>2</sub> addition appears to result in improved lime utilization and/or increased SO<sub>2</sub> removal capabilities in high sulfur operations.

However, some potentially negative impacts on the operation and maintenance of the spray dryer bag filter system were also reported. There was an increase in the pressure drop across the bag filters following the CaCl<sub>2</sub> addition, some chloride related stress corrosion cracking was detected on the 300 series stainless steel bag clamps, and changes occurred on the solid waste disposal properties (the unconfined compressibility values for wetted, compacted and cured samples of waste solid decreased when CaCl<sub>2</sub> was added). These potential problems need to be further investigated before CaCl<sub>2</sub> can be implemented on a full scale system.

Adipic acid has also been tested as an additive in spray dryer pilot plants, but the results were not very conclusive. When the spray dryer system was operated without solids recycle, the adipic acid did not

show a significant effect on the SO<sub>2</sub> removal efficiency (Parsons et al., 1981, Yeh et al., 1983). Some improvement of the removal efficiency was reported when the system was operated with solids recycle and 3000 ppm of adipic acid in the feed (Parsons et al., 1981). Because of the recycle the total concentration of adipic acid in the system increases due to recovery of residual adipic acid in the waste product. The results were reported as overall SO<sub>2</sub> removal, so it is not clear if the SO<sub>2</sub> removal in the bag filters was affected or not.

Some patents have been issued that involve the use of salt additives to improve the reactivity of Ca(OH)<sub>2</sub> towards SO<sub>2</sub> in spray drying bag filter systems. Lindau and Ahman (1980) patented the use of FeCl<sub>2</sub>, Fe(NO<sub>3</sub>)<sub>2</sub>, Fe(NO<sub>3</sub>)<sub>3</sub>, Al(NO<sub>3</sub>)<sub>3</sub>, Ca(NO<sub>3</sub>)<sub>2</sub>, Mg(ClO<sub>3</sub>)<sub>2</sub>, MnCl<sub>2</sub>, KSO<sub>4</sub>, NaAl(SO<sub>4</sub>)<sub>2</sub>, NaClO, Na<sub>3</sub>PO<sub>4</sub>, Na<sub>2</sub>SiO<sub>3</sub>, NaSO<sub>4</sub>, and Zn(NO<sub>3</sub>)<sub>2</sub>. Niro Atomizer included a claim involving the use of NaCl to improve the reactivity of slaked lime in their spray drying system with solids and fly ash recycle (Felsvang, Hansen and Rasmussen, 1981).

### 4.3 Experimental Apparatus

The experimental apparatus used in the additive experiments was the same as that used in the experiments with no additives and it was described in Chapter 3, Section 3.3.

#### 4.4 Reactants

Most of the experiments with additives were run using reagent grade  $\text{Ca}(\text{OH})_2$  (Lime A). Lime A has a BET surface area of  $9.4 \text{ m}^2/\text{g}$  and a median particle size of  $5.6 \mu\text{m}$  (determined by Coulter Counter). One experimental run was also made using pressure hydrated dolomitic lime (Sieved Ball Mill Lime) with a BET surface area of  $18.4 \text{ m}^2/\text{g}$  and an approximate composition of 40 mole%  $\text{Mg}(\text{OH})_2$  and 60 mole%  $\text{Ca}(\text{OH})_2$ . More details about size and surface area of these two limes along with Scanning Electron Microscope pictures of the  $\text{Ca}(\text{OH})_2$  and dolomitic lime particles can be found in Appendix A.

#### 4.5 Preparation of the Samples with Additives

An aqueous solution containing the desired additive was prepared. Five ml of this solution were then added to 1 g of  $\text{Ca}(\text{OH})_2$  and slurried. The sample was placed in an oven to dry at  $75^\circ\text{C}$  for about 14 hours then later sieved to separate the individual  $\text{Ca}(\text{OH})_2$  particles prior to mixing with the silica sand and being placed in the reactor.

#### 4.6 Organic Acids as Additives

Organic acids have been successfully used as additives to enhance lime and limestone scrubbing (Rochelle and King, 1977, Burbank et al., 1984, Rochelle et al., 1982, Chang and Rochelle, 1982, Burke et al., 1985, Glover et al., 1985). Organic acids buffer the pH in the lime/limestone  $\text{SO}_2$  absorbers, and improve the  $\text{SO}_2$  removal efficiency. The buffering action limits the drop in pH at the gas/liquid interface during  $\text{SO}_2$  absorption, and the resultant higher concentration of  $\text{SO}_2$  at the interface accelerates the liquid-phase mass transfer.

Two organic acids were selected as test additives for the reaction of  $\text{Ca}(\text{OH})_2$  with  $\text{SO}_2$ , adipic acid because of its extensive use in wet scrubbing, and glycolic acid, because of its deliquescent properties.

Both of these acids proved to be detrimental to the reaction of  $\text{Ca}(\text{OH})_2$  with  $\text{SO}_2$ , as can be seen from Table 4-1. At 74% relative humidity the average  $\text{Ca}(\text{OH})_2$  conversion in the reactor after 1 hour of reaction decreased from 22 to 11% when 5 wt% of glycolic acid was added to the  $\text{Ca}(\text{OH})_2$ , and from 22 to 20% when 1 wt% adipic acid was used as an additive.

**Table 4-1: Effect of Organic Acids and Organic Deliquescents on  $\text{Ca}(\text{OH})_2$  Reactivity**

500 ppm  $\text{SO}_2$ , 1.0 g lime A, 74% RH, 64.4°C, 4.6 l/min  $\text{N}_2$

Additive	Average $\text{Ca}(\text{OH})_2$ conversion after 1 hour (%)
None	22.4
<b>ORGANIC ACIDS</b>	
5 wt% Glycolic Acid	11.3
1 wt% Adipic Acid	20.3
<b>ORGANIC DELIQUESCENTS</b>	
5 wt% Monoethanolamine	19.6
5 wt% Ethylene Glycol	20.3
5 wt% TEG	20.5

#### 4.7 Organic Deliquescents as Additives

Ethylene glycol (EG), tri-ethylene glycol (TEG), and monoethanolamine (MEA), were selected to be tested as additives for the  $\text{Ca(OH)}_2$  due to their deliquescent or hygroscopic properties. Because of their high hygroscopicity, ethylene glycol and tri-ethylene glycol are commonly used as desiccants for natural gas (NGPSA, 1966). Ethylene glycol is also used as an antifreeze and as a refrigerant (Perry and Chilton, 1973, Kirk-Othmer, 1980). Monoethanolamine is used in scrubbing  $\text{H}_2\text{S}$  and  $\text{CO}_2$  from petroleum gas streams (NGPSA, 1966).

The experimental results of runs made adding 5 wt% of ethylene glycol, TEG, or MEA to the  $\text{Ca(OH)}_2$  are presented in Table 4-1. At a relative humidity of 74% all three additives slightly decreased the average  $\text{Ca(OH)}_2$  conversion after 1 hour of reaction, when compared with the conversion of pure  $\text{Ca(OH)}_2$  at the same experimental conditions.

#### 4.8 Inorganic Deliquescents as Additives

A number of deliquescent salts were tested as additives to improve the  $\text{Ca(OH)}_2$  reactivity towards  $\text{SO}_2$ . These inorganic salts were selected according to their deliquescent properties, or lowering of the water vapor pressure over their saturated solutions. The salts were added to the  $\text{Ca(OH)}_2$  by the slurring and drying process described in Section 4.5. X-ray analysis of the samples showed that most of the salts tried remained unchanged after this mixing procedure. However, with  $\text{CaCl}_2$  and  $\text{Ca(NO}_3)_2$  the less deliquescent solid phases,  $\text{Ca(OH)}_2 \cdot \text{CaCl}_2 \cdot \text{H}_2\text{O}$  and  $\text{Ca}_2\text{N}_2\text{O}_7 \cdot 2\text{H}_2\text{O}$  were formed. The presence of  $\text{Ca(OH)}_2 \cdot \text{CaCl}_2 \cdot \text{H}_2\text{O}$  was confirmed by x-ray powder diffraction analysis

**Table 4-2: Effect of Deliquescent Salts in  $\text{Ca}(\text{OH})_2$  Reactivity and Deliquescent Properties of the Salts**

500 ppm  $\text{SO}_2$ , 1.0 g lime A, 4.6 l/min ( $0^\circ\text{C}$ , 1 atm)  $\text{N}_2$

Additive (Mole%)	Ca(OH) <sub>2</sub> Conversion at 60 minutes (%)		Water Activity over Saturated Solutions	
	74% RH 64.4°C	54% RH 66°C	at 25°C	at 70°C
None	22.4	11.8	-	-
5% $\text{Na}_2\text{SO}_4$	28.3	-	.93 (4)	.887 (1)
5% $\text{Na}_2\text{SO}_3$	29.8	16.1	.95 (4)	-
5% $\text{CaCl}_2$ (**)	34.6	16.4	.850 (1)	.686(1)
10% NaCl	38.5	27.0	.753 (2)	.751 (3)
5% $\text{Ca}(\text{NO}_3)_2$ (**)	39.4	12.3	-	.553 (*,1)
5% $\text{Co}(\text{NO}_3)_2$		13.2		
10% $\text{NaNO}_2$	40.0	-	.66 (4)	.593(3)
10% $\text{NaNO}_3$	41.5	27.2	.738 (2)	.657 (3)
5% $\text{BaCl}_2$	-	19.4	.902 (2)	.876 (1)
5% $\text{Na}_2\text{S}_2\text{O}_3$	-	21.6	.78 (3)	.298(1)
10% KCl	-	37.3	.842 (2)	.80 (3)
10% NaBr	-	42.0	.577 (2)	.507 (3)
10% LiCl	-	43.9	.112 (2)	.099 (1)
100% $\text{SO}_2$ Removal	48.2	48.2		

(\*) data at  $100^\circ\text{C}$ .

(\*\*) Solid phases were  $\text{CaCl}_2 \cdot \text{Ca}(\text{OH})_2 \cdot \text{H}_2\text{O}$  and  $\text{Ca}_2\text{N}_2\text{O}_7 \cdot 2\text{H}_2\text{O}$  respectively.

(1) Source (National Research Council, 1930)

(2) Source (Stokes and Robinson, 1949)

(3) Source (Lange, 1961)

(4) Source (Lange, 1961) data at  $20^\circ\text{C}$ .

of the sample. The presence of  $\text{Ca}_2\text{N}_2\text{O}_7 \cdot 2\text{H}_2\text{O}$  could not be confirmed by x-ray analysis as the diffraction pattern of this solid phase was not available, but it was confirmed that neither  $\text{Ca}(\text{NO}_2)_2$  nor any of its hydrates was present. Details of the x-ray diffraction work can be found in Appendix A, Section A.6.

The results of experimental runs using salts as additives are presented in Table 4-2 as average  $\text{Ca}(\text{OH})_2$  conversion after 1 hour of reaction. Runs were made at 54 and 74% relative humidity. As can be seen from Table 4-2 all of the salts tried were successful in increasing the  $\text{Ca}(\text{OH})_2$  reactivity, but their effectiveness depended on the amount of additive added, the type of salt, and the relative humidity at which the experiment was performed. The prehumidification of the bed prior to each experimental run also affected the results.

#### 4.8.1 Effect of Amount of Additive

Figure 4-1 illustrates the effect of the amount of additive added on  $\text{Ca}(\text{OH})_2$  reactivity.  $\text{Ca}(\text{OH})_2$  conversion increases as the  $\text{NaCl}$  or  $\text{NaNO}_3$  concentration increases from 0 to 10 mole%. Further increase of the amount of additive to 15 mole% does not improve  $\text{Ca}(\text{OH})_2$  reactivity. The optimal amount of additive appears to be about 10 mole% for 1:1 electrolytes such as  $\text{NaCl}$  and  $\text{NaNO}_3$ , and that was the concentration used in the experiments. For 2:1 and 1:2 salts, 5 mole% was used because it gives about the same level of deliquescence.

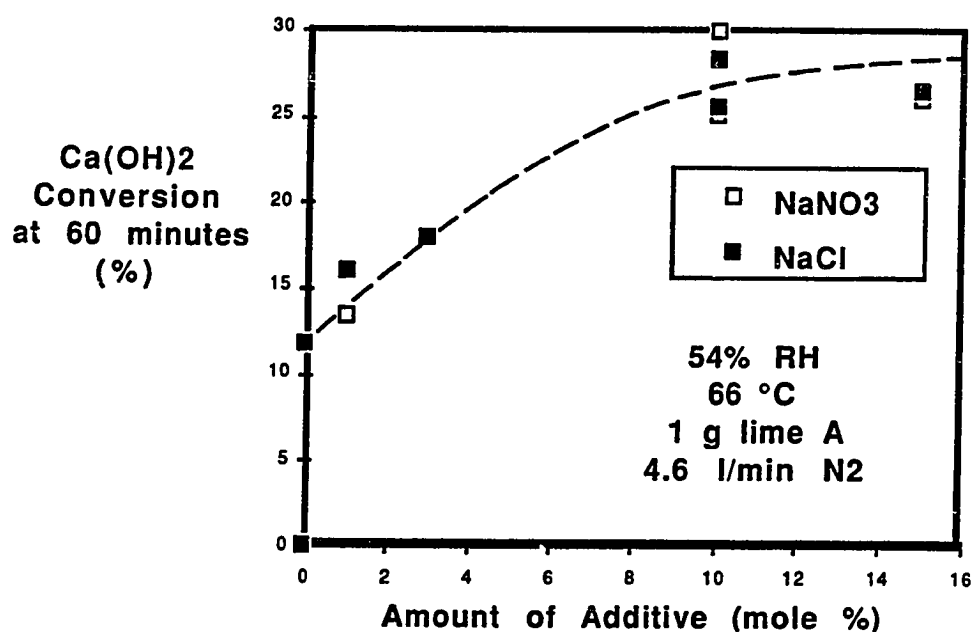


Figure 4-1: Effect of Amount of Additive on Ca(OH)<sub>2</sub> Reactivity

#### 4.8.2 Effect of Type of Deliquescent Salt

Also presented in Table 4-2 are the deliquescent properties of the salts expressed as water activity in saturated solutions of the salt at 25 and 70°C and 1 atm. The water activity is approximately equal to the relative humidity of the gas phase in equilibrium with the saturated solution.

If one of these deliquescent salts is contacted with a gas phase of relative humidity greater than the water activity, the salt will capture water from the gas phase and become a solution. This tendency to

capture water has been extensively documented in the literature by studies of the growth of salt containing aerosols as a function of the atmospheric relative humidity (Winkler, 1973, Ferron, 1977, Tang, 1976, Tang et al., 1977, Tang and Munkelwitz, 1977, Tang et al., 1978). A sharp increase in the diameter of the aerosol particle occurs when the relative humidity becomes greater than the water activity of the saturated solution of the salt.

From the data presented in Table 4-2, it is clear that the effectiveness of a salt is related to its deliquescent properties. A very deliquescent salt will be a good additive for  $\text{Ca(OH)}_2$ . Nevertheless, deliquescence alone can not explain the beneficial effect of some salts. For example KCl is the least deliquescent of all the salts tried but it is one of the most effective at 54% relative humidity.

For an additive to be effective it is necessary that the hydroxide of the cation to be very soluble, otherwise the cation will precipitate as the hydroxide and the anion will form the Ca salt. For example  $\text{Co(NO}_3)_2$  is a very deliquescent salt and the addition of  $\text{Co}^{+2}$  salts have been reported to increase dramatically the reactivity of limestone towards  $\text{SO}_2$  (Bjerle et al., 1983). However, when added to  $\text{Ca(OH)}_2$ , Co precipitates as the insoluble  $\text{Co(OH)}_2$ , and adding  $\text{Co(NO}_3)_2$  is equivalent to adding  $\text{Ca(NO}_3)_2$ , as can be seen from Table 4-2.

The effectiveness of a certain salt also depends on the relative humidity at which the experiment was performed. This could be expected because when the relative humidity of the gaseous phase is lower than the water activity in a saturated solution of the salt, the salt

should not absorb water and as a consequence should not be expected to increase  $\text{Ca}(\text{OH})_2$  reactivity in any appreciable degree. When examining the data in Table 4-2 it can be seen that the salts do not behave as could be expected from deliquescence considerations alone.  $\text{NaNO}_3$  and all the chlorides tried with the exception of  $\text{LiCl}$ , should not work at a relative humidity of 54%. Nevertheless,  $\text{Ca}(\text{OH})_2$  reactivity was improved by the presence of these salts at that relative humidity. A possible explanation for this phenomenon would be hysteresis, and this will be discussed in the next section.

#### 4.8.3 Effect of Prehumidification at 98% RH

As was mentioned in the Experimental Apparatus Section (Section 3.3), prior to each experimental run the fixed bed (consisting of  $\text{Ca}(\text{OH})_2$  dispersed in silica sand) was prehumidified by flushing with pure nitrogen at a relative humidity of about 98% for 10 minutes before flushing with nitrogen at the relative humidity at which the experiment was to be performed. This prehumidification was done to simulate the moisture conditions encountered in the bag filters during spray drying, where the solids are originally slurry droplets.

This prehumidification step could be the reason why some of the salts are still effective at a relative humidity lower than the one predicted from equilibrium considerations. Due to hysteresis it is possible that when the relative humidity was lowered to the experimental conditions after the prehumidification, some excess water remains in the solids. Strong hysteresis effects have been reported in  $\text{NaCl}$  aerosols (Tang and Munkelwitz, 1977).

To check if hysteresis was responsible for the beneficial effect of

some salts at low relative humidities, experimental runs were made omitting this step. Table 4-3 shows the results obtained at 54 and 17.4% relative humidity with and without prehumidification of the bed at 98% relative humidity. The additives used were NaCl, NaNO<sub>3</sub> and KCl.

**Table 4-3:** Effect of Prehumidification of the bed at 98% RH on Ca(OH)<sub>2</sub> Reactivity

500 ppm SO<sub>2</sub>, 1.0 g lime A, 4.6 l/min (0°C, 1 atm) N<sub>2</sub>

Additive (Mole%)	Average Ca(OH) <sub>2</sub> Conversion after 1 hour (%)			
	54% RH 66°C		17.4% RH 95°C	
	Prehumidified Yes	No	Prehumidified Yes	No
None	11.2	-	4.0	-
10% NaCl	27.0	23.2	9.7	4.0
10% NaNO <sub>3</sub>	27.2	23.7	11.9	-
10% KCl	37.3	19.3	3.4	-

At 54% relative humidity, though some decrease of the lime conversion was found without prehumidification, the results are still far superior to the pure lime case. Hysteresis then, cannot explain all of the improvement observed at 54% relative humidity. An alternate explanation would be that the chlorides and NaNO<sub>3</sub> modify the properties of the product CaSO<sub>3</sub>·1/2H<sub>2</sub>O layer that is formed as the reaction takes place thereby facilitating the access of the SO<sub>2</sub> to the unreacted Ca(OH)<sub>2</sub> which remains in the interior of the particle. NaCl

and  $\text{CaCl}_2$  have been reported to enhance the sulfur dioxide reactivity of limestones in fluidized bed combustion by affecting the pore structure of the lime during calcination, which then increases the extent of sulfation of the limestone (Chopra et al., 1980).

At 17.4% relative humidity all the beneficial effect in the case of the NaCl appears to be due to the prehumidification of the bed, i.e. due to a hysteresis phenomena.

#### 4.8.4 Effect of Nitrogen Purity

When experiments using NaCl as an additive were performed it was found that the lime conversion given by chemical analysis of the reacted solids was consistently lower than the lime conversion calculated by integration of  $\text{SO}_2$  removal over time. The disappearance of sulfite could be explained by: 1) a disproportionation reaction of sulfite to produce thiosulfate and sulfate or 2) the oxidation of the sulfite product by oxygen present as impurity in the nitrogen. The first explanation was discarded after chemical analysis showed no traces of thiosulfate in the reacted solids. The more likely explanation is then partial oxidation of the sulfite produced in the reaction by the oxygen present as an impurity in the nitrogen. To test this possibility some experiments were run using oxygen-free nitrogen (purity of 99.998%) instead of the nitrogen previously used that has a purity of 99.5%. Table 4-4 shows the comparison of two experiments run at the same experimental conditions but using the two different types of nitrogen. A much better agreement was found between the lime conversion obtained by chemical analysis and the one obtained by integrating  $\text{SO}_2$  removal when oxygen-free nitrogen was used.

**Table 4-4: Effect of Nitrogen Purity on Lime Reactivity**

500 ppm SO<sub>2</sub>, 54% RH, 10 mole% NaCl, 1.0 g lime A, 4.6 l/min N<sub>2</sub>

Type of Nitrogen	Average Ca(OH) <sub>2</sub> Conversion after 1 hour (%)	
	By Integrating SO <sub>2</sub> Curves	By Chemical Analysis
Common(99.5% purity)	27.0	19.7
O <sub>2</sub> Free (99.998% purity)	27.0	25.1

The lime conversion estimated by integration of SO<sub>2</sub> removal was the same in both experiments, indicating that the rate of SO<sub>2</sub> removal is not affected by the nitrogen purity even when some oxidation of the sulfite appears to be taking place when the less pure nitrogen was used. Differential Scanning Calorimetry (DSC) and X-ray powder diffraction results indicate that any sulfate produced in the reactor will be present in solid solution with CaSO<sub>3</sub>·1/2H<sub>2</sub>O and not as a separate gypsum or CaSO<sub>4</sub>·1/2H<sub>2</sub>O phase. Details of the DSC and X-rays work are given in Appendix A, Sections A.5 and A.6.

## 4.9 Other Experimental Runs

### 4.9.1 Effect of Relative Humidity

Several experiments were run keeping the absolute humidity of the gases constant but modifying the relative humidity by increasing the reactor temperature. The experiments were run using Ca(OH)<sub>2</sub> with NaCl or NaNO<sub>3</sub> as additives. Figure 4-2 shows the results of

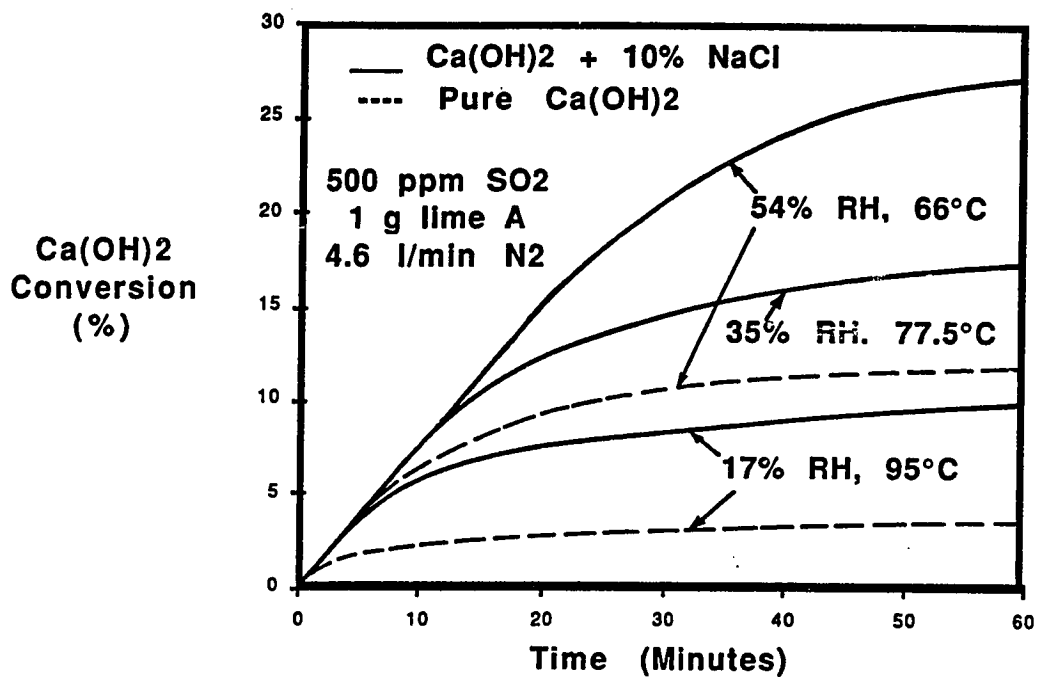


Figure 4-2: Decreasing Relative humidity by Increasing Temperature, 10 mole% NaCl

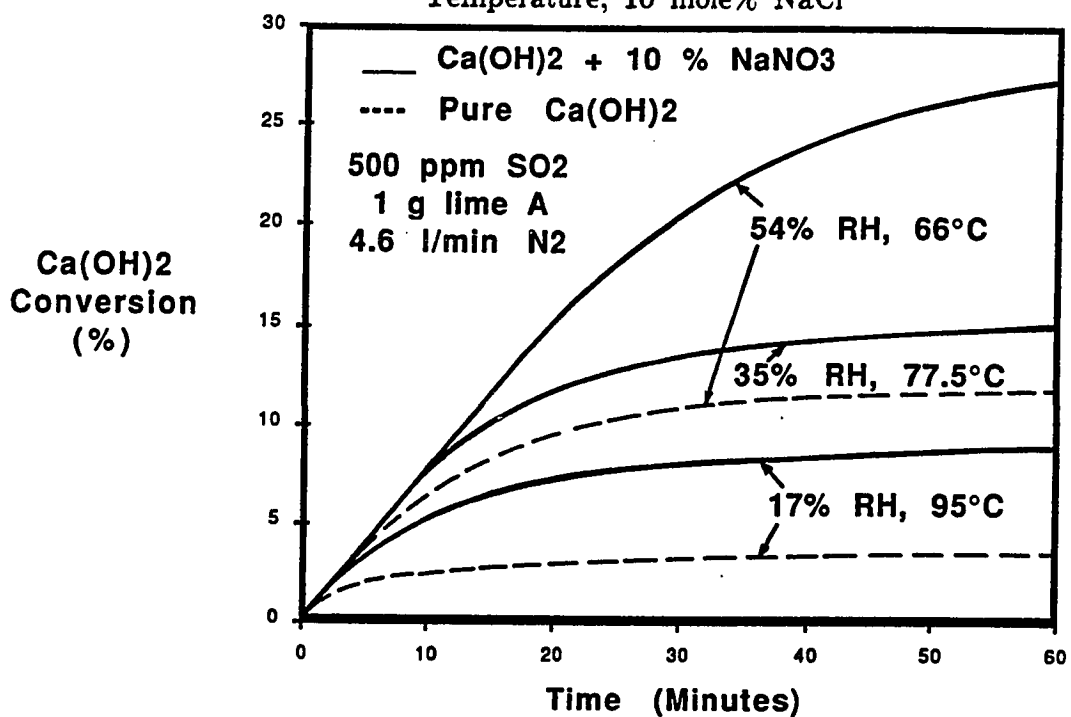


Figure 4-3: Decreasing Relative Humidity by Increasing Temperature, 10 mole% NaNO<sub>3</sub>

experimental runs made at 66, 77.5 and 95°C, which correspond to relative humidities of 54, 35 and 17%, using 10 mole% NaCl as additive.  $\text{Ca}(\text{OH})_2$  conversion decreases dramatically when the relative humidity decreases even when the reactor temperature is higher. Figure 4-3 shows the same results with 10 mole%  $\text{NaNO}_3$ . Both additives behaved in an almost identical way.

#### 4.9.2 $\text{CaCl}_2$ and Adipic Acid as Additives

As has been discussed, the addition of an organic acid like adipic acid proved to be detrimental to the reaction of  $\text{Ca}(\text{OH})_2$  with  $\text{SO}_2$ , while  $\text{CaCl}_2$  increased the reactivity of the  $\text{Ca}(\text{OH})_2$ . When adipic acid and  $\text{CaCl}_2$  were simultaneously added to the  $\text{Ca}(\text{OH})_2$ , the adipic acid detrimental effect nullified the beneficial effect of the salt and the combined result was a conversion that was very close to the  $\text{Ca}(\text{OH})_2$  with no additives. This is illustrated by Table 4-5 which shows the average  $\text{Ca}(\text{OH})_2$  conversion after a hour of reaction for  $\text{Ca}(\text{OH})_2$  with no additives, using adipic acid and  $\text{CaCl}_2$  alone and together.

#### 4.9.3 Differential Experiments

Differential experiments were also performed using pure  $\text{Ca}(\text{OH})_2$  and  $\text{Ca}(\text{OH})_2$  with NaCl. Differential experiments were run with a very small amount of lime in the reactor (0.125 g), so that the  $\text{SO}_2$  concentration across the reactor did not change significantly. In these experiments, the integration of  $\text{SO}_2$  removal was not accurate enough to determine the  $\text{Ca}(\text{OH})_2$  conversion, so the conversion was determined by chemical analysis of the reacted solids at different reaction times. All of the differential experiments were run using oxygen-free nitrogen to prevent oxidation of the sulfite in the reactor. Figures

**Table 4-5:** Effect of Adipic acid and  $\text{CaCl}_2$  as additives for  $\text{Ca}(\text{OH})_2$   
500 ppm  $\text{SO}_2$ ,  $64.4^\circ\text{C}$ , 74% RH, 1.0 g lime A, 4.6 l/min  $\text{N}_2$

Additives	Average Conversion after 1 hr (%)
None	22.4
5 mole% $\text{CaCl}_2$	34.6
1 wt% Adipic Acid	20.3
1 wt% Adipic Acid + 5 mole% $\text{CaCl}_2$	23.5

4-4 and 4-5 show the results of these differential experiments for pure  $\text{Ca}(\text{OH})_2$  and  $\text{Ca}(\text{OH})_2$  with 10 mole%  $\text{NaCl}$  and 5 mole%  $\text{CaCl}_2$ . The rate of reaction decreased much more slowly during the first minutes of reaction when  $\text{NaCl}$  is present.

#### 4.9.4 Effect of $\text{NaCl}$ in the Reactivity of Dolomitic Lime

An experimental run was also made to see how the addition of  $\text{NaCl}$  affected the reactivity of pressure hydrated dolomitic lime towards  $\text{SO}_2$ . The sample of dolomitic lime used was provided by Dr. John Chang (Acurex), and corresponds to dolomitic lime collected after the ball mill. The lime sample was dry sieved through a  $125\ \mu\text{m}$  sieve to eliminate the bigger particles. Table 4-6 shows the average lime conversion after 1 hour of reaction for dolomitic lime without additive and with 10 mole%  $\text{NaCl}$ . To calculate the conversion the composition of the dolomitic lime was assumed to be 40 mole%  $\text{Mg}(\text{OH})_2$  and 60 mole%  $\text{Ca}(\text{OH})_2$ . The average conversion at 74% relative humidity and  $64.4\ ^\circ\text{C}$  increased from 31.2 to 39.3% with the addition of the  $\text{NaCl}$ .

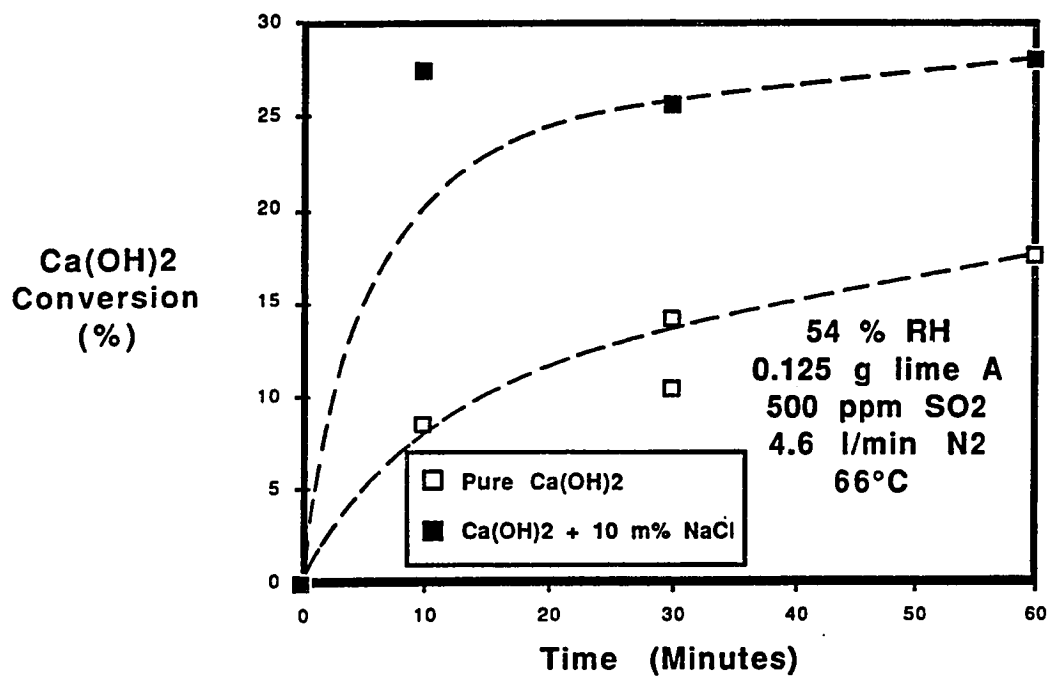


Figure 4-4: Differential Experiments, Effect of NaCl

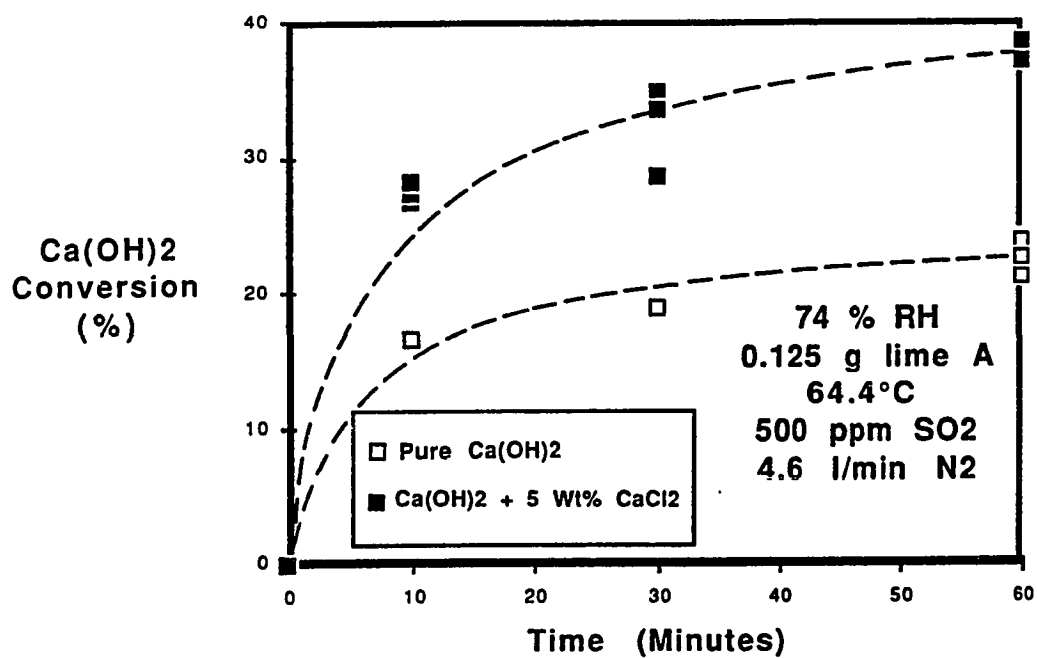


Figure 4-5: Differential Experiments, Effect of CaCl<sub>2</sub>

**Table 4-6: Effect of NaCl on the Reactivity of Pressure Hydrated Dolomitic Lime**

500 ppm SO<sub>2</sub>    74% RH    64.4°C    1.0 g lime A    4.6 l/min N<sub>2</sub>

Type of Sample	Average Lime Conversion after 1 hr (%)
Sieved Ball Mill Lime (< 125 μm)	31.2
Sieved Ball Mill Lime + 10 Mole% NaCl	39.3

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## Chapter 5

### Modelling of the Reaction of SO<sub>2</sub> with Ca(OH)<sub>2</sub>

#### 5.1 Summary

A shrinking core model with zero order kinetics in SO<sub>2</sub> was used to model experimental data on the reaction of SO<sub>2</sub> with Ca(OH)<sub>2</sub> solids in a fixed bed reactor at 30.4 to 66°C and 19 to 74% relative humidity. An empirical correlation was included in the model to account for shape and surface roughness of the Ca(OH)<sub>2</sub> particles. The diffusion coefficient of the SO<sub>2</sub> through the product layer increases linearly with relative humidity, and the kinetic rate constant increases exponentially with relative humidity. With a few exceptions the model was able to predict the experimental data within the margin of experimental error ( $\pm 10\%$ ). At high relative humidity and/or high SO<sub>2</sub> concentration, reaction kinetics control the rate, while at low relative humidity and/or low SO<sub>2</sub> concentration, SO<sub>2</sub> diffusion through the CaSO<sub>3</sub>·1/2H<sub>2</sub>O product layer controls the rate. Diffusion coefficient values ranging from 0.75E-9 to 1.20E-6 (cm<sup>2</sup>/s) and kinetic constant values ranging from 1.0E-9 to 8.23E-9 (cm<sup>4</sup>/gmol s) simulated the experimental results. An activation energy of 2.9 kcal/gmol was estimated for the reaction. Deliquescent salt additives increase the SO<sub>2</sub> diffusion coefficient and the kinetic rate constant in the same manner as relative humidity. Depending on the amount or type of deliquescent salt the rate can be kinetically or diffusion controlled.

## 5.2 Introduction

A bench scale study of the reaction of  $\text{SO}_2$  with  $\text{Ca}(\text{OH})_2$  with and without deliquescent salt additives was reported in chapters 3 and 4. The study was done at experimental conditions similar to the ones found in the bag filters following the spray dryer during flue gas desulfurization. This chapter presents the modelling of those experimental results using a modified shrinking core model with kinetics of zero order in  $\text{SO}_2$ .

The shrinking core model originally developed by Yagi and Kunii (1961) for the isothermal reaction of spherical solid particles assumes that the solid reactant has a low porosity and is practically impervious to the gaseous reactant. Under these conditions the reaction is narrowly confined to the surface of the solid particle, or to the interface between unreacted solid and the porous product layer. After the reaction has progressed, the solid will consist of an unreacted core surrounded by an envelope of reacted material. The reactant fluid must then diffuse through the reacted solid region to reach the inner-core and react. The original shrinking core model of Yagi and Kunii was extended to nonisothermal cases by several researchers (Hills, 1968, Shen and Smith, 1965, Wen and Wei, 1971). The shrinking core model has been extensively used to interpret experimental results of a number of gas-solid reactions (McKewan, 1962, St. Clair, 1966, Lu and Bistsianes, 1966, Spitzer et al., 1966, Yagi and Kunii, 1961, Hellinckx, 1954, Narsimhan, 1961, Samuel and Lapp, 1980, Samuel et al., 1984).

Klingspor et al. (1983, 1984) used an integral shrinking core model with kinetics as the controlling step to explain the dependence of reaction rate on lime conversion for the reaction of  $\text{SO}_2$  with different

types of slaked limes in a fixed bed reactor. They found the model did not fit their experimental data at the beginning of the reaction and it only applied after a certain lime conversion had been reached. They attributed the sharp decrease in reaction rate to a decrease in surface roughness of the solid particles.

In the present work, the reaction of  $\text{SO}_2$  with  $\text{Ca(OH)}_2$  was modelled by a differential shrinking core model with zero order kinetics in  $\text{SO}_2$ . The model includes  $\text{SO}_2$  diffusion through the gas film surrounding the solid particle, diffusion of  $\text{SO}_2$  through the product layer, and chemical reaction. An empirical correlation to account for the non-sphericity and surface roughness of the  $\text{Ca(OH)}_2$  particles was also included in the model.

### 5.3 Experimental

The experimental data being modelled was obtained in a bench scale fixed bed reactor, the bed consisting of a mixture of silica sand and reagent grade  $\text{Ca(OH)}_2$ . The gaseous phase consisted of a mixture of  $\text{N}_2$ ,  $\text{SO}_2$  and water vapor. Details of the experimental apparatus and procedure have been given in section 3.3, Chapter 3. Two batches of reagent grade  $\text{Ca(OH)}_2$  differing slightly in particle size distribution and BET surface area (namely lime 0 and lime A) were used in the experiments. The particle size distribution of these two batches of  $\text{Ca(OH)}_2$  was measured by a Coulter Counter IIA (See Section A-1 of Appendix A). The BET surface area measured by nitrogen adsorption isotherms was  $8.2 \text{ m}^2/\text{g}$  for lime 0 and  $9.4 \text{ m}^2/\text{g}$  for lime A. Direct observation of the  $\text{Ca(OH)}_2$  particles using the Scanning Electron Microscope showed them to be of irregular shape and considerable surface roughness. No pores were visible under the microscope. Scanning

electron microscope pictures of reacted and unreacted samples of limes 0 and A are shown in Appendix A, section A-2.

The deliquescent salts tested as additives were added to the  $\text{Ca}(\text{OH})_2$  by a slurring and drying procedure.

#### 5.4 Model

The equations that describe the absorption of a component from a moving gas stream by a fixed solid in a packed bed consist of two partial differential equations obtained from material balances in the gaseous and solid phases.

$$\frac{\partial C_{\text{SO}_2}}{\partial t} + \frac{v_m \partial C_{\text{SO}_2}}{A \partial z} = r_{\text{SO}_2} \quad (5.1)$$

$$\frac{dC_{\text{lime}}}{dt} = r_{\text{SO}_2} \quad (5.2)$$

Where:

$C_{\text{SO}_2}$  = concentration of  $\text{SO}_2$  in the gas phase ( $\text{gmol}/\text{cm}^3$ )

$v_m$  = volumetric flow rate of gas ( $\text{cm}^3/\text{sec}$ )

$A$  = cross sectional area of the reactor ( $\text{cm}^2$ )

$z$  = length of the reactor (cm)

$C_{\text{lime}}$  =  $\text{Ca}(\text{OH})_2$  concentration ( $\text{gmol}/\text{cm}^3$ )

$t$  = time (sec)

$r_{\text{SO}_2}$  = rate of disappearance of  $\text{SO}_2$  ( $\text{gmol}/\text{cm}^3 \text{ sec}$ )

For most cases the concentration of  $\text{SO}_2$  in the gas phase does not change rapidly with time at a given point (von Rosenberg et al., 1977), thus the time derivative of the  $\text{SO}_2$  concentration in equation (5.1) is much smaller than the spatial derivative. The time derivative can then be dropped from equation (5.1) and the set of differential equations reduces to:

$$\frac{v_m dC_{\text{SO}_2}}{A dz} = r_{\text{SO}_2} \quad (5.3)$$

$$\frac{dC_{\text{lime}}}{dt} = r_{\text{SO}_2}$$

with boundary and initial conditions:

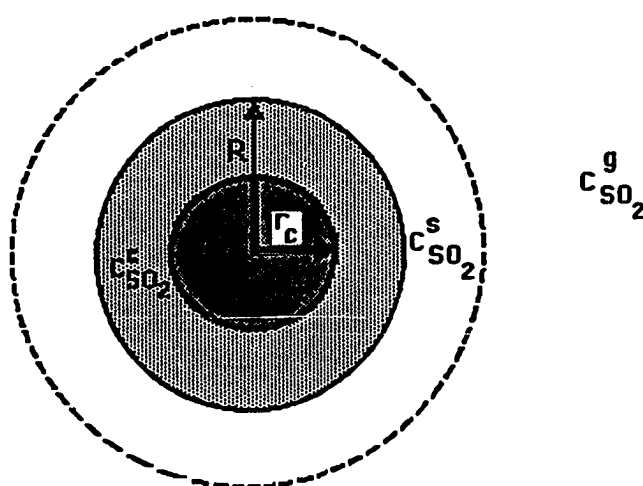
$$\text{At } z = 0 \quad C_{\text{SO}_2} = C_{\text{SO}_2}^{\circ} \quad (5.4)$$

$$\text{At } t = 0 \quad C_{\text{lime}} = C_{\text{lime}}^{\circ}$$

the rate expression  $r_{\text{SO}_2}$  will depend on the model selected to represent the kinetics of the reaction.

The shrinking core model for spherical particles of constant radius with kinetics of zero order in  $\text{SO}_2$  was chosen to fit the experimental data. Because the  $\text{Ca}(\text{OH})_2$  particles are non-spherical and have a rough surface, their surface area is much higher than that of spherical particles of the same volume. An empirical expression was introduced to account for the decrease in roughness as the reaction progress.

The shrinking core model or unreacted core model assumes that the reaction takes place at the exterior surface of the particle. As the reaction proceeds the surface of reaction will move into the interior of the solid leaving behind a layer of inert product. The external radius of the particle remains the same, this assumes no shrinkage or swelling of the product layer. Schematically at any given time  $t$  we have:



Shrinking Core Model

Where:

$R$  = Radius of the particle (cm)

$r_c$  = Radius of the unreacted core (cm)

$C_{SO_2}^g$  =  $SO_2$  concentration at the gas bulk ( $gmol/cm^3$ )

$C_{SO_2}^s$  =  $SO_2$  concentration at the surface of the particle ( $gmol/cm^3$ )

$C_{SO_2}^c$  =  $SO_2$  concentration at the surface of the core ( $gmol/cm^3$ )

In order for the gaseous reactant to reach the surface of the

unreacted core it must diffuse through the gas film surrounding the particle and through the inert product layer. Once the reactant reaches the surface of the core, the chemical reaction takes place.

Assuming that the chemical reaction at the surface of the core is zero order in  $\text{SO}_2$  and irreversible, the rate of disappearance of  $\text{SO}_2$  with time is given by:

$$r_{\text{SO}_2} = \frac{1}{V} 4\pi R^2 k_g N (C_{\text{SO}_2}^g - C_{\text{SO}_2}^s) \quad \text{Gas film diffusion} \quad (5.5)$$

$$r_{\text{SO}_2} = \frac{1}{V} \frac{4\pi R r_c D_e N (C_{\text{SO}_2}^s - C_{\text{SO}_2}^c)}{R - r_c} \quad \text{Product diffusion} \quad (5.6)$$

$$r_{\text{SO}_2} = \frac{1}{V} 4\pi r_c^2 N k_s \rho_{\text{lime}} \quad \text{Chemical reaction} \quad (5.7)$$

where:

$k_g$  = mass transfer coefficient (cm/sec)

$D_e$  = diffusivity of  $\text{SO}_2$  through product ( $\text{cm}^2/\text{sec}$ )

$k_s$  = kinetic rate constant ( $\text{cm}^4/\text{gmol sec}$ )

$\rho_{\text{lime}}$  =  $\text{Ca}(\text{OH})_2$  molar density ( $\text{gmol}/\text{cm}^3$ )

$N$  = number of  $\text{Ca}(\text{OH})_2$  particles

$V$  = volume of reactor ( $\text{cm}^3$ )

If the chemical reaction is slow, the rate of disappearance of  $\text{SO}_2$  will be given by equation (5.7). If the chemical reaction is fast, all of the  $\text{SO}_2$  that reaches the surface of the core will be immediately consumed and the concentration of the  $\text{SO}_2$  at the surface of the unreacted core will become zero. At these conditions the rate of diffusion of the  $\text{SO}_2$  through the gas film and product layer will become the limiting steps. In this case equations (5.5) and (5.6) can be combined to give:

$$r_{\text{SO}_2} = \frac{1}{V} \frac{C_{\text{SO}_2}^g}{\frac{R - r_c}{4\pi D_e N R r_c} + \frac{1}{4\pi R^2 N k_g}} \quad (5.8)$$

Using the relationship:

$$r_c = X_{\text{lime}}^{1/3} R \quad (5.9)$$

Where  $X_{\text{lime}}$  is the fraction of lime unreacted, equations (5.7) and (5.8) become :

$$r_{\text{SO}_2} = \frac{1}{V} 4\pi R^2 N \rho_{\text{lime}} k_s X_{\text{lime}}^{2/3} \quad (5.10)$$

$$r_{\text{SO}_2} = \frac{1}{V} \frac{C_{\text{SO}_2}^g}{\frac{X_{\text{lime}}^{-1/3} - 1}{4\pi D_e N R} + \frac{1}{4\pi R^2 k_g N}} \quad (5.11)$$

Of equations (5.10) and (5.11), the one that gives the smallest rate of disappearance of  $\text{SO}_2$  will determine the overall reaction rate.

The model developed so far is for spherical particles. To account for the nonsphericity of the lime particles and their surface roughness, a roughness parameter was defined as:

$$\sigma = \frac{A}{A_{\phi}} \quad (5.12)$$

Where:

$A$  = actual surface area of the lime

$A_{\phi}$  = surface area of spherical particles of equal volume

When the lime is unreacted,  $\sigma$  can be estimated as the ratio of the BET surface area of the lime and the surface area calculated from the Coulter Counter particle size distribution assuming spherical particles. As the reaction progresses  $\sigma$  should decrease and approach the limit  $\sigma = 1.0$  when all the lime has reacted. This roughness parameter should decrease very rapidly at the beginning of the reaction and more slowly as the particles approach spherical shape.

An empirical expression of the form:

$$\sigma = 1.0 + \exp(aX_{\text{lime}} + b) \quad (5.13)$$

was used to describe the change of roughness with the fraction of  $\text{Ca}(\text{OH})_2$  unreacted. Equation (5.13) must satisfy the condition:

$$\text{at } X_{\text{lime}} = 1.0 \quad \sigma = \sigma_o = \text{BET area}/A_{\phi} \quad (5.14)$$

To force  $\sigma$  to decrease more rapidly at high values of  $X_{\text{lime}}$  and to simulate the experimental results, an additional condition was incorporated:

$$\text{at } X_{\text{lime}} = 0.8 \quad \sigma = 2.0 \quad (5.15)$$

For the two batches of  $\text{Ca}(\text{OH})_2$  used in the experiments, namely lime 0 and lime A which differ slightly in surface area and particle size, the constants a and b in equation (5.13) took slightly different values.

For lime 0:

$$\sigma = 1 + \exp(12.8775 X_{\text{lime}} - 10.3020) \quad (5.16)$$

For lime A:

$$\sigma = 1 + \exp(13.428 X_{\text{lime}} - 10.7424) \quad (5.17)$$

After introducing the roughness parameter  $\sigma$ , equations (5.10) and (5.11) become:

$$r_{\text{SO}_2} = \frac{1}{V} 4\pi R^2 N \sigma \rho_{\text{lime}} k_s X_{\text{lime}}^{2/3} \quad (5.18)$$

$$r_{\text{SO}_2} = \frac{1}{V} \frac{C_{\text{SO}_2}^g}{\frac{X_{\text{lime}}^{-1/3} - 1}{4\pi D_e N R (\sigma \sigma_o)^{1/2}} + \frac{1}{4\pi R^2 k_s N \sigma_o}} \quad (5.19)$$

Of equations (5.18) and (5.19), the one that gives the lowest rate of  $\text{SO}_2$  disappearance will determine the overall kinetic rate. The

parameters of the model are  $k_g$ ,  $D_e$ , and  $k_s$ . The integration assumed an average particle size which gave the same surface area as the measured particle size distribution assuming spherical particles. The mass transfer coefficient,  $k_g$  was not used as an adjustable parameter because at the conditions at which the experiments were performed, gas film diffusion is not likely to be important. The only effect of gas film diffusion is that it provides a limit to the rate expression (5.19) at the beginning of the reaction where product layer resistance is zero as there is no product formed. The value of  $k_g$  was estimated using a Sherwood number of 2 (Sherwood et al., 1975):

$$\frac{k_g d_p}{D_e} = 2.0 \quad (5.20)$$

corresponding to mass transfer from spherical particles in an stagnant fluid. In fact, mass transfer coefficients several orders of magnitude smaller than the value given by this correlation ( $k_g = 544$  cm/sec) can be used in the model without affecting the results, which confirms the fact that gas phase diffusion is not likely to become a limiting factor during the reaction of  $\text{Ca(OH)}_2$  with  $\text{SO}_2$ .

Thus  $D_e$  and  $k_s$  were the only parameters used to fit the experimental data. As will be discussed in the next section, which presents the results of fitting the experimental data, depending on whether mass transfer or chemical reaction is the controlling step, only one of these parameters may be important.

A computer program with variable step size in time and in distance along the reactor was written to model the reaction. This computer program uses the IMSL integration routine DGEAR to carry

out the integration, and the IMSL interpolation routine ICSCCU to provide interpolated values of lime conversion needed for each time integration step. A listing of the computer program is given in Appendix C.

### 5.5 Modelling Results

Figures 5-1 to 5-7 show the results of correlating with the model the experimental data obtained by reacting pure  $\text{Ca}(\text{OH})_2$  with  $\text{SO}_2$ . The adjustable parameters of the model are the diffusion coefficient of  $\text{SO}_2$  through the product layer ( $D_e$  in  $\text{cm}^2/\text{sec}$ ), and the kinetic constant ( $k_s$  in  $\text{cm}^4/\text{gmol sec}$ ).

Figure 5-1 shows several sets of experiments performed using 4 g of  $\text{Ca}(\text{OH})_2$  at 66°C, and 2000 ppm  $\text{SO}_2$  at different relative humidities. At high relative humidity the chemical reaction is the controlling step and  $k_s$  is the parameter that determines the rate of reaction. Any value of  $D_e$  greater than  $8.0\text{E-}8$   $\text{cm}^2/\text{sec}$  will give essentially the same result.  $\text{SO}_2$  diffusion through the product layer becomes more important as the relative humidity decreases. At 19% relative humidity  $D_e$  is the parameter that determines the rate of adsorption of  $\text{SO}_2$ . At 19% relative humidity any value of  $k_s$  greater than  $1.0\text{E-}9$   $\text{cm}^4/(\text{gmol sec})$  will give essentially the same results. Both  $D_e$  and  $k_s$  are affected by the relative humidity, but in the range of relative humidities studied  $k_s$  increases approximately linearly while  $D_e$  increases exponentially (see Figure 5-2). Because the  $\text{SO}_2$  diffusion coefficient changes more rapidly than the kinetic constant, a change in the controlling mechanism occurs when the relative humidity is increased.

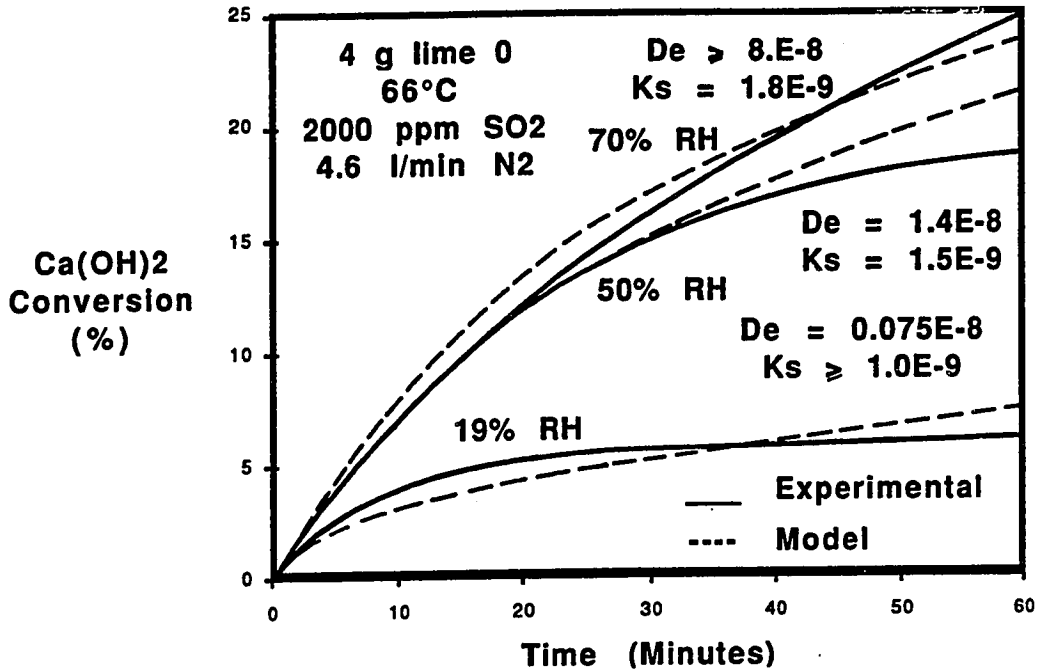


Figure 5-1: Effect of Relative Humidity on Reaction Rate, Lime 0

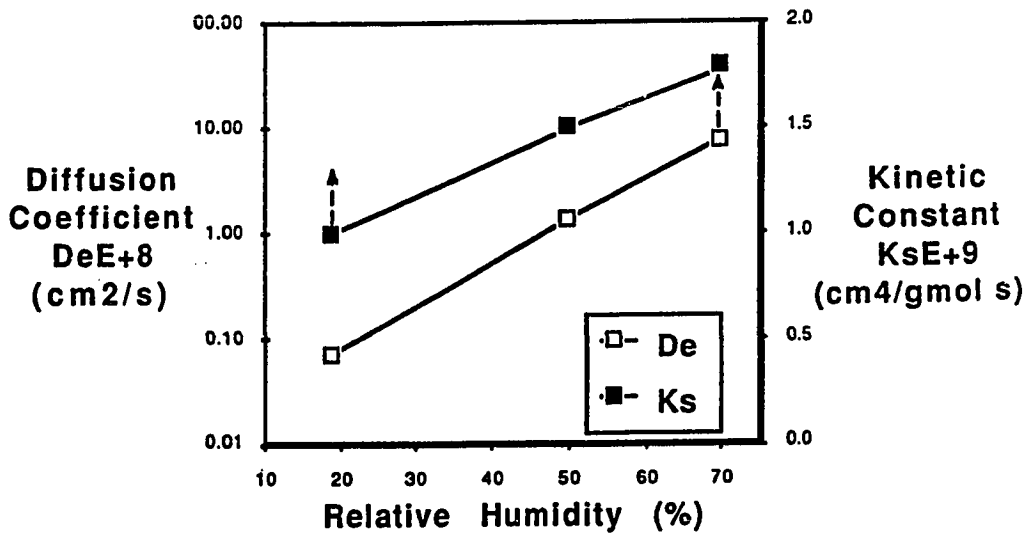


Figure 5-2: Effect of Relative Humidity on Model Parameters

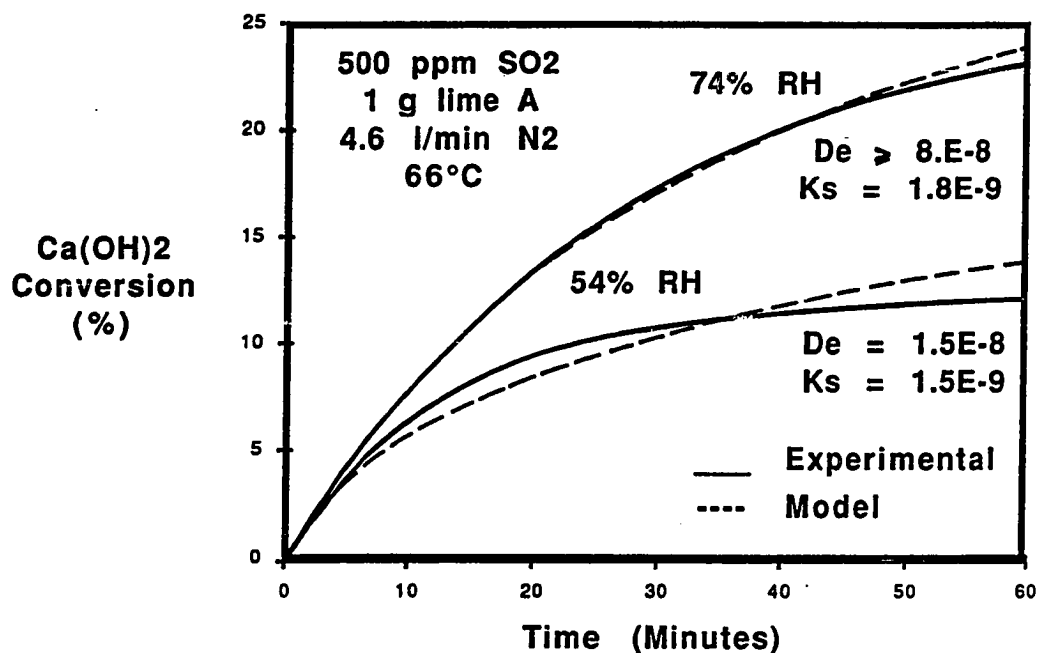


Figure 5-3: Effect of Relative Humidity on Reaction Rate, Lime A

The same values of  $D_e$  and  $k_s$  were used to model the results obtained using a 1 g of lime A and 500 ppm SO<sub>2</sub>, as illustrated by Figure 5-3. Because the SO<sub>2</sub> concentration in these experiments is much lower than in the experiments presented in Figure 5-1, SO<sub>2</sub> diffusion through the product layer becomes the controlling step at a much higher relative humidity (54%).

The effect of SO<sub>2</sub> concentration on lime conversion at high relative humidity is illustrated in Figure 5-4. These experiments were run at 70% relative humidity, and 4 g lime 0 loaded in the reactor. At high relative humidity and high SO<sub>2</sub> levels the reaction rate is kinetically controlled, so changing the SO<sub>2</sub> concentration from 1060 to

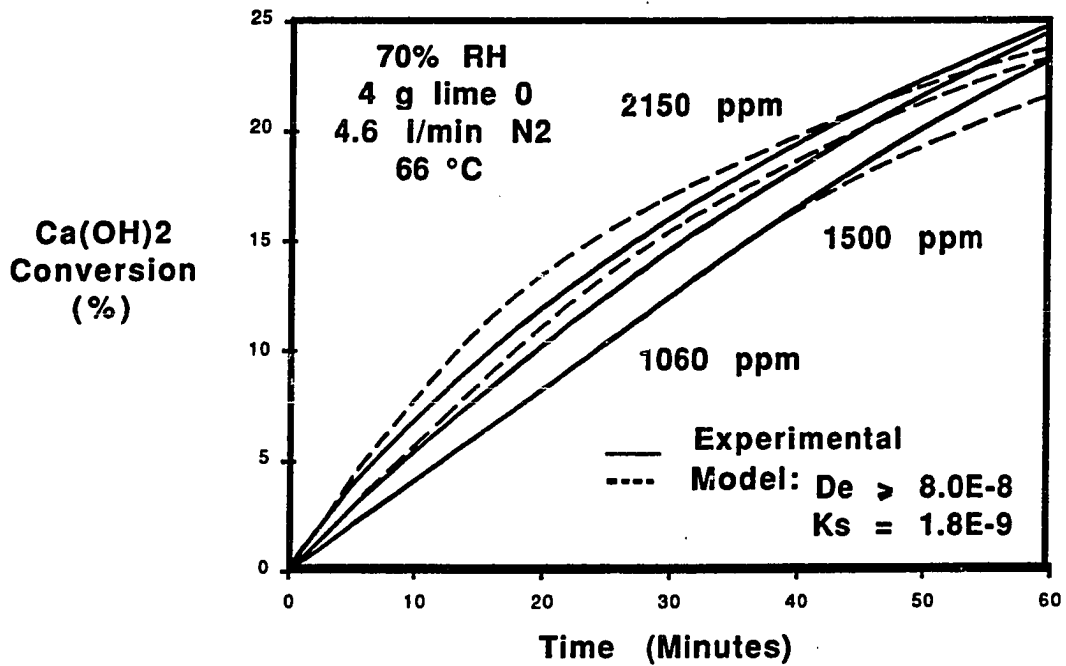


Figure 5-4: Effect of SO<sub>2</sub> Concentration, 70% Relative Humidity

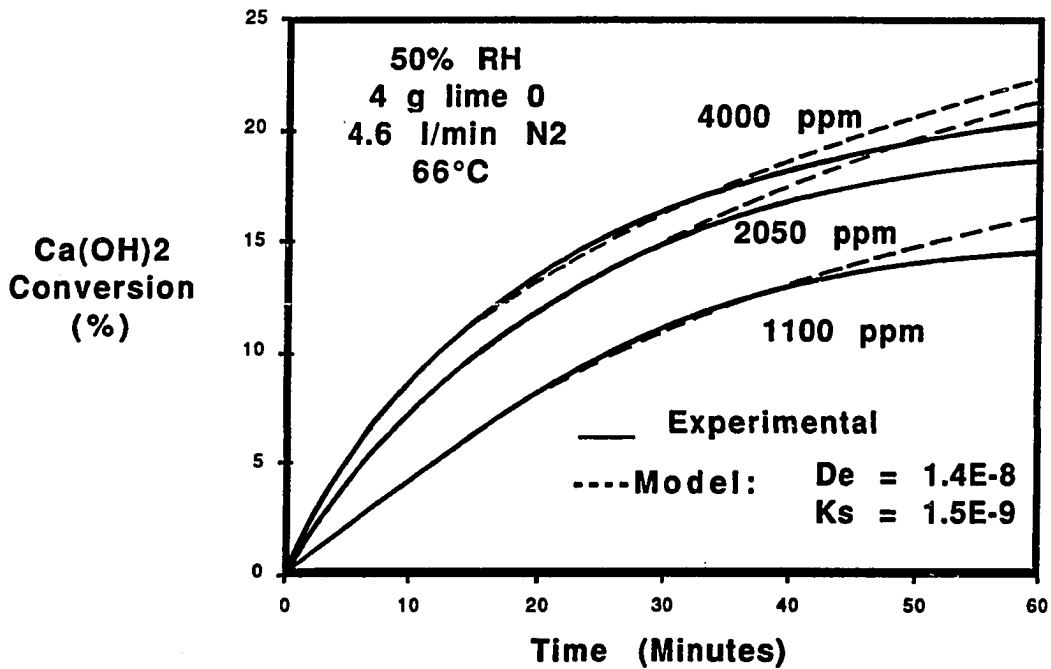


Figure 5-5: Effect of SO<sub>2</sub> Concentration, 50% Relative Humidity

2150 ppm has little effect on the reaction rate. At lower relative humidity (50%) and high  $\text{SO}_2$  concentrations reaction kinetics are still controlling, so the reaction rate is practically independent of  $\text{SO}_2$  concentration as illustrated by Figure 5-5. When the  $\text{SO}_2$  concentration is reduced to 1000 ppm, mass transfer of the  $\text{SO}_2$  through the product layer becomes important, and the reaction rate is dependent on the  $\text{SO}_2$  level. As can be seen from Figures 5-4 and 5-5, the model is able to predict the  $\text{SO}_2$  effect with reasonable accuracy.

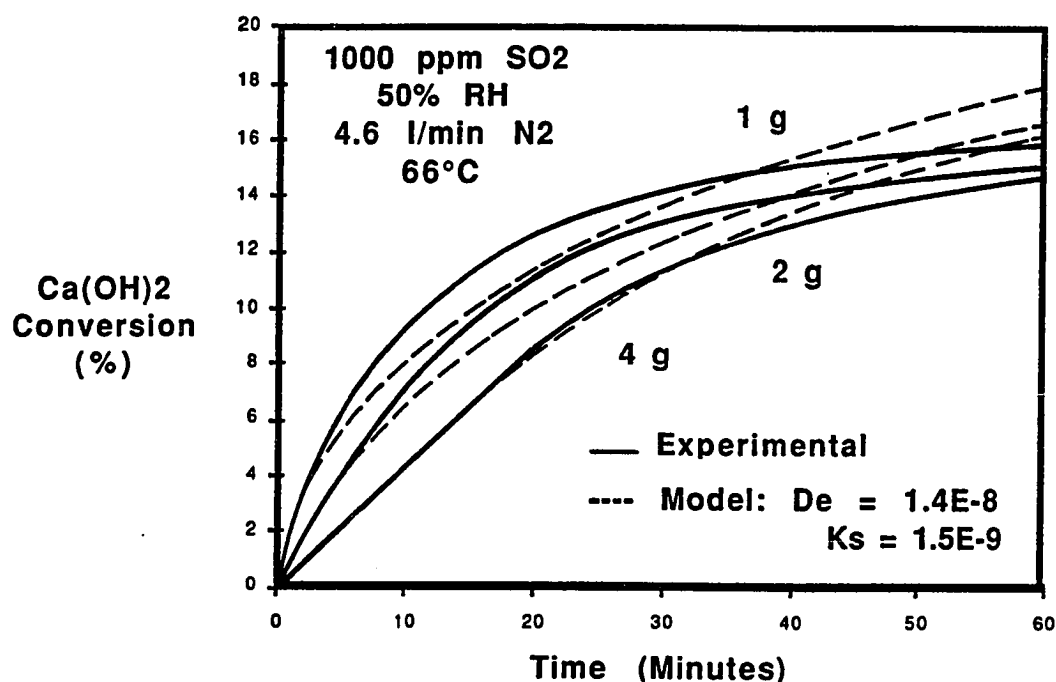


Figure 5-6: Effect of  $\text{Ca(OH)}_2$  Load on Reaction Rate

The ability of the model to predict the effect of changing the lime 0 load in the reactor is illustrated by Figure 5-6 for experiments run at 50% relative humidity and 1000 ppm  $\text{SO}_2$ . During the first 20 or 30 minutes of reaction, the  $\text{SO}_2$  removal in the reactor is high and

the amount of lime present in the reactor affects the reaction rate because the lime at the end of the reactor "sees" different levels of  $\text{SO}_2$ . At later times, when the  $\text{SO}_2$  removal is lower, the  $\text{SO}_2$  level inside the reactor is practically the same regardless of how much lime is present, and the reaction rates are essentially the same in all three cases.

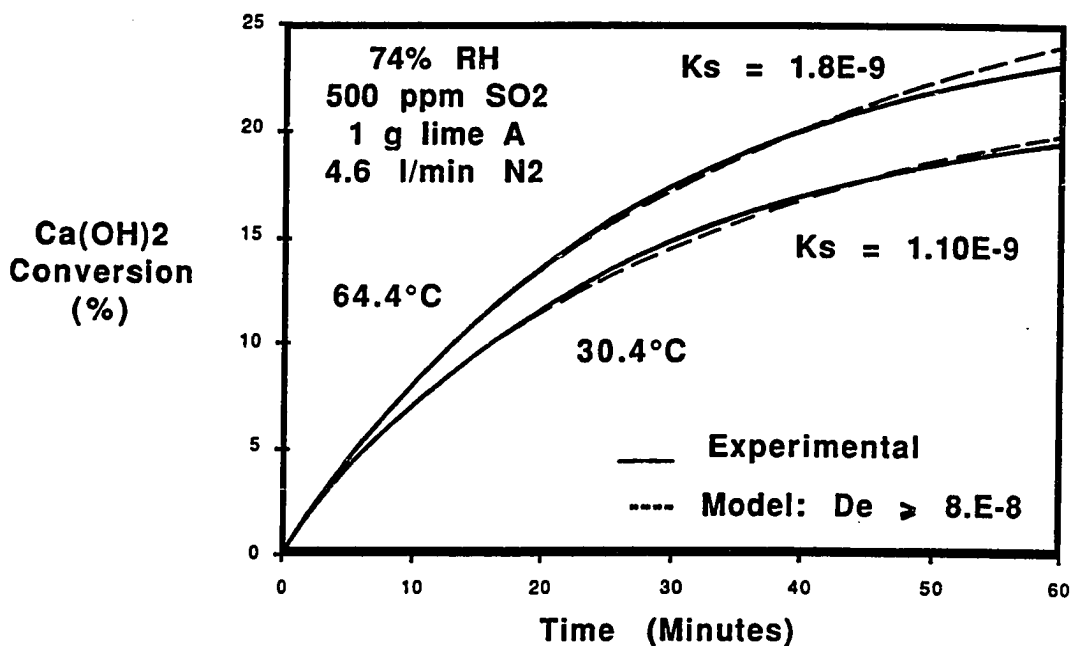


Figure 5-7: Effect of Temperature on Reaction Rate

Figure 5-7 shows the effect of temperature on the kinetic constant  $k_s$ . At the conditions at which the experiments were performed the reaction rate is kinetically controlled, so  $k_s$  is the only important adjustable parameter in the model. By using the values of  $k_s$  given by the model an apparent activation energy of 2.9 kcal/gmol can be estimated for  $\text{Ca(OH)}_2$ . This value of activation energy is somewhat lower than the value of 6 kcal/gmol reported by other sources for this reaction (Acurex, 1985).

**Table 5-1: Modelling Experiments with Salt Additives**74% RH, 64.4 °C, 1 g lime A, 4.6 l/min N<sub>2</sub>, 500 ppm SO<sub>2</sub>

Exp #	Additive (Mole%)	Conversion at 60 min (%)	Model Constants D <sub>e</sub> E+8 (cm <sup>2</sup> /s)	Constants k <sub>s</sub> E+9 (cm <sup>4</sup> /mol s)	St. Dev. (*)	Max. Error (%)
77	None	23	≥ 8.0	1.8	0.39	3.8
127	10% NaOH	39	≥ 90.0	6.2	0.42	2.6
128	5% Na <sub>2</sub> SO <sub>3</sub>	30	≥ 17.0	2.6	1.17	7.7
129	5% Na <sub>2</sub> SO <sub>4</sub>	28	≥ 18.0	2.7	0.43	3.1
130	10% NaCl	39	≥ 85.0	6.1	0.37	3.0
131	10% NaNO <sub>3</sub>	42	≥ 95.0	7.6	0.49	2.9
132	10% NaNO <sub>2</sub>	40	≥ 80.0	7.0	1.23	7.5
133	5% Ca(NO <sub>3</sub> ) <sub>2</sub>	39	≥ 85.0	7.0	0.40	2.7
98	5% CaCl <sub>2</sub>	37	≥ 73.0	5.4	0.29	2.6

\* The standard deviation was calculated using the experimental and predicted values of % lime converted every 5 minutes of reaction time.

**Table 5-2: Modelling Experiments with Salt Additives RH**54% RH, 66°C, 1 g lime A, 4.6 l/min N<sub>2</sub>, 500 ppm SO<sub>2</sub>

Exp #	Additive (Mole%)	Conversion at 60 min (%)	Model Constants D <sub>e</sub> E+8 (cm <sup>2</sup> /s)	k <sub>s</sub> E+9 (cm <sup>4</sup> /mol s)	St. Dev.	Max. Error (%)
136	None	12	1.5	≥ 1.50	1.08	14.9
140	10% NaCl	27	≥ 18	2.75	0.73	5.8
162	10% NaCl (O <sub>2</sub> free N <sub>2</sub> )	27	≥ 18	2.75	0.82	5.3
150	3% NaCl	18	4.1	≥ 1.85	0.88	9.5
191	3% NaCl	16*	4.1	≥ 1.85	0.89	10.5
149	1% NaCl	16	2.8	≥ 1.60	0.78	9.1
134	10% NaNO <sub>3</sub>	27	≥ 18	2.75	0.56	4.7
143	3% NaNO <sub>3</sub>	18	4.1	≥ 1.85	1.30	13.6
135	5% Ca(NO <sub>3</sub> ) <sub>2</sub>	12	1.6	≥ 1.50	1.39	19.4
139	10% NaOH	17	3.9	≥ 1.80	1.27	13.6
141	5% Na <sub>2</sub> SO <sub>3</sub>	16	3.3	≥ 1.70	1.50	17.0
142	5% Na <sub>2</sub> S <sub>2</sub> O <sub>3</sub>	22	6.6	2.15	0.90	7.8
176	5% BaCl <sub>2</sub>	19	4.5	≥ 1.90	0.70	6.8
177	5% Co(NO <sub>3</sub> ) <sub>2</sub>	13	1.9	≥ 1.50	1.29	17.0
178	10% NaBr	42	≥ 90	7.70	0.48	3.2
179	10% KCl	35	≥ 80	4.80	0.54	2.5
180	10% LiCl	43	≥ 120	8.23	0.20	2.8
183	5% CaCl <sub>2</sub>	17	2.9	≥ 1.60	1.38	15.7

\* 330 ppm SO<sub>2</sub>

Experiments using lime with a number of deliquescent salt additives can also be simulated using the modified shrinking core model. The results obtained for the modelling of experiments run at 74 and 54% relative humidity are presented in Tables 5-1 and 5-2. A reasonably good agreement was found between the predictions of the model and the experimental results. The standard deviation was calculated using the experimental and predicted values of percentage of  $\text{Ca}(\text{OH})_2$  converted at intervals of five minutes of reaction time. The maximum percentage of error between the experimental data and predicted values is also presented in the tables. For most cases the maximum errors are below 10% with a few exceptions where it is below 20%.

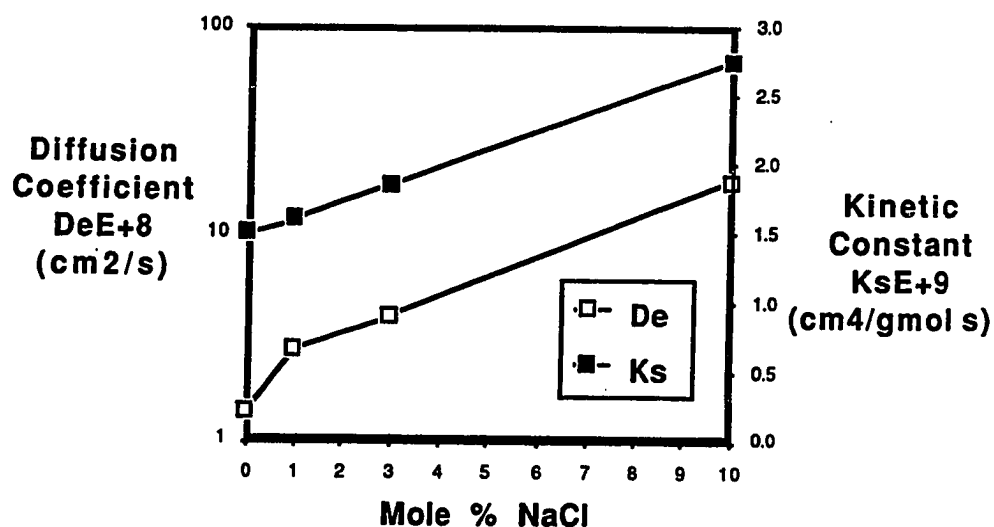


Figure 5-8: Effect of NaCl on the Model Parameters

The deliquescent salts affected the model parameters in a

similar way to the relative humidity, the diffusion coefficient increasing more rapidly than the kinetic constant.  $D_e$  values ranging from  $1.5E-8$  to  $120E-8$  ( $\text{cm}^2/\text{s}$ ) and  $k_g$  values from  $1.5E-9$  to  $8.23E-9$  ( $\text{cm}^4/\text{gmol s}$ ) were used in the simulation of the salt experiments. Depending on the amount and type of salt added, chemical reaction or  $\text{SO}_2$  diffusion can become the controlling step. Figure 5-8 illustrates the effect of NaCl on the model parameters. The kinetic constant increased linearly when NaCl concentration was increased from 0 to 10 mole%, while the diffusion coefficient increased exponentially after a sharp increase from 0 to 1 mole% NaCl.

## 5.6 Discussion

The only previous modelling effort for this reaction was the work of Klingspor et al. (1983, 1984). Their work used an integral shrinking core model with only reaction kinetics to explain the dependence of reaction rate on lime conversion. Their experimental data fit this integral shrinking core model only after a certain lime conversion had been reached. They attributed the sharp decrease on reaction rate observed at initial times to a decrease in surface roughness, but did not attempt to correlate this decrease in surface roughness with lime conversion. Their model neglects the effects of  $\text{SO}_2$  diffusion through the product layer and their model also neglected the  $\text{SO}_2$  concentration and lime concentration profiles in the fixed bed reactor. All of these factors will be more important at initial times, when the  $\text{SO}_2$  removal is higher, so it is not surprising that they were able to fit the the experimental data only at later times.

The simple model presented in this paper seems able to predict with reasonable accuracy the effect of all the process variables tested

and explain the trends observed in the experimental data. The experimental data are estimated to have 10% experimental error, so the predictions of the model are well within the range of experimental error in most cases. The values of the diffusion coefficient used in the modelling (from  $0.75\text{E-}9$  to  $1.20\text{E-}6$ ) seem reasonable for diffusion of  $\text{SO}_2$  in a solid, as they are of the same order of magnitude of the diffusivities of gases in polymers (Vieth and Amini, 1974, Brzozowski and Kumins, 1974, MacDonald and Haung, 1981, McBride et al., 1979, Minoura et al., 1981).

## 5.7 Conclusions

The modified shrinking core model presented in this chapter proved to be a very helpful in interpreting experimental data obtained in the fixed bed reactor. The most important process variable for the reaction is the relative humidity of the gas, which affects both the diffusion coefficient of  $\text{SO}_2$  and the kinetic constant. In the range of relative humidity studied (19 to 74%) the kinetic constant increased linearly with relative humidity while the diffusion coefficient increased exponentially. This dependence of the parameters on the relative humidity leads to a change in controlling mechanism as the relative humidity decreases. At high relative humidity and/or high  $\text{SO}_2$  concentration the reaction rate is kinetically controlled and the reaction rate is independent on the  $\text{SO}_2$  level. At low relative humidity and/or low  $\text{SO}_2$  concentration the controlling step is the diffusion of the  $\text{SO}_2$  through the  $\text{CaSO}_3 \cdot 1/2\text{H}_2\text{O}$  product layer. At these conditions the overall reaction rate becomes affected by the  $\text{SO}_2$  concentration which is the driving force for diffusion.

The addition of deliquescent salts increases the diffusion

coefficient and the kinetic constant in a similar way to the relative humidity, the diffusion coefficient increasing more rapidly than the rate constant. When increasing amounts of the same salt (NaCl) were added,  $k_s$  increased linearly and  $D_e$  nearly exponentially. Depending on the amount and type of salt additive, chemical reaction or gas diffusion can be the controlling mechanism.

The kinetic constant was a very weak function of temperature. The estimated activation energy was 2.9 kcal/gmol.

## Chapter 6

### Conclusions and Recommendations

#### 6.1 Conclusions

- Relative humidity is the most important variable affecting the reaction of  $\text{SO}_2$  and  $\text{Ca}(\text{OH})_2$ . At 500 ppm  $\text{SO}_2$ , increasing the relative humidity from 54 to 74% increased  $\text{Ca}(\text{OH})_2$  conversion after 1 hour of reaction from 12 to 23%.
- The reaction rate has zero order kinetics in  $\text{SO}_2$ .
- At high relative humidity and/or high  $\text{SO}_2$  concentration, the overall reaction rate is kinetically controlled.
- At low relative humidity and/or low  $\text{SO}_2$  levels, diffusion of  $\text{SO}_2$  through the solid product layer becomes the controlling step.
- Deliquescent salt additives increase the reaction rate of  $\text{SO}_2$  with  $\text{Ca}(\text{OH})_2$ . The extent of the increase depending on the type and concentration of the salt, and on the relative humidity.

- Deliquescence alone cannot explain the observed effect of the salt additives. Some of the salts show beneficial effect at relative humidities well below the values predicted by their deliquescent properties.
- A Shrinking core model with an empirical correlation to account for the decrease in the  $\text{Ca}(\text{OH})_2$  particles surface roughness due to reaction can be used to simulate the observed reaction rates with reasonable accuracy.
- The parameters of the model are the  $\text{SO}_2$  diffusion coefficient through the product layer ( $D_p$ ) and the kinetic constant ( $k_s$ ). Diffusion coefficient values ranging from  $0.75\text{E-}9$  to  $1.20\text{E-}6$  ( $\text{cm}^2/\text{s}$ ) and kinetic constant values ranging from 1.0 to  $8.23\text{E-}9$  ( $\text{cm}^4/\text{gmol s}$ ) can be used to simulate all the experimental results.
- Relative humidity and the presence of deliquescent salts affect both the kinetic constant and the  $\text{SO}_2$  diffusion coefficient.
- The diffusion coefficient increases exponentially with relative humidity and amount of salt added, while the kinetic constant increase linearly.
- The reaction rate has a weak temperature dependence, the estimated activation energy being 2.9 Kcal/gmol.
- The reaction product is mainly  $\text{CaSO}_3 \cdot 1/2\text{H}_2\text{O}$ . The oxygen present as impurity in the nitrogen oxidizes some of the

sulfite to sulfate. X-ray and Differential Scanning Calorimeter results indicate that the sulfate produced is present in solid solution with the  $\text{CaSO}_3 \cdot 1/2\text{H}_2\text{O}$ .

- The presence of small amounts of oxygen (< than 0.5%) as impurity of the nitrogen does not affect the reaction rate of  $\text{Ca(OH)}_2$  with  $\text{SO}_2$ .
- Organic acid additives such as adipic and glycolic acid decrease the  $\text{Ca(OH)}_2$  reactivity towards  $\text{SO}_2$ .
- Organic deliquescents such as monoethanolamine, ethylene glycol, and tri-ethylene glycol do not affect  $\text{Ca(OH)}_2$  reactivity.

## 6.2 Recommendations

- The present research was performed using as the gas phase a mixture of  $\text{SO}_2$  and  $\text{N}_2$ . Gases like  $\text{CO}_2$ ,  $\text{NO}_x$ , and  $\text{O}_2$  are important components of flue gas and their effect on the reaction rate of  $\text{SO}_2$  with  $\text{Ca(OH)}_2$  should be investigated. Some oxygen was present in our gas mixture as an impurity of the nitrogen and showed no effect on the  $\text{SO}_2$  absorption, but higher  $\text{O}_2$  levels may affect the reaction.
- Most of the experiments in this research were made using powder reagent  $\text{Ca(OH)}_2$  as the solid reactant, only a couple of experiments were made using pressure hydrated dolomitic lime. Additional sources of  $\text{Ca(OH)}_2$  should be tested. It would also be interesting to investigate the behavior of industrial samples of spray dryer solids.

- Additional research should be done on the effect of salt additives. It would be useful to further study the correlation between relative humidity and water retention of the solids in the presence and absence of additives.

**Appendix A.**  
**Solids Characterization**

### A.1 Coulter Counter particle size distribution

The particle size distribution of the  $\text{Ca}(\text{OH})_2$  powder reagent used in the experiments was determined using a Coulter Counter, model T<sub>AII</sub>. The Coulter Counter determines the number and size of particles suspended in a conductive liquid by forcing the suspension to flow through a small aperture. Electrodes are immersed in the conductive fluid on opposite sides of the aperture. As a particle passes through the aperture, it changes the resistance between the electrodes. This produces a current pulse of short duration having a magnitude proportional to the particle volume. The series of pulses is electronically classified by size and counted.

The Coulter Counter method has been extensively used in limestone dissolution studies (Chan, 1981, Chan and Rochelle, 1982, Toprac, 1981) and  $\text{CaSO}_3$  crystallization studies (Tseng, 1984). It has proved to be efficient, reliable, and reproducible in measuring particle size distribution in micrometer size ranges. The particle size distributions of the two batches of  $\text{Ca}(\text{OH})_2$  used in the experiments, namely lime 0 and lime A are presented in Table A-1. The median of the particle size distribution is 7.4  $\mu\text{m}$  for lime 0 and 5.6  $\mu\text{m}$  for lime A. The electrolyte used was 4 wt%  $\text{CaCl}_2$ , saturated with  $\text{Ca}(\text{OH})_2$  (to minimize lime dissolution). A nonionic dispersant agent (Coulter Type IA) was also added to the electrolyte solution to prevent agglomeration of the lime particles.

The particle size distribution of lime 0 was measured using a single 140  $\mu\text{m}$  aperture tube, but a multi aperture analysis was needed to cover the complete size range of lime A. The particle size distribution was measured with the 140  $\mu\text{m}$  aperture tube. Part of the sample was

**Table A-1: Ca(OH)<sub>2</sub> Particle Size Distributions**

Effective Diameter ( $\mu\text{m}$ )	Volume% between the two diameters	
	Lime 0	Lime A
1.00	-	1.0
1.26	-	2.1
1.59	-	2.9
2.00	1.4	4.5
2.52	3.0	6.3
3.17	1.6	7.6
4.00	3.4	8.8
5.04	7.8	10.8
6.35	16.7	13.5
8.00	22.7	13.9
10.08	18.9	12.2
12.7	8.5	7.8
16.0	4.9	4.2
20.2	3.1	1.8
25.4	2.2	1.2
32.0	3.3	0.5
40.3	2.5	0.9
50.8	0	0
<b>Median of Distribution</b>	<b>7.4 <math>\mu\text{m}</math></b>	<b>5.6 <math>\mu\text{m}</math></b>

then "scalped" by wet sieving through a 20  $\mu\text{m}$  sieve, and the size distribution of the subsieved suspension measured with a 50  $\mu\text{m}$  aperture tube. The overlap between the size distributions measured with each tube was used to normalize the distribution using the volume percent method described in the Coulter Counter Operator's Manual (Coulter, 1980).

$\text{Ca}(\text{OH})_2$  powder reagent was used in most of the experiments, but three samples of pressure hydrated dolomitic lime, provided by John Chang of Acurex, were also tested for their reactivity towards  $\text{SO}_2$ . The particle size distributions of these samples of dolomitic lime could not be determined using the Coulter Counter method. As will be discussed in the Scanning Electron Microscope section, these dolomitic limes consist mostly of agglomerates of very small particles (of the order of 1  $\mu\text{m}$  or below) that are below the size range that can be measured using the Coulter Counter. The smallest tube available for the Coulter Counter has an aperture of 50  $\mu\text{m}$ , and it can measure particles greater than 1  $\mu\text{m}$ .

## A.2 BET Surface Area Measurement

The standard method for measuring surface area of porous solids is the Brunauer-Emmett-Teller (BET) method (Brunauer et al., 1938). The BET method is based on the physical adsorption of a gas, normally nitrogen at its normal boiling point (- 195.8 K), on the surface of the solid. The method involves measuring the amount of nitrogen adsorbed ( $v$ ) over a range of nitrogen pressures ( $p$ ) below 1 atm.

The BET equation can be written as:

$$\frac{p}{v(p_o - p)} = \frac{1}{v_m C} + \frac{(C - 1) p}{C v_m p_o} \quad (A.1)$$

Where  $p_o$  is the saturation pressure,  $C$  is a constant for the particular temperature and gas-solid system, and  $v_m$  is the volume of gas required to form a complete unimolecular adsorbed layer. A plot of  $p/v(p_o - p)$  versus  $p/p_o$  will give a straight line. Extrapolating this straight line to  $p/p_o = 0$  gives the intercept  $I$ . The intercept together with the slope  $S$  of the line gives  $v_m$  as:

$$v_m = \frac{1}{I + S} \quad (A.2)$$

Once  $v_m$  is known, the surface area of the solid can be calculated as:

$$S_g = \frac{v_m N_o}{V} \alpha \quad (A.3)$$

Where:

$N_o$  = Avogadro's Number

$V$  = molar volume of the gas at the conditions of  $v_m$

$\alpha$  = surface area of one adsorbed molecule

The BET approach is essentially an extension of the Langmuir approach to multimolecular layers. It assumes that the rate of condensation of the gas on the bare surface of the solid is equal to the rate of evaporation from the first layer, and that the heat of adsorption in layers other than the first is equal to the heat of liquefaction of the adsorbate material (ie, Van der Waals forces of the adsorbent are transmitted only to the first layer (Brunauer et al., 1938, Hill, 1977)).

**Table A-2: BET Surface Area of the Solids**

Sample	BET Surface Area (m <sup>2</sup> /g)
<b>Reagent Grade Calcium Hydroxide</b>	
Lime 0 (non-slurried)	8.2
Lime A (non-slurried)	9.4
Lime A (slurried)	8.8
Lime A + 5 mole% CaCl <sub>2</sub> ·2H <sub>2</sub> O	7.7
Lime A + 10 mole% NaCl	8.1
Lime A + 10 mole% NaNO <sub>3</sub>	7.0
Lime A + 10 mole% KCl	9.3
Lime A + 10 mole% NaBr	8.6
Lime A + 10 mole% LiCl	9.6
Lime A + 5 mole% Co(NO <sub>3</sub> ) <sub>2</sub>	7.2
Lime A + 5 mole% BaCl <sub>2</sub> ·2H <sub>2</sub> O	7.2
Reacted Lime A (25% conversion)	6.5
Reacted Lime A + 10 mole% NaCl (46% conversion)	5.9
<b>Pressure-Hydrated Dolomitic Lime</b>	
after hydrator	20.1
after ball mill	21.1
sieved material after ball mill (< 125 μm)	18.4

The surface area given by the BET method may not correspond exactly to the surface area of the solid, but the procedure is standardized and the results are reproducible (Smith, 1981, Rase, 1977).

The BET surface area of  $\text{Ca}(\text{OH})_2$  and  $\text{Ca}(\text{OH})_2$  with salt additives was measured in the laboratory using an Accusorb Model 2100E Physical Adsorption Analyzer. The adsorbent used was nitrogen at its normal boiling point. The results obtained are listed in Table A-2. The surface areas of limes O and A were 8.2 and 9.4  $\text{m}^2/\text{g}$  respectively. The surface area of samples of lime A with different salt additives was found to be in the range 7.0 to 9.6  $\text{m}^2/\text{g}$ . In most cases a small decrease of the surface area occurred with the addition of the deliquescent salt. The surface area of pure lime A after being slurried with distilled water and dried in the same way as when salt additives were added showed a slight decrease of surface area to 8.8  $\text{m}^2/\text{g}$ . Measurement of surface area of reacted  $\text{Ca}(\text{OH})_2$  solids showed a decrease in surface area with conversion. Pure reacted  $\text{Ca}(\text{OH})_2$  (25% conversion) has a surface area of 6.5  $\text{m}^2/\text{g}$ , while reacted  $\text{Ca}(\text{OH})_2$  with NaCl as additive (46% conversion) has a surface area of 5.9  $\text{m}^2/\text{g}$ .

Finally, the surface area of three samples of pressure hydrated dolomitic lime were measured. The samples correspond to dolomitic lime collected after the lime leaves the hydrator (hydrator lime), dolomitic lime collected after the lime leaves the ball mill (ball mill lime) and a sample of ball mill lime sieved through a 125  $\mu\text{m}$  sieve (sieved ball mill lime). The surface area of these dolomitic lime samples was in the range 18.4 to 21.1  $\text{m}^2/\text{g}$ .

### A.3 Scanning Electron Microscope (SEM)

The Scanning Electron Microscope (SEM) is one of the most versatile instruments available for the examination and analysis of the microstructural characteristics of solids objects (Goldstein et al., 1975). It is a surface examination tool. The surface to be examined is irradiated with a finely focused electron beam. When the electron beam impinges on a specimen surface different types of signals are produced: secondary electrons, backscattered electrons, characteristic x-rays, Auger electrons, and photons of various energies. In the SEM the primary signal of interest is the variation in secondary electron emissions that takes place as the electron beam is swept in a raster across the surface of a specimen due to differences in surface topography. The secondary electron yield is confined near the beam impact area, which permits images to be obtained at relatively high resolutions. The three dimensional appearance of the images is due to the large depth of focus of the SEM.

A SEM JEOL, model JSM-3C was used to examine the  $\text{Ca}(\text{OH})_2$  and hydrated lime samples, along with reaction products. The powdery samples were sprinkled over a thin film of graphite glue previously spread on a SEM stage. After the glue was dried, a thin layer of conductive element (Al or Au-Pd alloy) was applied to the sample by vacuum evaporation at high temperature. The conductive applied layer must be as thin as possible so that it does not obscure fine details of the sample under observation, but it must be continuous in order to provide a conductive path to ground.

The SEM micrographs of the two batches of  $\text{Ca}(\text{OH})_2$  (lime 0 and lime A) used in most of the experiments are shown in Figures A-1

to A-4. Figures A-1 and A-3 correspond to 400 magnification, and Figures A-2 and A-4 to 4000 magnification. The figures confirm that the  $\text{Ca(OH)}_2$  particles are in the micron size range. The particles are of irregular shape and have a lot of surface irregularities and roughness. No pores were visible.

SEM micrographs of the  $\text{Ca(OH)}_2$  with different salt additives showed no significant difference in size or shape from the pure  $\text{Ca(OH)}_2$  particles. This is illustrated by Figure A-5 that shows the SEM micrograph of a sample of  $\text{Ca(OH)}_2$  with 10 mole% NaCl at 10000 magnification.

Observation of reacted samples of  $\text{Ca(OH)}_2$  showed that the surface of the particles is more globular. This is illustrated by Figure A-6 which shows a micrograph of reacted  $\text{Ca(OH)}_2$  with 10 mole% NaCl with a conversion of 46% (determined by chemical analysis).

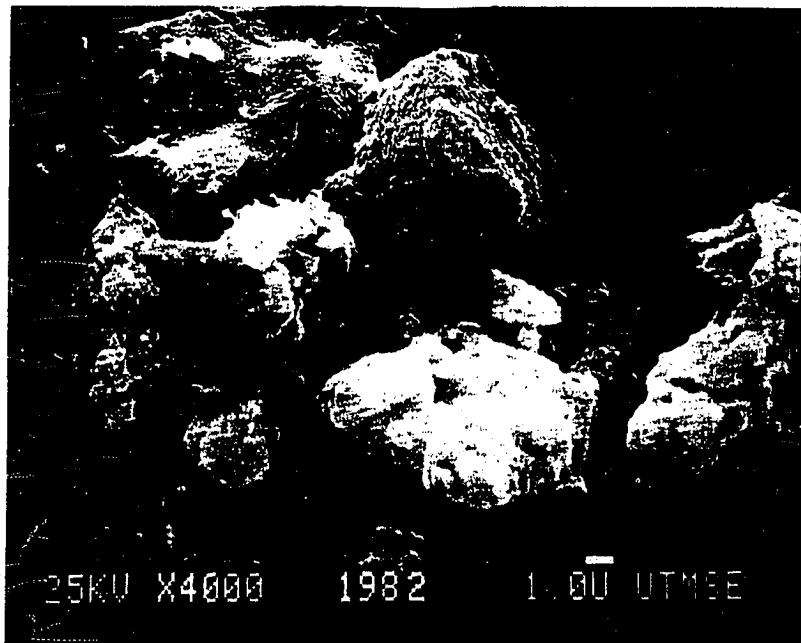
Finally, Figures A-7 to A-10 show SEM micrographs of pressure hydrated dolomitic lime at 400 and 4000 magnification. These dolomitic limes have some very large particles of 40 to over 100  $\mu\text{m}$  diameter, but most of the particles are very small, below 2  $\mu\text{m}$ , and tend to form agglomerates.

#### A.4 Energy Dispersive Spectroscopy (EDS)

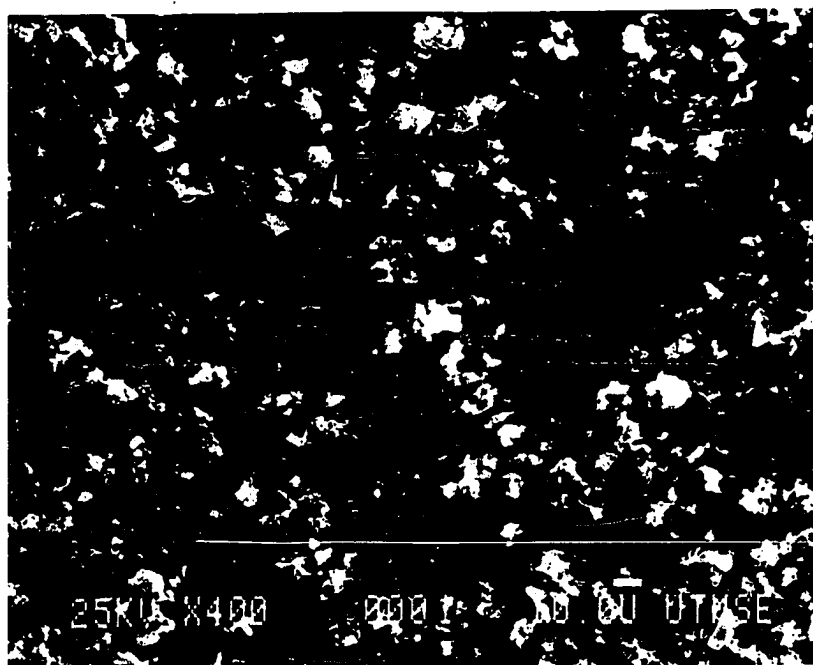
As was mentioned in the section dealing with the SEM, when a electron beam impinges the surface of a sample, characteristic x-rays are produced together with other types of signals. Energy dispersive spectroscopy uses a x-ray detector that separates the x-ray spectrum by energy rather than by wavelength. This energy dispersive detector is



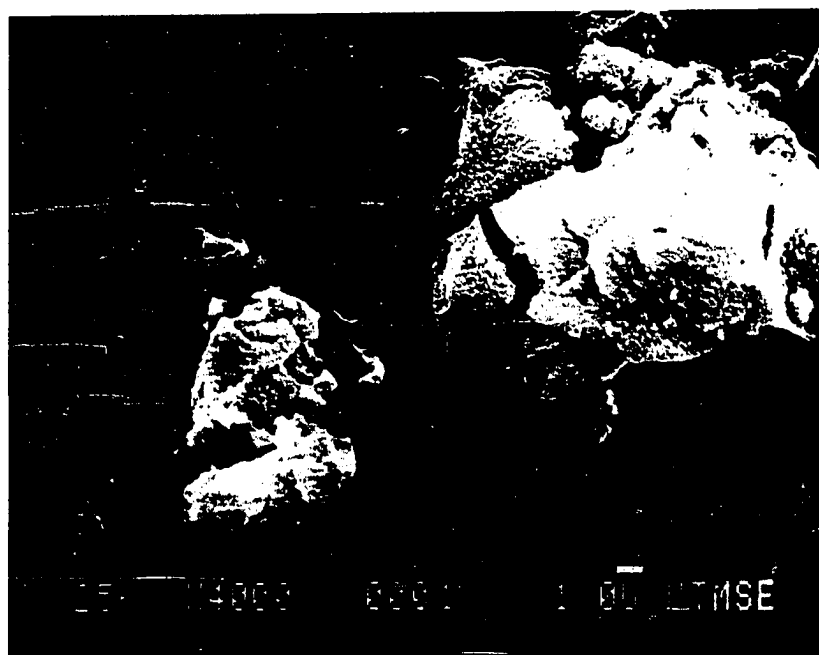
**Figure A-1:** SEM Micrograph Lime 0, 400 Magnification



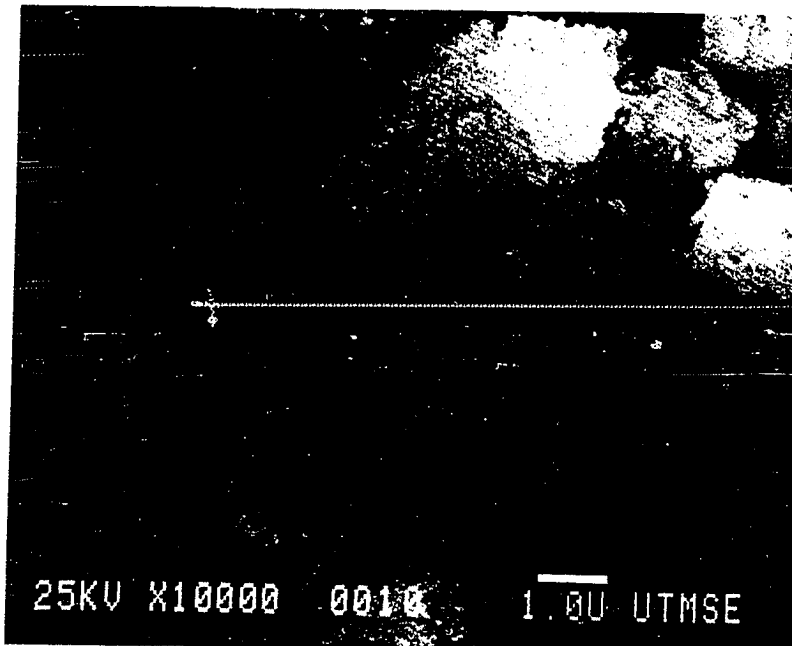
**Figure A-2:** SEM Micrograph Lime 0, 4000 Magnification



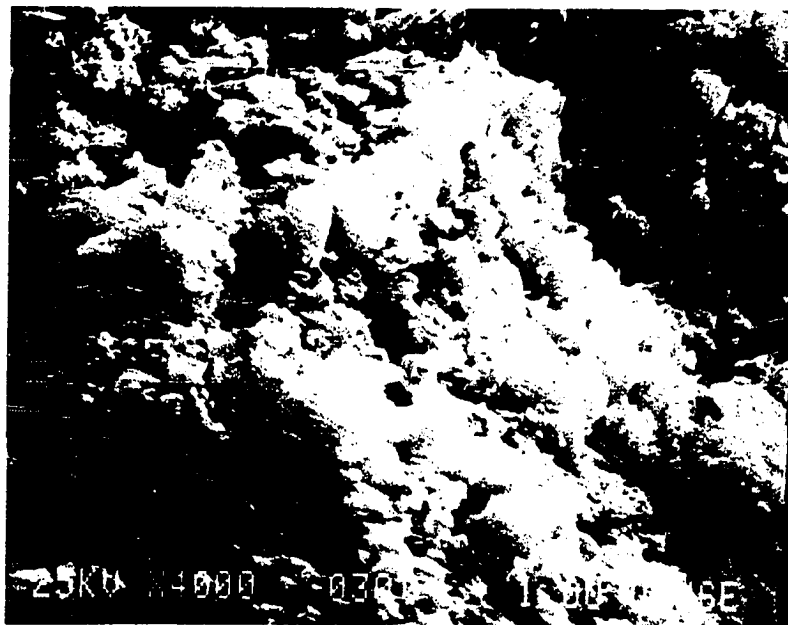
**Figure A-3:** SEM Micrograph Lime A, 400 Magnification



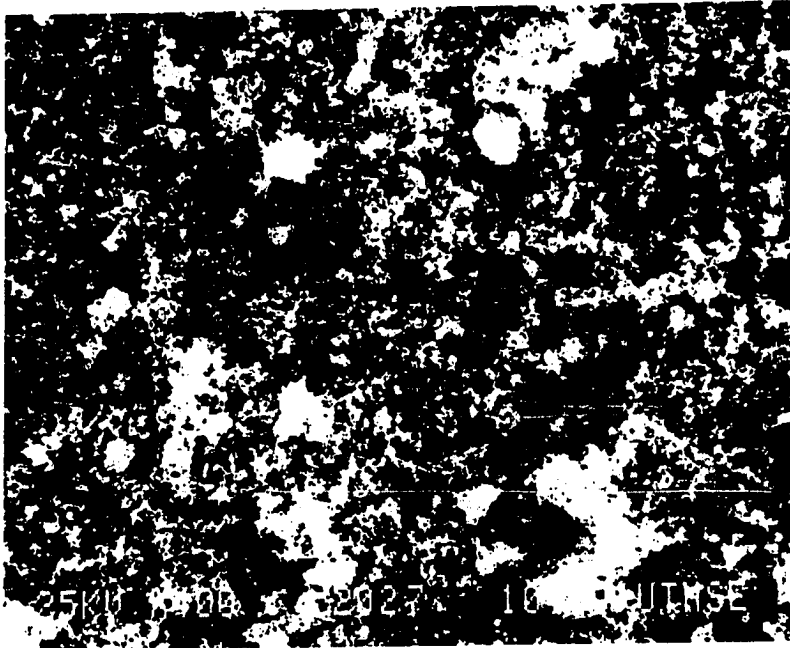
**Figure A-4:** SEM Micrograph Lime A, 4000 Magnification



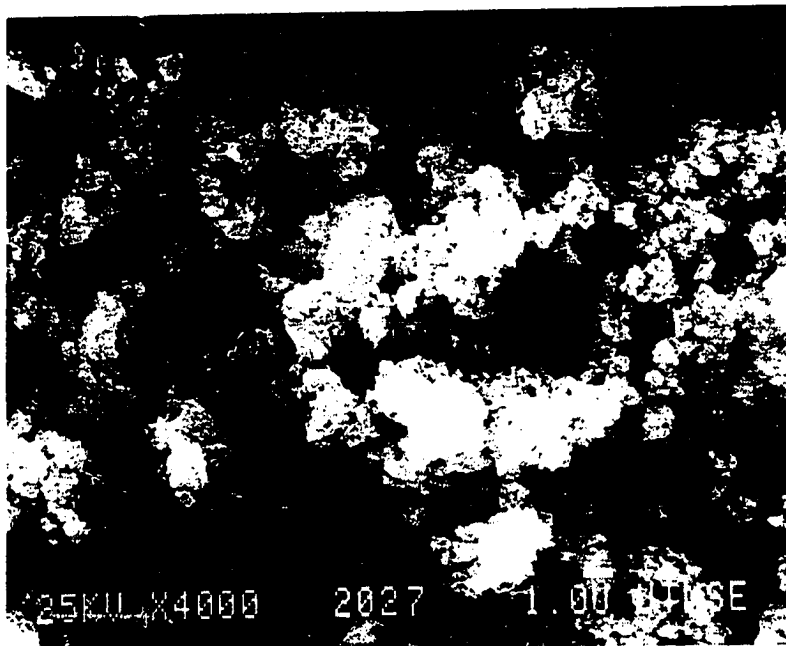
**Figure A-5:** SEM Micrograph  $\text{Ca}(\text{OH})_2$  + 10 mole% NaCl,  
10000 Magnification



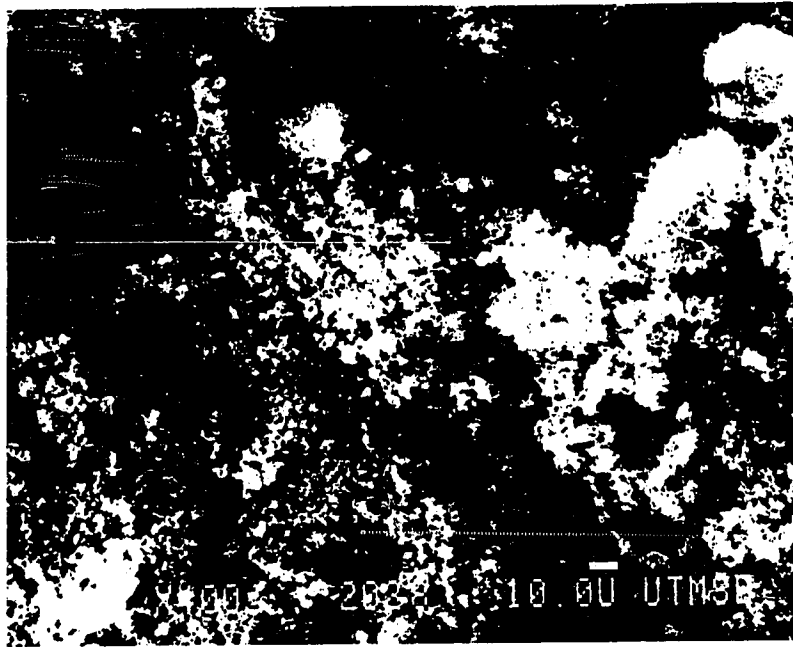
**Figure A-6:** SEM Micrograph Reacted Lime A + 10 mole% NaCl,  
4000 Magnification, 74% RH, 500 ppm  $\text{SO}_2$ ,  
64.4°C, 2 hr Reaction Time, Conversion 46%



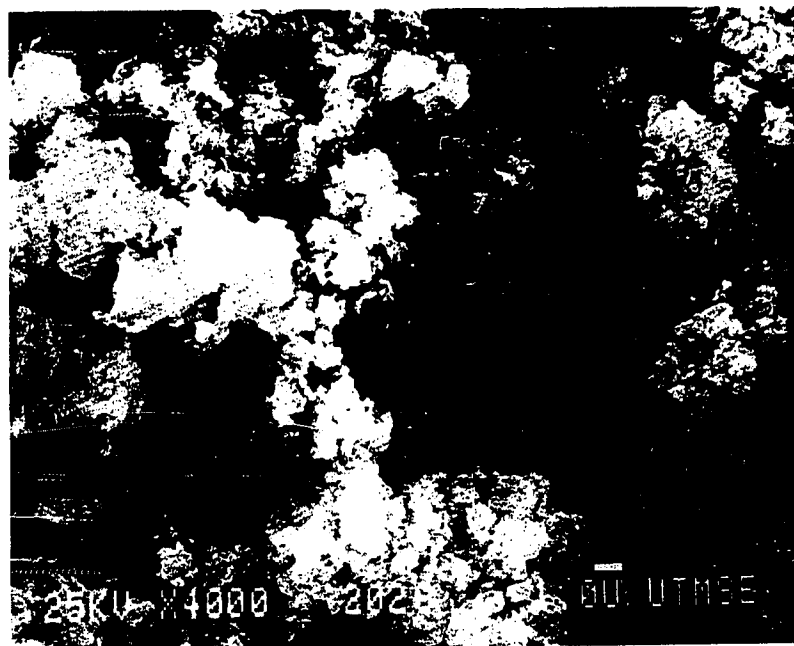
**Figure A-7:** SEM Micrograph Ball Mill Hydrated Dolomitic Lime, 400 Magnification



**Figure A-8:** SEM Micrograph Ball Mill Hydrated Dolomitic Lime, 4000 Magnification



**Figure A-9:** SEM Micrograph Hydrator Hydrated Dolomitic Lime, 400 Magnification



**Figure A-10:** SEM Micrograph Hydrator Hydrated Dolomitic Lime, 4000 Magnification

incorporated within the SEM and possesses enough sensitivity to provide x-ray spectral data at the low SEM beam current. Quantitative analysis using EDS, involves accurately measuring the intensity of spectral lines corresponding to preselected elements for both sample and standards under identical operating conditions. The intensity ratio (relative x-ray intensity ratio between the elements of interest in the sample and the same elements in the standards) is calculated, and from the intensity ratio, the weight fraction of the elements of interest in the sample are estimated. A limitation of the EDS is that it can not identify elements of molecular weight below sodium.

EDS was used to estimate the elemental analysis of reacted and unreacted samples of  $\text{Ca}(\text{OH})_2$  with salt additives. An example of this type of analysis is given in Table A-3 which shows the weight percent of Cl and S in a reacted sample of lime with NaCl as additive. The conversion of this sample (given by chemical analysis) was 30%. The analysis was done for a great number of particles (bulk) and for individual particles. From the results presented in Table A-3 it can be concluded that the additive (in this case NaCl) is more or less uniformly distributed on the lime particles. The lime conversion was very uniform in the particles analyzed. For comparison purposes, the concentrations of Cl and S obtained by chemical analysis are also presented in the table.

EDS was also used to analyze a sample of pressure hydrated dolomitic lime. The analysis showed the dolomitic lime to contain 40.7 mole% Mg and 59.3 mole% Ca. Oxygen and hydrogen can not be analyzed.

**Table A-3: Elemental Analysis using EDS**

Sample: Converted Lime A + 10 mole% NaCl

54% RH, 66°C, 500 ppm SO<sub>2</sub>, 1 hr Reaction Time, 30% Conversion

	Wt% Cl	Wt% S
Bulk	4	17
Individual Particle	9	17
”	4	14
”	5	18
”	3	17
”	5	17
<hr/>		
From Chemical Analysis	7	18

**A.5 Differential Scanning Calorimetry (DSC)**

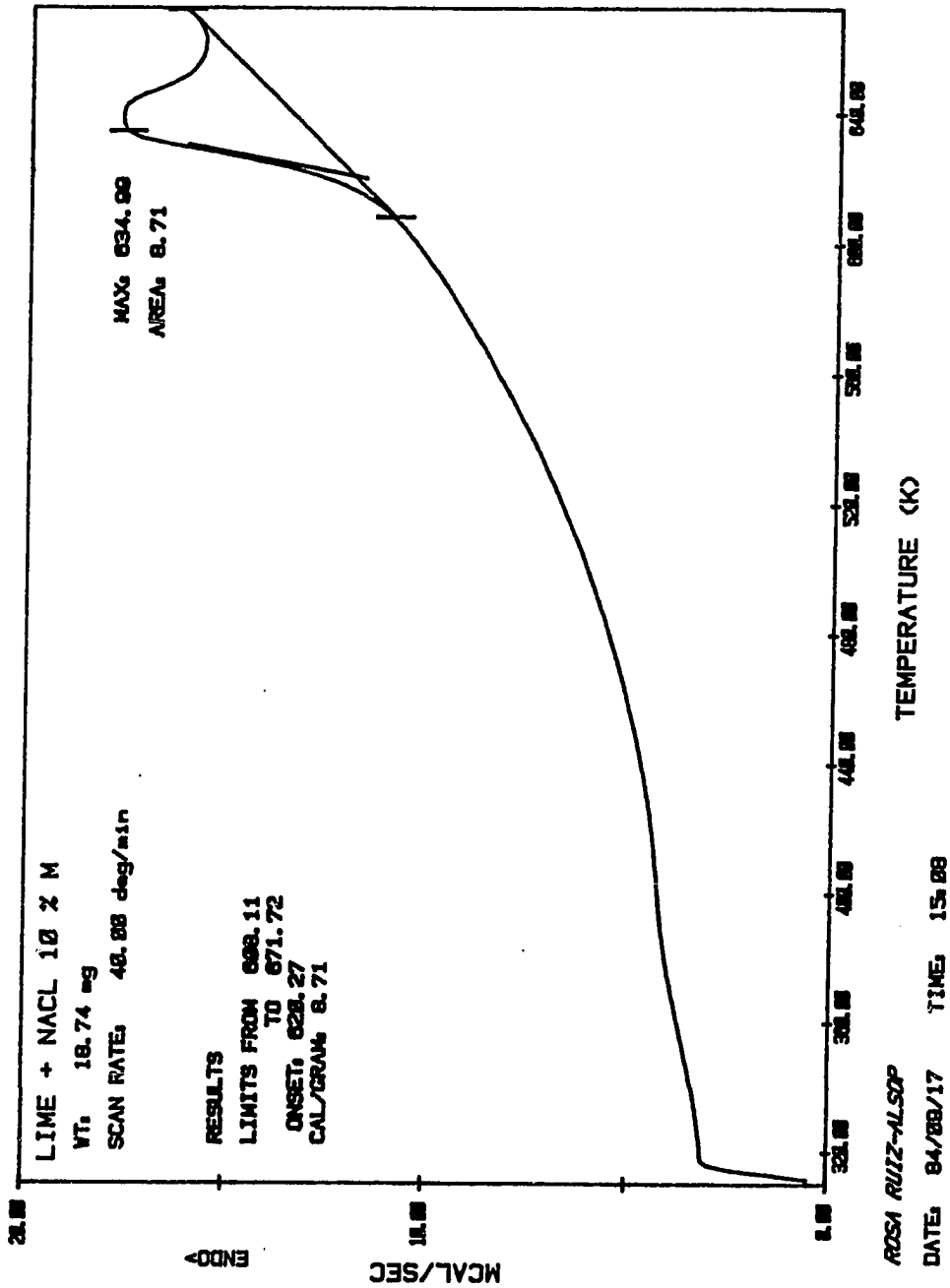
The scanning differential calorimeter determines the enthalpy change of a sample as a function of temperature. The enthalpy change is determined by measuring the differential heat flow required to maintain the sample and an inert reference at the same temperature (Mortimer, 1984). The temperature is programmed to increase linearly at a predetermined rate. Phase changes will be marked by rapid changes in  $dH/dt$  or, in other words rapid changes in heat capacity.

Peaks should appear in the  $dH/dt$  versus temperature curve in the temperature ranges of 120 - 140°C for gypsum, 150 - 170°C for calcium sulfate hemihydrate, and 350 - 430°C for calcium sulfite

hemihydrate (Jones et al., 1976, Tseng, 1984). These heat capacity changes correspond to the loss of hydrated water in the solids.

A Perkin-Elmer Differential Scanning Calorimeter (Model DSC-2) was used to characterize reacted samples of  $\text{Ca}(\text{OH})_2$  with and without salt additives. Some of these samples were obtained using nitrogen of 99.5% purity as the carrier for  $\text{SO}_2$ , and others using oxygen free nitrogen (99.998% purity) as the carrier. Figure A-11 shows a typical DSC curve of a sample of reacted  $\text{Ca}(\text{OH})_2$  with 10 mole% NaCl as additive. This sample was obtained by using oxygen of 99.5% purity. The change in heat capacity occurs at 652 K (378.9°C), which correspond to the endothermic dehydration of  $(\text{CaSO}_3)_x(\text{CaSO}_4)_{1-x} \cdot 1/2\text{H}_2\text{O}$  solid solutions. No peak was found in the 120-140°C range which indicates that no gypsum phase is present. Also no peak was detected in the 150-170°C range which means that no  $\text{CaSO}_4 \cdot 1/2\text{H}_2\text{O}$  phase is present. Any sulfate produced in the reactor will then be present in solid solution with  $\text{CaSO}_3 \cdot 1/2\text{H}_2\text{O}$ , and not as separate phases of  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$  or  $\text{CaSO}_4 \cdot 1/2\text{H}_2\text{O}$ .

The DSC curves of reacted  $\text{Ca}(\text{OH})_2$  with and without NaCl additive run using oxygen free nitrogen (99.998% purity) are shown in Figures A-12 and A-13 respectively. Again, only one peak is present in the DSC curves, in the 638 to 652 K range, which corresponds to the endothermic dehydration of  $(\text{CaSO}_3)_x(\text{CaSO}_4)_{1-x} \cdot 1/2\text{H}_2\text{O}$ .



**Figure A-11:** DSC Curve Reacted  $\text{Ca}(\text{OH})_2$  + 10 mole% NaCl,  
 $\text{N}_2$  of 99.5% purity, 54% RH, 66°C, 500 ppm  $\text{SO}_2$ ,  
 1 hr Reaction Time, Conversion 30%

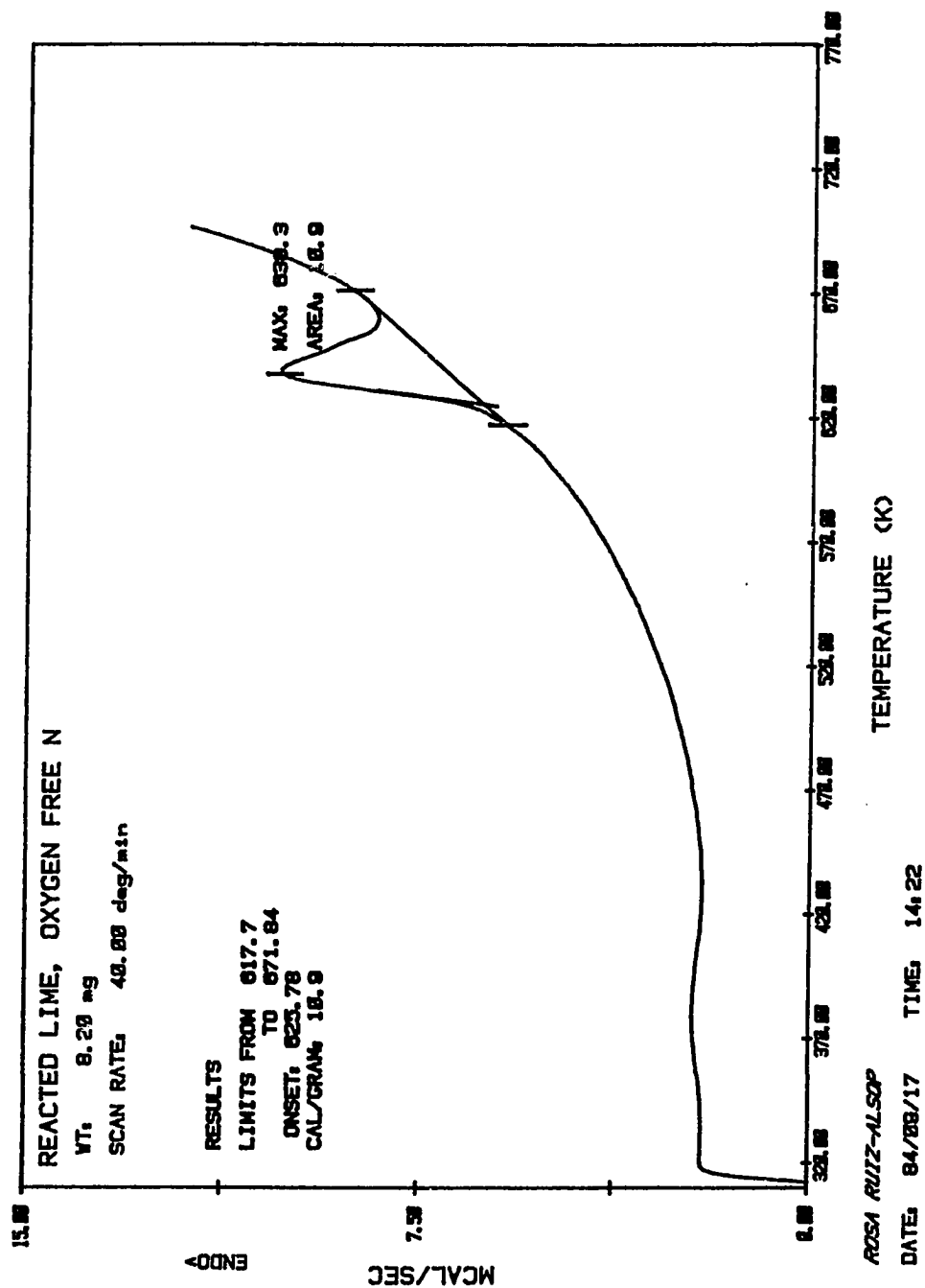


Figure A-12: DSC Curve Reacted  $\text{Ca}(\text{OH})_2$ ,  $\text{O}_2$  Free  $\text{N}_2$ , 74% RH,  
 64.4°C, 500 ppm  $\text{SO}_2$ , 1 hr Reaction Time,  
 Conversion 24.5%

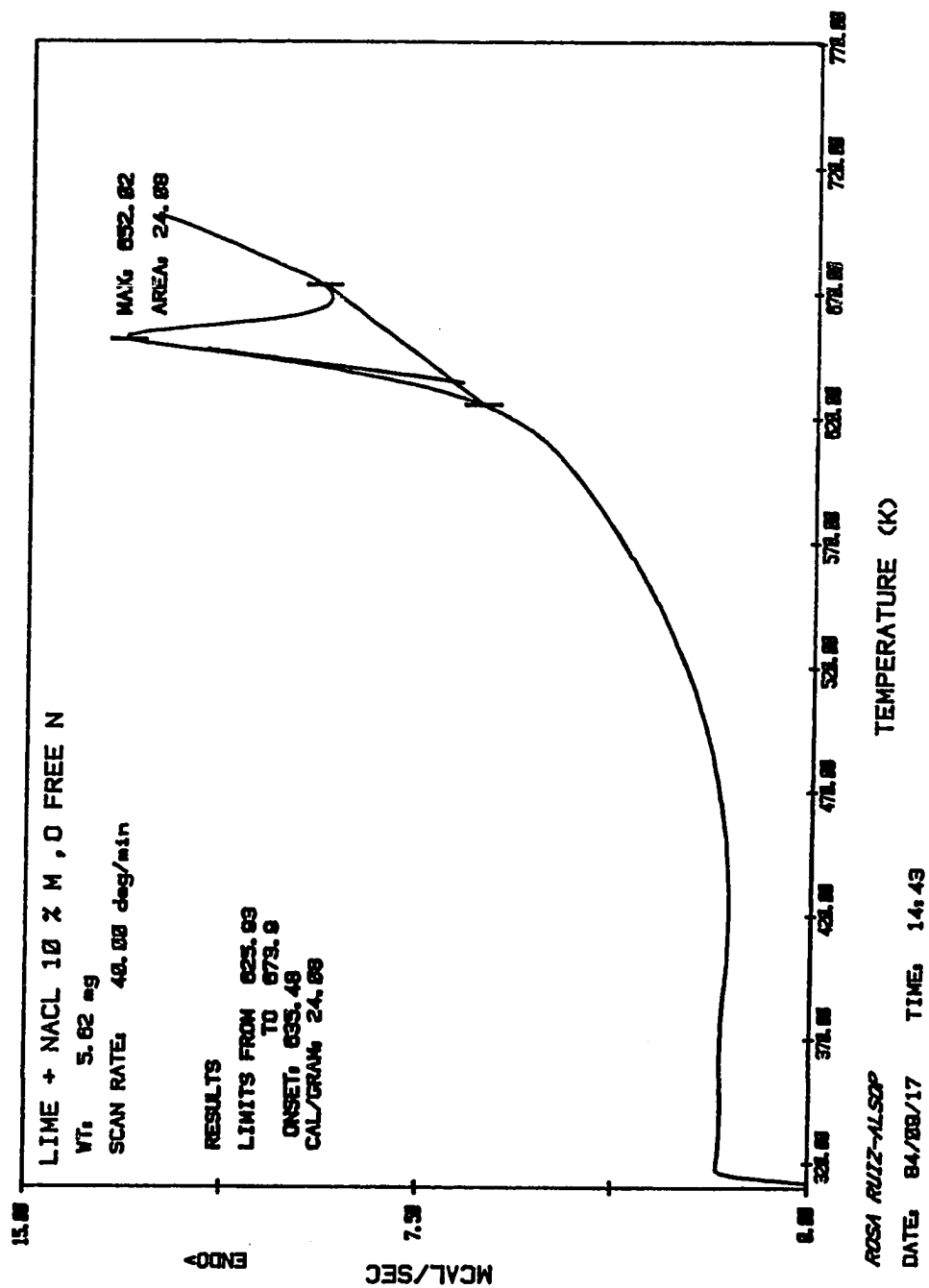


Figure A-13: DSC Curve Reacted  $\text{Ca}(\text{OH})_2$  + 10 mole% NaCl,  
 $\text{O}_2$  Free  $\text{N}_2$ , 74% RH, 64.4°C, 500 ppm  $\text{SO}_2$ ,  
 2 hr Reaction Time, Conversion 46%

## A.6 X-Ray Diffraction

X-ray powder diffraction was used to characterize the reactants and products. The x-ray diffraction method is based on the scattering of x-rays by the crystals, the scattering being caused by the electron atmosphere of the atom. When certain geometrical conditions as expressed by the Bragg law are satisfied, a diffraction pattern is produced by the scattering.

The Bragg law states:

$$\lambda = 2 d \sin \theta$$

Where:

$\lambda$  = x-rays wavelength

$d$  = lattice spacing

$\theta$  = diffraction angle

The diffraction pattern produced can be used to identify molecules, and to determine their atomic and molecular structure (Olsen, 1975).

The x-ray diffraction pattern of  $\text{Ca(OH)}_2$ , and  $\text{Ca(OH)}_2$  with different salt additives are shown in Figures A-14 to A-21. The X-ray diffraction pattern gives intensity versus  $2\theta$ .  $\text{Ca(OH)}_2$  has eight major peaks in its x-ray diffraction pattern (JCPDS, 1984). The d-spacing of these major peaks is 4.90, 3.11, 2.63, 1.93, 1.80, 1.69, 1.48, and 1.45 Å, which correspond to diffraction angles of 9.03, 14.33, 16.85, 23.55, 25.3, 27.11, 31.27, and 32.11 degrees respectively. These peaks appear in the  $\text{Ca(OH)}_2$  diffraction pattern shown in Figure A-14.

Figure A-15 shows the x-ray diffraction pattern of  $\text{Ca(OH)}_2$

UNIT NUMBER 1 LOG NUMBER 413 TIME: 14:45:45 DATE: 4/20/84  
STEP INCREMENT= .050 TIME/STEP(SEC)= 1.500 NPTS= 1201  
SLURRIED LIME

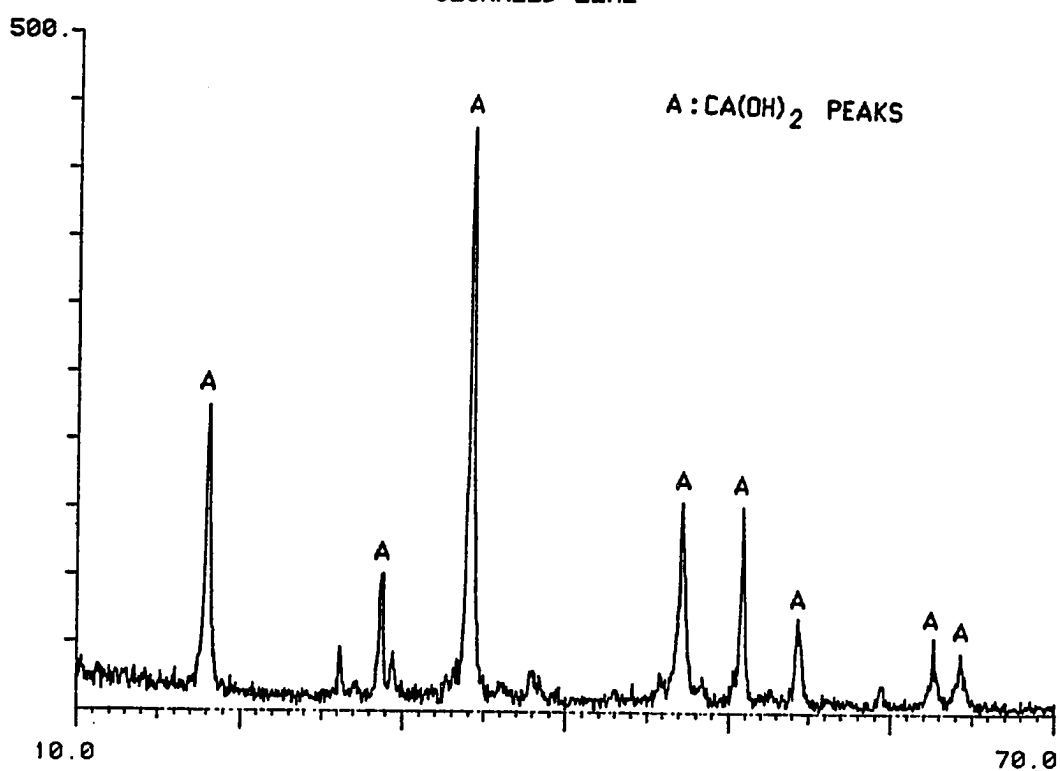


Figure A-14: X-ray Diffraction Pattern: Slurred  $\text{Ca(OH)}_2$

UNIT NUMBER 1 LOG NUMBER 654 TIME: 14: 1:40 DATE: 10/15/84

STEP INCREMENT= .050 TIME/STEP(SEC)= 1.500 NPTS= 1201

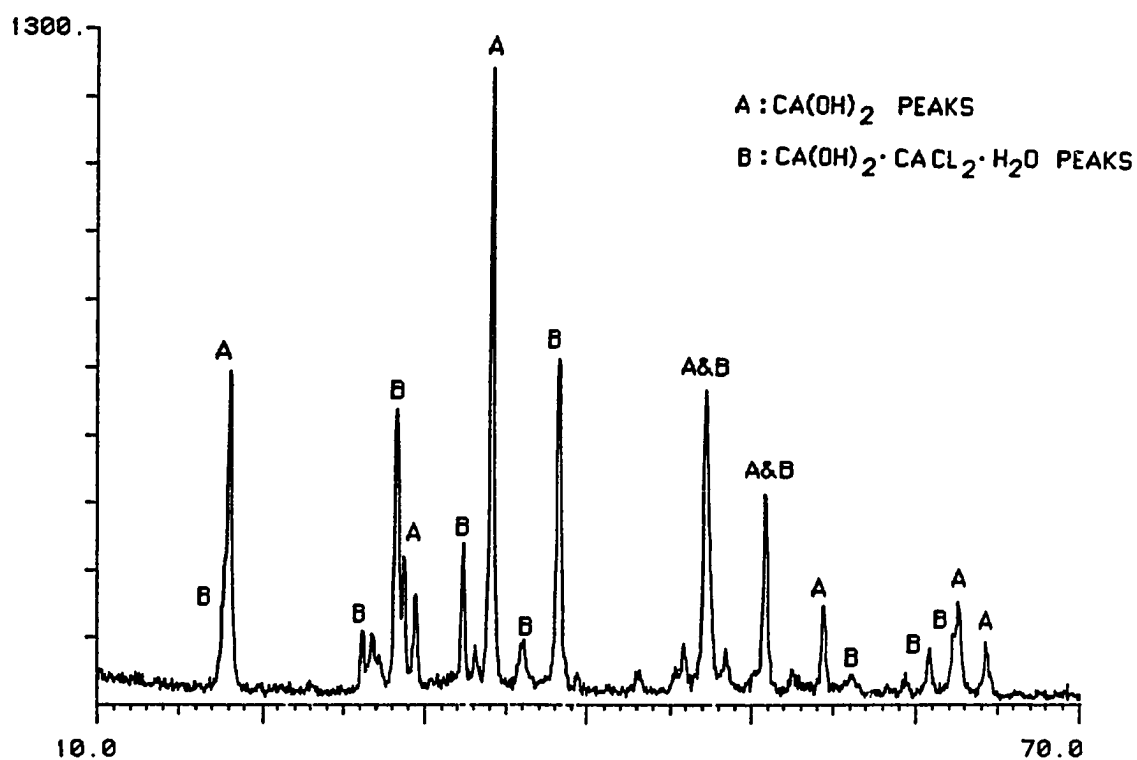
LIME + 20 % M  $\text{CaCl}_2 \cdot 2\text{H}_2\text{O}$ 

Figure A-15: X-Ray Diffraction Pattern:  $\text{Ca(OH)}_2$  with  
20 mole%  $\text{CaCl}_2 \cdot 2\text{H}_2\text{O}$

with 20 mole%  $\text{CaCl}_2 \cdot 2\text{H}_2\text{O}$  as additive. Neither anhydrous  $\text{CaCl}_2$  nor any of the calcium chloride hydrates was detected, but the x-ray diffraction pattern shows the presence of the mixed salt  $\text{CaCl}_2 \cdot \text{Ca}(\text{OH})_2 \cdot \text{H}_2\text{O}$ . The five major peaks of  $\text{CaCl}_2 \cdot \text{Ca}(\text{OH})_2 \cdot \text{H}_2\text{O}$  (JCPDS, 1984) are indicated in Figure A-15.

Figures A-16 to A-21 show the x-ray diffraction patterns of  $\text{Ca}(\text{OH})_2$  with  $\text{NaCl}$ ,  $\text{NaNO}_3$ ,  $\text{LiCl}$ ,  $\text{KCl}$ ,  $\text{BaCl}_2 \cdot 2\text{H}_2\text{O}$ , and  $\text{NaBr}$  as additives. The peaks corresponding to the solid phase detected in each sample are labeled in the Figures. Table A-4 is a summary of the x-ray diffraction work showing the additive added to the lime in its original form, and the solid phase detected by x-ray diffraction analysis.

In most cases the additive remains unchanged after being added to the lime by the slurring and drying process mentioned in Section 3.1, and precipitate in a separate phase. In some cases the hydration state of the additive changes, but in most cases it remains unaltered. The exception is  $\text{CaCl}_2$ , where the mixed salt  $\text{CaCl}_2 \cdot \text{Ca}(\text{OH})_2 \cdot \text{H}_2\text{O}$  is formed. This finding agrees with data reported in the literature for the equilibrium of the  $\text{Ca}(\text{OH})_2 \cdot \text{CaCl}_2 \cdot \text{H}_2\text{O}$  system (Seidell and Linke, 1958). In the case of  $\text{Ca}(\text{NO}_3)_2$  additive, the formation of the solid phase  $\text{Ca}_2\text{N}_2\text{O}_7 \cdot 2\text{H}_2\text{O}$  has been reported in the literature (Seidell and Linke, 1958). The presence of this solid phase could not be confirmed by x-ray diffraction analysis as the diffraction pattern of  $\text{Ca}_2\text{N}_2\text{O}_7 \cdot 2\text{H}_2\text{O}$  was not available.

When reacted samples of  $\text{Ca}(\text{OH})_2$  with and without  $\text{NaCl}$  were analyzed using x-ray diffraction, the presence of calcium sulfite hemihydrate was detected. Figures A-22 and A-23 show the diffraction

UNIT NUMBER 1 LOG NUMBER 408 TIME: 10:14:19 DATE: 4/18/84  
STEP INCREMENT= .050 TIME/STEP(SEC)= 1.500 NPTS= 1201  
NACL 10 % MOLAR + LIME

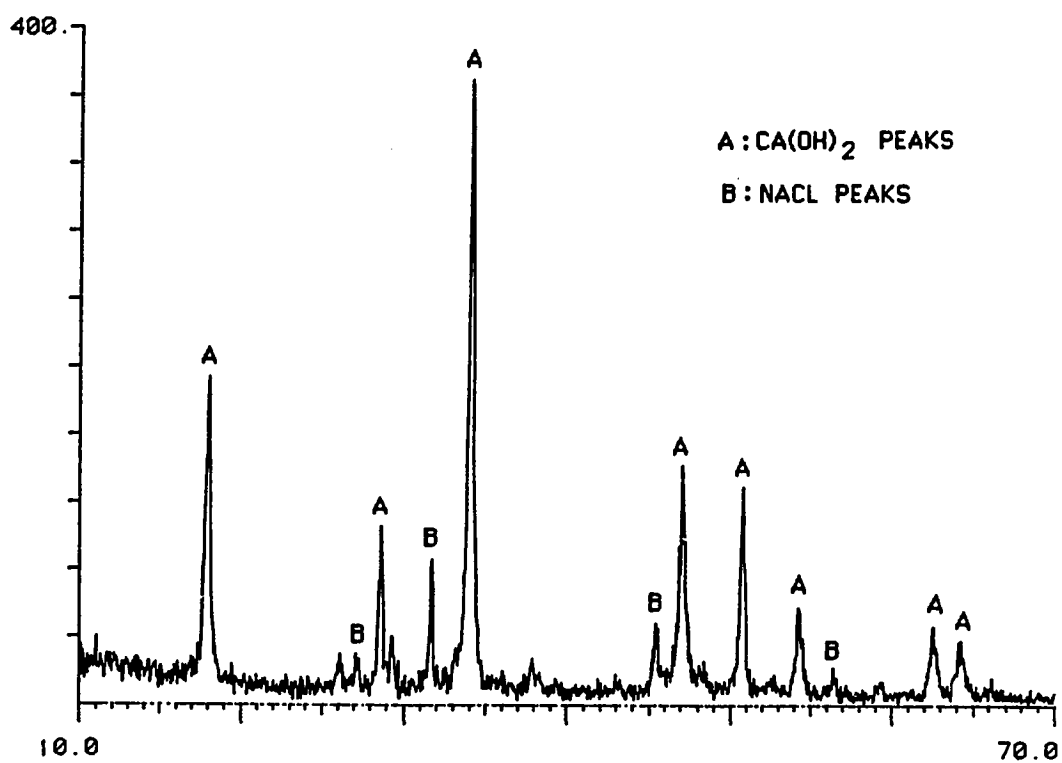


Figure A-16: X-ray Diffraction Pattern:  $\text{Ca(OH)}_2$  with  
10 mole% NaCl

UNIT NUMBER 1 LOG NUMBER 653 TIME: 13: 0:22 DATE: 10/15/84  
STEP INCREMENT= .050 TIME/STEP(SEC)= 1.500 NPTS= 1201  
LIME + 30 % M NAN03

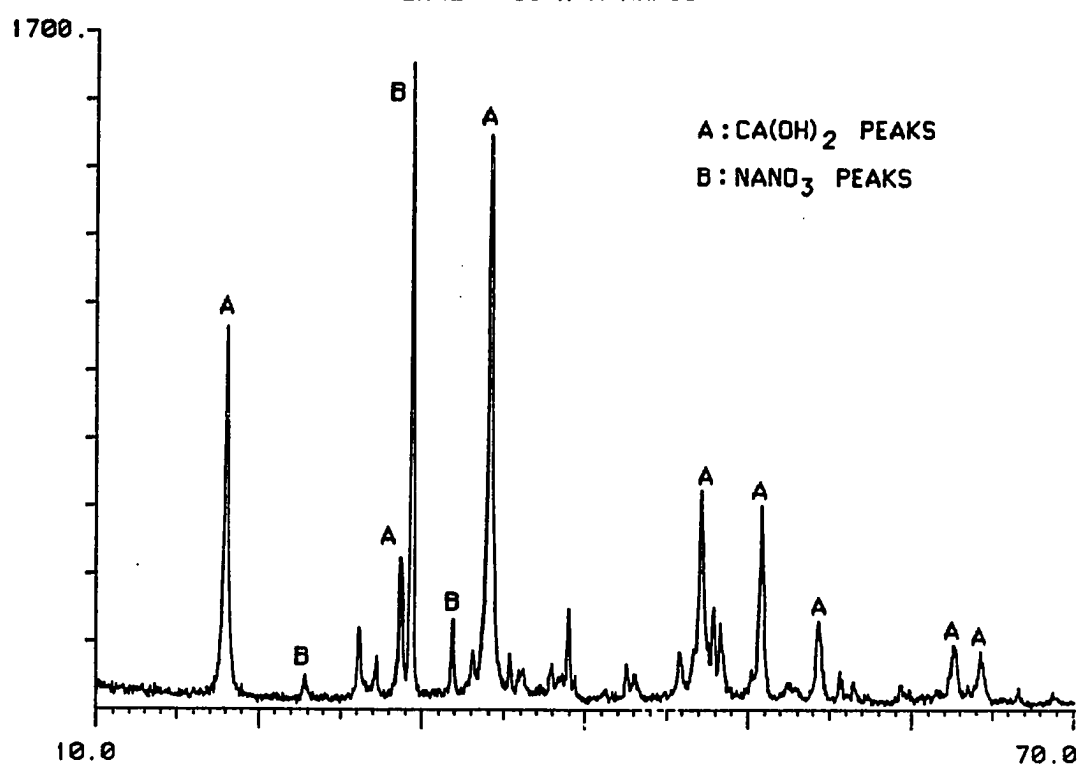


Figure A-17: X-ray Diffraction Pattern: Ca(OH)<sub>2</sub> with  
30 mole% NaNO<sub>3</sub>

UNIT NUMBER 1 LOG NUMBER 655 TIME: 14:55: 4 DATE: 10/15/84  
STEP INCREMENT= .050 TIME/STEP(SEC)= 1.500 NPTS= 1201

LIME + 30 % M LICL

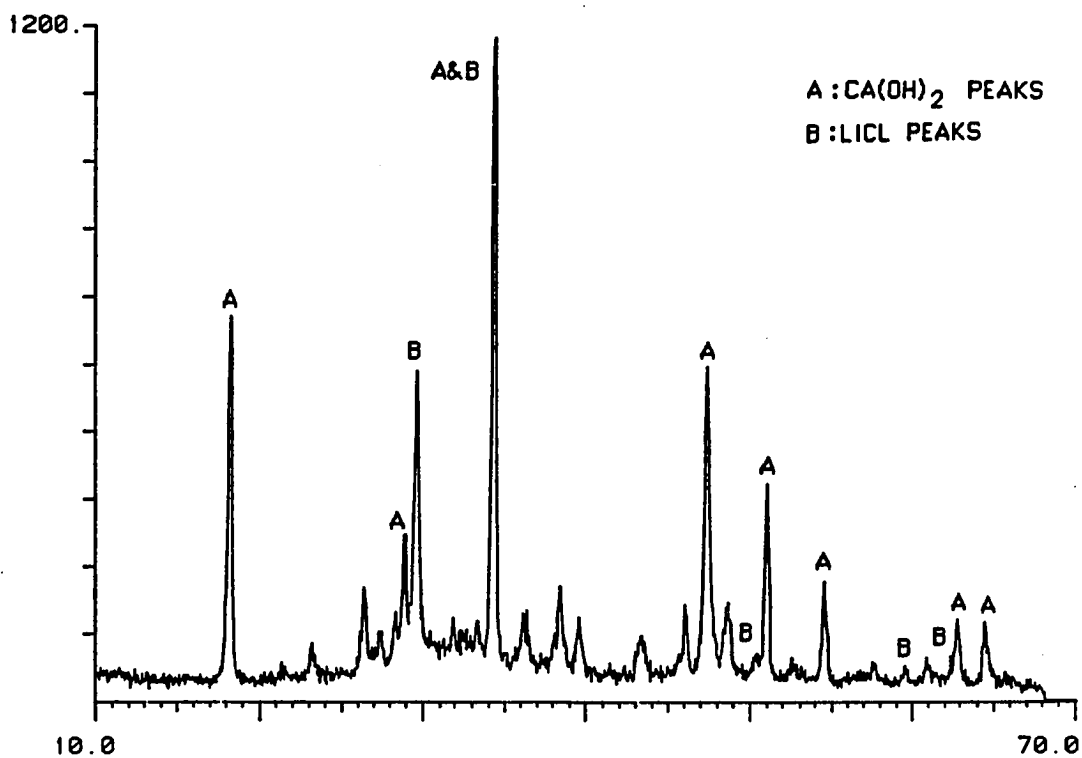


Figure A-18: X-ray Diffraction Pattern: Ca(OH)<sub>2</sub> with  
30 mole% LiCl

UNIT NUMBER 1 LOG NUMBER 607 TIME: 22:19:39 DATE: 9/20/84  
STEP INCREMENT= .050 TIME/STEP(SEC)= 1.500 NPTS= 1001  
LIME A + 10% M KCL

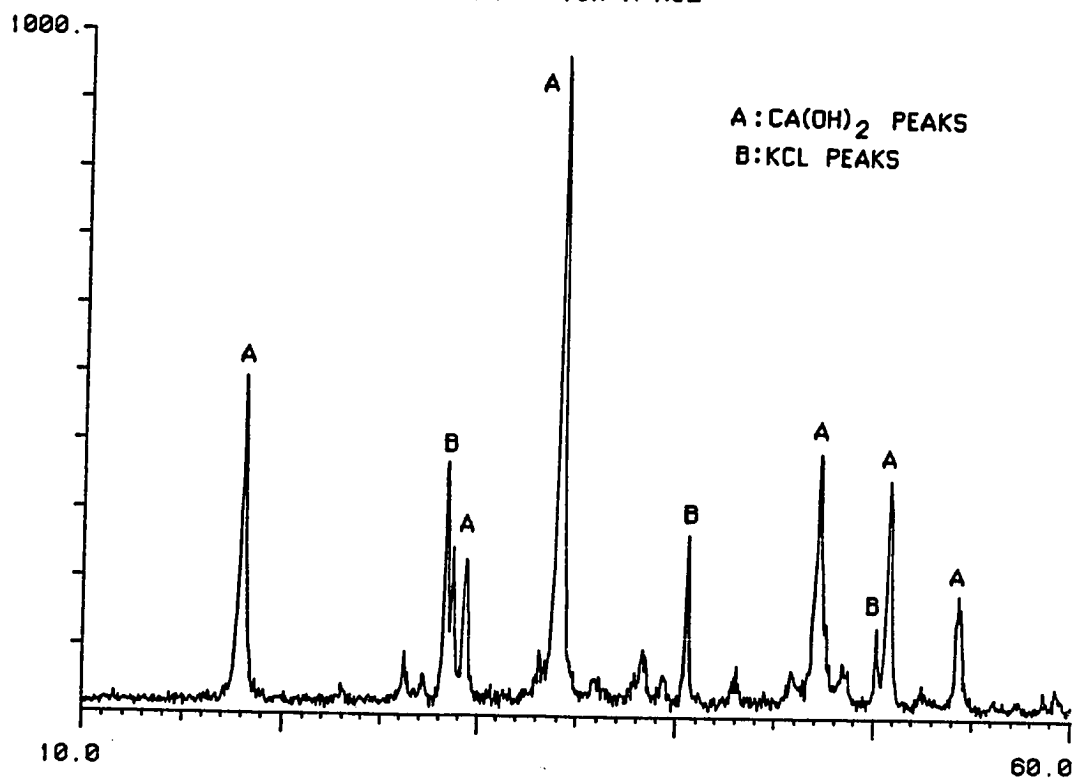


Figure A-19: X-ray Diffraction Pattern:  $\text{Ca(OH)}_2$  with  
10 mole% KCl

UNIT NUMBER 1 LOG NUMBER 664 TIME: 13:46: 6 DATE: 10/17/84  
STEP INCREMENT= .050 TIME/STEP(SEC)= 1.500 NPTS= 1201  
LIME + 20 % BA<sub>2</sub>CL<sub>2</sub>.2H<sub>2</sub>O

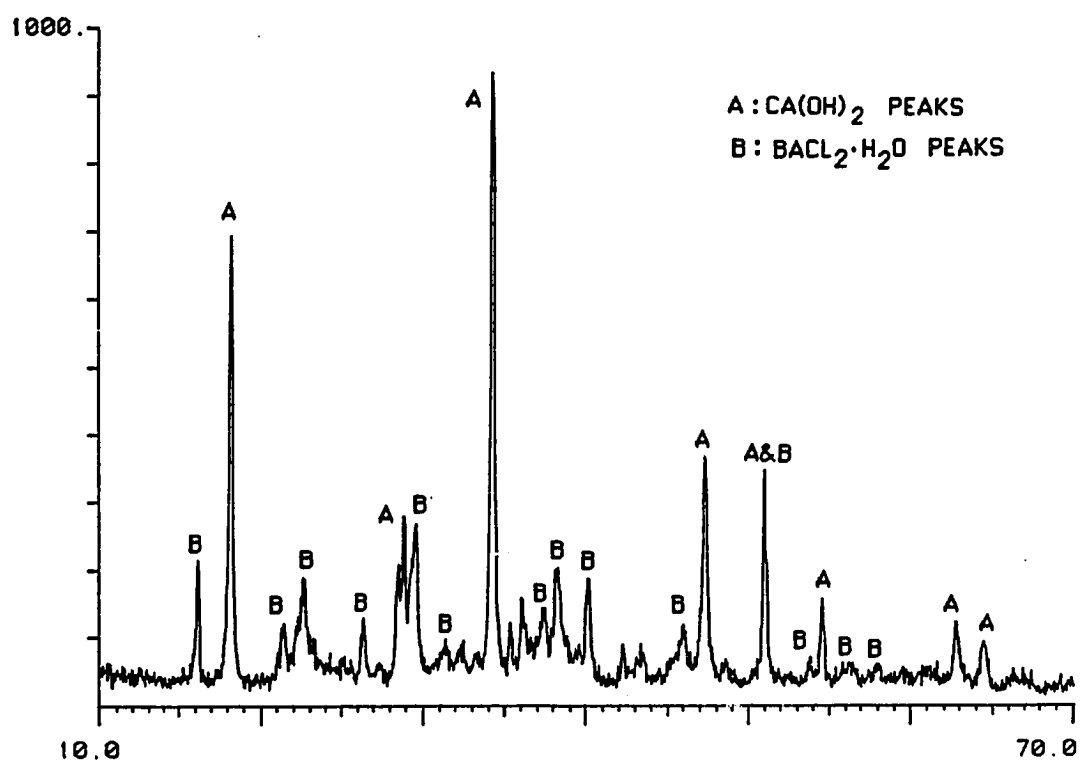


Figure A-20: X-ray Diffraction Pattern: Ca(OH)<sub>2</sub> with  
20 mole% BaCl<sub>2</sub>·2H<sub>2</sub>O

UNIT NUMBER 1 LOG NUMBER 646 TIME: 14:58:10 DATE: 10/11/84  
STEP INCREMENT= .050 TIME/STEP(SEC)= 1.500 NPTS= 1201  
LIME + 10 % M NABR

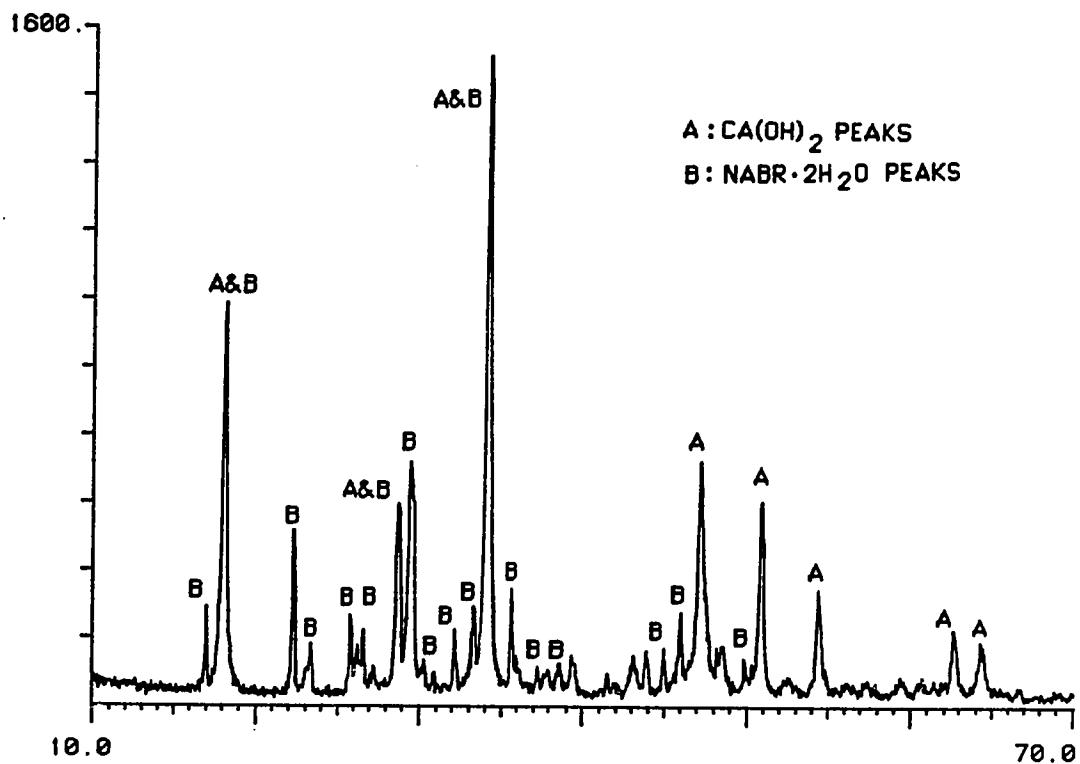
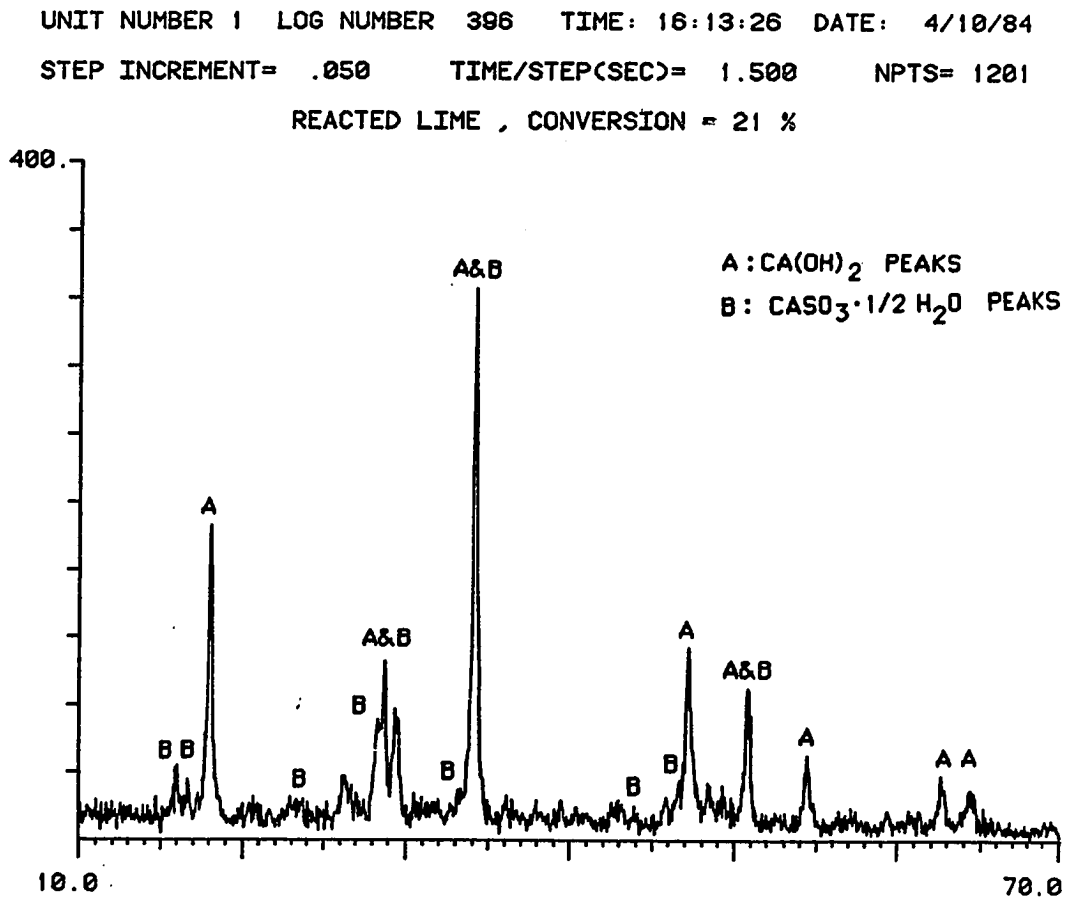
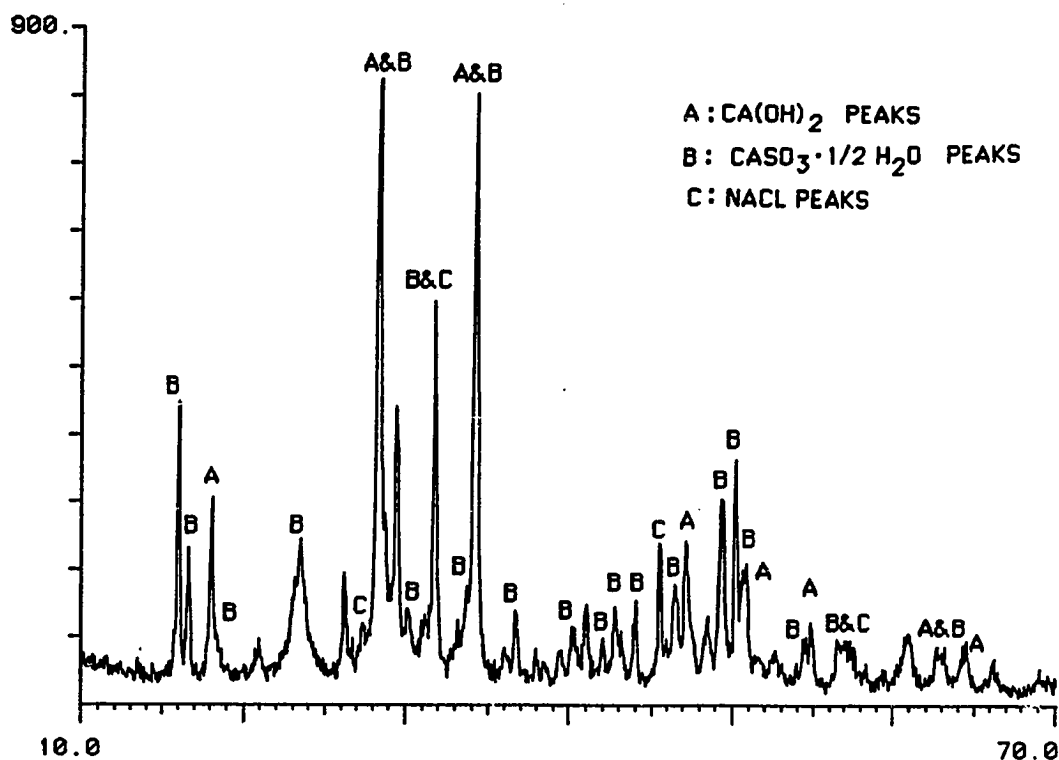


Figure A-21: X-ray Diffraction Pattern:  $\text{Ca(OH)}_2$  with  
10 mole% NaBr



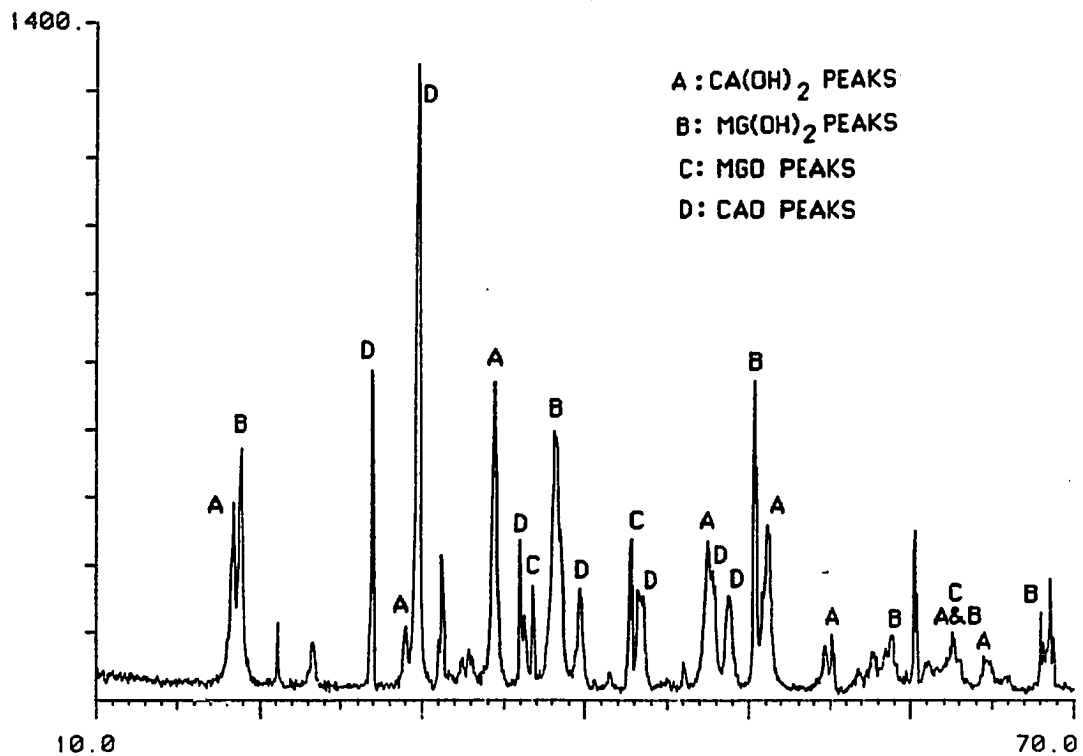
**Figure A-22:** X-ray Diffraction Pattern: Reacted Ca(OH)<sub>2</sub>, 21%  
Conversion, 500 ppm SO<sub>2</sub>, 74% R H, 64.4°C,  
1 hr reaction

UNIT NUMBER 1 LOG NUMBER 647 TIME: 15:54:18 DATE: 10/11/84  
 STEP INCREMENT= .050 TIME/STEP(SEC)= 1.500 NPTS= 1201  
 LIME + 10 % M NA CL CONVERTED 46 %



**Figure A-23:** X-ray Diffraction Pattern: Reacted  $\text{Ca(OH)}_2$  with 10 mole% NaCl, 74% R H, 64.4°C, 500 ppm  $\text{SO}_2$ , 2 hr Reaction, 46% Conversion

UNIT NUMBER 1 LOG NUMBER 625 TIME: 15:19:15 DATE: 10/ 1/84  
STEP INCREMENT= .050 TIME/STEP(SEC)= 1.500 NPTS= 1201  
SIEVED BALL MILL DOLOMITIC LIME



**Figure A-24:** X-ray Diffraction Pattern: Pressure Hydrated Dolomitic Lime

**Table A-4: X-Ray Powder Diffraction Results**

Additive	Solid Phase Detected Besides $\text{Ca(OH)}_2$
NaCl	NaCl
$\text{NaNO}_3$	$\text{NaNO}_3$
$\text{CaCl}_2 \cdot 2\text{H}_2\text{O}$	$\text{CaCl}_2 \cdot \text{Ca(OH)}_2 \cdot \text{H}_2\text{O}$
LiCl	LiCl
KCl	KCl
$\text{BaCl}_2 \cdot 2\text{H}_2\text{O}$	$\text{BaCl}_2 \cdot \text{H}_2\text{O}$
NaBr	$\text{NaBr} \cdot 2\text{H}_2\text{O}$

---

Reacted $\text{Ca(OH)}_2$	$\text{CaSO}_3 \cdot 1/2\text{H}_2\text{O}$
Pressure Hydrated Dolomitic Lime	$\text{Mg(OH)}_2$ , MgO

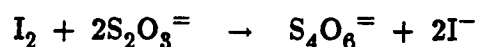
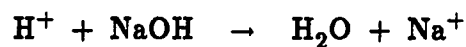
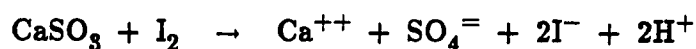
pattern of reacted solids. No gypsum or any other sulfate phase was detected, further supporting the hypothesis that any sulfate produced in the reactor will be present in solid solution with the  $\text{CaSO}_3 \cdot 1/2\text{H}_2\text{O}$ . As has been reported in the literature (Setoyama and Takahashi, 1978, Jones et al., 1976) the x-ray diffraction pattern of the solid solution is indistinguishable from the patterns of the pure  $\text{CaSO}_3 \cdot 1/2\text{H}_2\text{O}$ .

The X-ray analysis of pressure hydrated dolomitic lime (Figure A-24) showed the presence of  $\text{Mg(OH)}_2$ ,  $\text{Ca(OH)}_2$ , CaO and MgO. This indicates that the sample was not completely hydrated.

### A.7 Acid/Base and Iodometric Titration

Acid/base and iodometric titration were used to analyze the reacted solids for sulfite and hydroxide. The analysis consisted of dissolving the solid sample in about 30 cc of distilled water, adding known excess of HCl and iodine solutions, and back-titrating with NaOH solution to pH 6, then with sodium thiosulfate solution to the starch end point.

The chemistry involved in the analysis is given by:



Because the reaction of iodine with sulfite produces  $\text{H}^+$  ions, the analyses of sulfite and hydroxide are interrelated.

Given:

$$a = \text{ml of } x \text{ N HCl}$$

$$b = \text{ml of } y \text{ N I}_2$$

$$c = \text{ml of } z \text{ N NaOH}$$

$$d = \text{ml of } w \text{ N Na}_2\text{S}_2\text{O}_3$$

The amount of  $\text{CaSO}_3$  and  $\text{Ca(OH)}_2$  are given by:

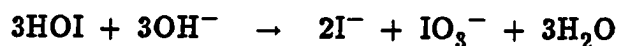
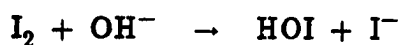
$$\text{gmol CaSO}_3 = \frac{by - dw}{2000}$$

$$\text{gmol Ca(OH)}_2 = \frac{ax + by - cz - dw}{2000}$$

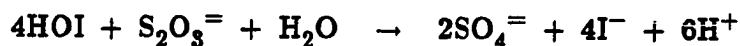
$$\text{lime conversion} = \frac{by - dw}{ax + 2by - cz - 2dw}$$

In calculating the lime conversion we are assuming that the product is sulfite. Any oxidation of sulfite to sulfate taking place in the reactor, will cause the apparent lime conversion given by chemical analysis to be lower than the actual value.

Some side reactions have been reported to occur at high pH (Dick, 1973). These side reactions are:



The hydrolysis of the iodine becomes significant at a pH of about 8, with the reaction of thiosulfate and byperiodite being:



This reaction would produce a departure from the expected stoichiometry for the iodine-thiosulfate reaction. Because during the analysis the pH was lower or equal to 6, these side reactions are not likely to represent a problem.

There is another reaction that occurs at low pH, that could be important in the analysis. This reaction is the oxidation of iodide by air.



In order to minimize the amount of iodine consumed by this reaction, the analysis time was kept as short as possible. When tested with known mixtures of  $\text{CaSO}_3$  and  $\text{Ca}(\text{OH})_2$ , the chemical analysis was able to predict the amounts of sulfite and hydroxide with less than 2% error. This indicates that oxidation of iodide by air is not occurring in any appreciable degree during the analysis.

**Appendix B.**  
**Experimental Data**

Table B-1: Experimental Data Lime 0

4.6 l/min N<sub>2</sub>, 66°C, Lime 0  
Percentage of Ca(OH)<sub>2</sub> Converted

(\*) Experimental runs modelled

Exp #	Inlet SO <sub>2</sub> (ppm)	RH (%)	Amount lime (g)	Time (Minutes)											
				5	10	15	20	25	30	35	40	45	50	55	60
27*	1500	70	4.0	2.9	5.6	8.2	10.5	12.7	14.7	16.6	18.4	20.1	21.7	23.2	24.5
31	1650	70	4.0	3.2	6.3	8.8	11.1	13.1	15.0	16.8	18.4	19.9	21.3	22.6	23.8
28*	1060	70	4.0	2.1	4.2	6.3	8.3	10.4	12.5	14.6	16.6	18.6	20.4	22.0	23.4
30	1150	70	4.0	2.3	4.5	6.8	9.1	11.3	13.5	15.5	17.5	19.3	21.0	22.6	24.2
34*	2150	70	4.0	4.0	7.2	9.9	12.2	14.2	16.1	17.9	19.5	21.0	22.4	23.7	24.8
44	2050	50	4.0	3.7	6.5	8.6	10.3	11.5	12.6	13.5	14.1	14.7	15.2	15.6	15.9
46*	2050	50	4.0	4.0	7.2	9.9	12.0	13.7	15.1	16.2	17.0	17.7	18.2	18.6	18.8
47	2040	50	4.0	4.0	7.8	10.5	12.3	13.5	14.3	14.8	15.2	15.5	15.8	16.1	16.3
37*	2000	19	4.0	2.8	4.1	4.8	5.3	5.6	5.8	5.9	5.9	5.9	5.9	5.9	5.9
48*	2100	50	2.0	6.3	9.8	12.1	13.8	14.9	15.6	16.2	16.7	17.1	17.4	17.8	18.1
40	2070	50	2.0	6.3	10.2	12.7	14.4	15.6	16.5	17.3	18.1	18.7	19.3	19.9	20.4
45	1980	50	2.0	6.4	11.1	13.7	15.3	16.4	17.2	17.9	18.5	19.0	19.5	19.9	20.2
43*	2000	50	1.0	8.7	11.8	14.6	16.4	17.5	18.5	19.4	20.2	20.9	21.5	22.1	22.6
50*	2000	50	1.0	8.7	11.4	13.1	14.2	15.2	16.1	16.9	17.7	18.4	19.2	19.8	20.5
56*	1000	50	1.0	6.6	9.3	11.4	12.7	13.5	14.1	14.5	14.9	15.2	15.5	15.7	16.0
53*	940	50	2.0	3.7	7.2	9.7	11.2	12.3	13.0	13.5	13.9	14.2	14.6	14.8	15.1
42*	4000	50	4.0	5.4	9.0	11.7	13.8	15.3	16.5	17.5	18.4	19.1	19.7	20.1	20.5
57	4000	50	4.0	6.7	10.3	12.8	14.6	15.8	16.7	17.3	17.7	18.1	18.5	18.7	19.0
58	4000	50	4.0	6.4	10.1	12.8	14.7	16.0	17.0	17.7	18.3	18.8	19.3	19.7	19.9
52*	1100	50	4.0	2.2	4.3	6.5	8.5	10.2	11.3	12.3	13.0	13.6	14.0	14.4	14.7

Table B-2: Experimental Data Lime A

4.6 l/min N<sub>2</sub>, 1 g lime A  
Percentage of Ca(OH)<sub>2</sub> Converted

Exp #	SO <sub>2</sub> (ppm)	RH (%)	Temp (°C)	Time (Minutes)											Chemical Analysis	
				5	10	15	20	25	30	35	40	45	50	55		60
63	490	78	66	4.0	7.6	10.8	13.5	15.9	18.0	20.0	21.8	23.4	24.9	26.2	27.3	-
64	530	78	55.3	4.2	8.0	11.1	13.6	15.8	17.7	19.5	21.0	22.4	23.6	24.7	25.7	-
77*	510	74	64.4	4.0	7.8	10.9	13.5	15.6	17.4	18.9	20.1	21.8	22.5	23.2	21.2	-
96	490	74	64.4	3.9	7.7	11.5	14.9	17.3	18.7	19.5	20.2	20.7	21.1	21.5	21.9	18.2
99	500	74	64.4	3.9	7.9	11.6	14.9	17.1	18.4	19.3	20.0	20.6	21.2	21.6	22.1	18.3
66	530	45	66	3.8	6.3	7.9	8.8	9.3	9.6	9.9	10.1	10.2	10.4	10.5	10.7	-
67	570	45	66	4.2	6.4	7.7	8.5	8.9	9.2	9.4	9.5	9.6	9.7	9.8	9.8	-
82*	500	74	30.4	3.7	6.9	9.5	11.6	13.4	14.8	15.9	16.8	17.6	18.2	18.9	19.5	16.3
83	560	74	30.5	4.1	7.4	10.1	12.2	13.8	15.2	16.2	17.1	17.8	18.5	19.1	19.7	19.3
84	500	74	30.4	3.6	6.8	9.5	11.6	13.3	14.8	15.9	16.8	17.6	18.3	19.0	19.6	18.8
136*	505	54	66	3.7	6.5	8.5	9.7	10.4	10.8	11.2	11.4	11.5	11.6	11.7	11.8	13.4

(\*) Experimental runs modelled

Table B-3: Experimental Data, Lime with Organic Additives

74% RH, 64.4°C, 4.6 l/min N<sub>2</sub>, 1 g lime A  
Percentage of Ca(OH)<sub>2</sub> Converted

Exp #	SO <sub>2</sub> (ppm)	Additive (Wt%)	Time (Minutes)												Chemical Analysis
			5	10	15	20	25	30	35	40	45	50	55	60	
101	500	1% AA + 7% CaCl <sub>2</sub>	3.8	7.3	10.3	12.8	15.0	16.8	18.3	19.6	20.9	22.0	22.9	23.8	20.5
108	515	1% AA + 7% CaCl <sub>2</sub>	4.1	8.1	11.8	15.2	18.1	20.3	21.7	22.8	23.6	24.3	24.9	25.4	27.3
109	515	1% AA + 7% CaCl <sub>2</sub>	4.1	8.1	11.7	14.8	17.2	18.7	19.7	20.5	21.0	21.6	22.0	22.4	23.7
112	490	1% AA + 7% CaCl <sub>2</sub>	3.8	7.4	10.4	13.2	15.6	17.6	19.1	20.2	21.1	21.7	22.1	22.5	21.4
110	505	1% AA	3.8	7.1	10.0	12.5	14.6	16.1	16.9	17.3	17.7	18.0	18.4	18.7	18.5
111	540	1% AA	4.3	8.6	12.1	14.8	16.8	18.3	19.3	20.0	20.6	21.1	21.5	21.9	22.5
116	500	5% GA	2.3	3.2	4.0	4.9	5.7	6.5	7.2	7.9	8.6	9.4	10.1	10.7	11.4
118	510	5% GA	2.6	3.7	4.8	5.8	6.8	7.7	8.5	9.3	10.0	10.7	11.3	11.9	13.0
114	490	5% TEG	3.6	6.9	9.9	12.4	14.1	15.4	16.4	17.2	17.7	18.2	18.6	18.9	18.6
115	480	5% TEG	3.7	7.4	10.8	13.6	15.7	17.3	18.5	19.4	20.2	20.9	21.5	22.1	21.3
117	504	5% EG	3.8	7.4	10.5	13.2	15.2	16.5	17.3	17.8	18.2	18.5	18.8	18.9	19.2
119	515	5% EG	4.1	8.1	11.8	15.0	17.5	19.0	19.9	20.5	20.9	21.2	21.4	21.6	21.1
121	500	5% MEA	4.1	8.3	12.0	14.9	16.7	17.7	18.3	18.8	19.2	19.5	19.8	20.0	20.9
122	490	5% MEA	4.2	7.8	10.6	13.0	15.0	16.3	17.2	17.8	18.3	18.6	19.0	19.2	19.8

AA = Adipic Acid GA = Glycolic Acid EG = Ethylene Glycol

TEG = Tri-Ethylene Glycol MEA = Monoethanolamine

**Table B-4: Experimental Data of Lime with Salts Additives at 74% RH**

74% RH, 64.4°C, 4.6 l/min N<sub>2</sub>, 1 g lime A

Percentage of Ca(OH)<sub>2</sub> Converted

Exp #	SO <sub>2</sub> (ppm)	Additive (Mole%)	Time (Minutes)												Chemical Analysis
			5	10	15	20	25	30	35	40	45	50	55	60	
97	510	7% CaCl <sub>2</sub>	4.0	8.0	12.0	16.1	19.9	23.6	26.4	29.0	30.8	32.0	32.8	33.6	27.8
98	515	7% CaCl <sub>2</sub>	4.1	8.1	12.2	16.0	19.6	23.1	26.2	29.0	31.4	33.6	35.4	37.0	28.7
100	500	7% CaCl <sub>2</sub>	3.9	7.9	11.8	15.6	19.0	22.1	24.9	27.4	29.4	31.1	32.4	33.6	27.1
127	510	10% NaOH	3.8	7.6	11.5	15.3	19.1	22.8	26.3	29.6	34.5	35.0	37.1	38.8	35.0
128	510	5% Na <sub>2</sub> SO <sub>3</sub>	3.9	7.5	10.8	14.0	16.9	19.4	21.7	23.8	25.6	27.2	28.6	29.8	30.8
129	507	5% Na <sub>2</sub> SO <sub>4</sub>	4.0	8.0	11.8	15.1	18.0	20.3	22.3	24.0	25.4	26.4	27.4	28.3	26.6
130	520	10% NaCl	4.1	8.2	12.3	16.2	19.9	23.4	26.7	29.7	32.4	34.8	36.8	38.5	39.0
131	510	10% NaNO <sub>3</sub>	4.0	8.0	12.0	16.1	19.9	23.7	27.5	30.9	34.1	37.0	39.5	41.5	40.7
132	510	10% NaNO <sub>2</sub>	4.0	8.0	12.0	15.7	19.2	22.6	25.9	29.0	32.0	34.8	37.5	40.0	31.5
133	502	5% Ca(NO <sub>3</sub> ) <sub>2</sub>	4.0	7.9	11.9	15.8	19.7	23.7	27.6	31.1	34.1	36.4	38.1	39.4	40.1

Table B-5: Experimental Data of Lime with Salts Additives at 54% RH

54% RH, 66°C, 4.6 l/min N<sub>2</sub>, 1 g lime A

Percentage of Ca(OH)<sub>2</sub> Converted

Exp #	SO <sub>2</sub> Additive (ppm)	Additive (Mole%)	Time (Minutes)												Chemical Analysis	
			5	10	15	20	25	30	35	40	45	50	55	60		
136	505	None	3.7	6.5	8.5	9.7	10.4	10.8	11.2	11.4	11.5	11.6	11.7	11.8	13.4	
135	500	5% Ca(NO <sub>3</sub> ) <sub>2</sub>	3.7	7.2	9.9	11.3	11.8	12.1	12.4	12.6	12.7	12.8	13.0	13.1	-	
137	520	5% Ca(NO <sub>3</sub> ) <sub>2</sub>	3.7	6.6	8.7	9.8	10.4	10.7	11.0	11.1	11.3	11.4	11.5	11.5	11.2	
134	520	10% NaNO <sub>3</sub>	4.1	8.2	12.2	15.9	19.1	21.9	24.1	25.9	27.2	28.2	28.8	29.3	29.6	
138	530	10% NaNO <sub>3</sub>	4.1	8.1	11.6	14.5	17.1	19.2	21.0	22.4	23.5	24.2	24.7	25.1	23.5	
139	510	10% NaOH	3.9	7.5	10.5	12.9	14.6	15.6	16.2	16.5	16.8	17.0	17.2	17.3	-	
140	500	10% NaCl	3.9	7.9	11.8	15.6	19.1	21.9	24.1	25.7	26.8	27.5	28.0	28.4	21.5	
140B	500	10% NaCl	3.9	7.8	11.4	14.8	17.5	19.8	21.6	23.0	23.9	24.6	25.2	25.7	17.8	
141	500	5% Na <sub>2</sub> SO <sub>3</sub>	3.9	7.5	10.8	13.0	14.1	14.7	15.1	15.3	15.6	15.8	15.9	16.1	17.8	
142	505	5% Na <sub>2</sub> S <sub>2</sub> O <sub>3</sub>	4.0	8.0	11.5	14.2	16.1	17.7	18.9	19.8	20.5	21.0	21.3	21.6	-	
143	500	3% NaNO <sub>3</sub>	3.9	7.7	11.0	13.3	14.9	16.0	16.6	17.0	17.3	17.6	17.8	18.0	16.6	
145	500	1% NaNO <sub>3</sub>	4.0	7.4	9.8	11.2	11.9	12.4	12.8	13.0	13.2	13.3	13.4	13.5	16.7	
148	512	15% NaNO <sub>3</sub>	4.0	8.1	11.9	15.4	18.3	20.6	22.3	23.5	24.3	25.0	25.6	26.1	24.8	
149	500	1% NaCl	3.5	6.3	8.7	10.7	12.4	13.8	14.6	15.1	15.3	15.7	15.9	16.0	14.0	

Table B-5: Continuation  
Percentage of  $\text{Ca}(\text{OH})_2$  Converted

Exp #	$\text{SO}_2$ Additive (ppm)	Additive (Mole%)	Time (Minutes)												Chemical Analysis
			5	10	15	20	25	30	35	40	45	50	55	60	
162	515	10% NaCl**	4.1	8.1	12.1	15.8	18.8	21.2	23.1	24.5	25.6	26.3	26.8	27.1	25.1
150	500	3% NaCl	3.9	7.3	10.3	12.5	14.1	15.3	16.2	16.8	17.3	17.7	18.0	18.1	18.1
155B	520	15% NaCl	4.1	8.2	12.2	15.9	19.0	21.3	23.1	24.2	25.1	25.8	26.3	26.7	-
155	518	10% NaCl*	4.1	8.1	11.7	14.7	17.2	19.1	20.5	21.5	22.1	22.6	22.9	23.2	22.7
157	490	10% $\text{NaNO}_3$ *	3.9	7.7	11.4	14.6	17.2	19.0	20.3	21.2	21.9	22.6	23.1	23.7	22.6
185	507	10% KCl*	3.9	7.5	10.7	13.1	14.7	15.7	16.6	17.3	17.9	18.4	18.9	19.3	20.4
176	515	5% BaCl	3.9	7.4	10.3	12.6	14.5	16.0	17.1	17.8	18.3	18.7	19.1	19.4	14.4
177	508	5% $\text{Co}(\text{NO}_3)_2$	3.8	7.1	9.4	10.7	11.6	12.1	12.4	12.6	12.8	12.9	13.1	13.2	12.6
178	507	10% NaBr	4.0	8.0	12.0	16.0	19.8	23.5	27.1	30.4	33.6	36.5	39.3	42.0	44.2
179	535	10% KCl	4.2	8.4	12.6	16.6	20.3	23.5	26.4	28.9	30.9	32.5	33.9	35.0	35.8
175	510	10% KCl	4.0	8.0	12.0	16.0	19.9	23.7	27.5	31.1	34.1	36.4	38.3	39.7	41.9
180	510	10% LiCl	4.0	8.0	12.0	16.1	20.1	24.1	27.9	31.5	34.8	37.8	40.7	42.9	47.2
183	600	5% $\text{CaCl}_2$	4.6	8.8	11.7	13.1	13.9	14.4	14.9	15.3	15.8	16.2	16.6	17.0	14.6
191	330	3% NaCl	2.6	5.0	7.4	9.5	11.2	12.6	13.6	14.4	15.0	15.5	15.9	16.2	20.3

(\*) No Prehumidification of the bed at 98% RH

(\*\*)  $\text{O}_2$  free  $\text{N}_2$

**Table B-6: Experimental Data of Lime with Salts Additives at 17 and 35% RH**  
 4.6 l/min N<sub>2</sub>, 1 g lime A, 10 mole% Additive

Exp #	SO <sub>2</sub> Additive (ppm)	Temperature (°C)	Percentage of Ca(OH) <sub>2</sub> Converted													Chemical Analysis	
			5	10	15	20	25	30	35	40	45	50	55	60			
34.6% RH, 77.5°C																	
151	490 NaCl		3.9	7.6	10.6	12.4	13.6	14.4	15.3	15.9	16.4	16.7	17.0	17.3	17.3	15.9	
144	520 NaNO <sub>3</sub>		4.1	7.9	10.6	12.0	12.8	13.4	13.8	14.2	14.5	14.7	14.9	15.1	16.5		
17.4% RH, 95°C																	
152	510 NaCl		3.7	6.2	7.0	7.6	8.1	8.4	8.7	9.0	9.2	9.4	9.6	9.8	9.7		
146	512 NaNO <sub>3</sub>		3.6	5.6	6.6	7.2	7.6	7.9	8.2	8.4	8.6	8.8	8.9	8.9	11.9		
147	512 None		2.2	2.5	2.7	2.9	3.1	3.2	3.3	3.4	3.4	3.4	3.4	3.4	4.0		
184	508 NaBr		3.6	5.5	6.7	7.6	8.3	8.9	9.4	9.9	10.3	10.7	11.1	11.3	11.0		
186	500 LiCl		3.7	6.0	6.8	7.3	7.7	8.1	8.4	8.7	8.9	9.2	9.4	9.6	9.1		
182	500 KCl		-	-	-	-	-	-	-	-	-	-	-	-	3.4	2.9	
187	510 NaCl*		-	-	-	-	-	-	-	-	-	-	-	-	3.3	4.0	

(\*) No prehumidification of bed at 98% RH

**Table B-7: Experimental Data, Pressure Hydrated Dolomitic Lime**

74% RH, 64.4°C, 4.6 l/min N<sub>2</sub>, 1 g lime

Percentage of Lime Converted Assuming 40% Mg(OH)<sub>2</sub>

Exp #	SO <sub>2</sub> (ppm)	Type Lime	Time (Minutes)												Chemical Analysis
			5	10	15	20	25	30	35	40	45	50	55	60	
166	530	Ball Mill	3.8	7.6	11.3	14.4	16.8	18.6	19.9	21.1	22.1	23.1	23.9	24.6	22.3
167	510	Hydrator	3.7	7.3	11.0	14.3	16.2	17.6	18.8	20.1	21.1	22.1	23.0	24.2	21.6
171	510	Ball Mill (Sieved)	3.3	6.7	10.0	13.2	16.3	19.2	21.9	24.3	26.4	28.2	29.8	31.2	-
172	510	Ball Mill + 10% NaCl	3.5	7.0	10.4	14.0	17.4	20.9	24.3	27.7	30.9	34.0	36.8	39.3	-

**Table B-8: Differential Experiments**0.125 g lime A, 500 ppm SO<sub>2</sub>, 4.6 l/min N<sub>2</sub>

Additive (Mole%)	RH (%)	Temp (°C)	Time (Minutes)	Conversion (%)
None	54	66	10	8.4
			30	14.1
			30	10.4
			60	17.6
None	74	64.4	10	16.6
			30	19.1
			60	24.3
			60	21.2
			60	23.9
			60	22.7
10% NaCl	54	66	10	27.3
			30	25.6
			60	28.1
5% CaCl <sub>2</sub>	74	64.4	10	26.8
			10	27.5
			10	28.2
			30	28.6
			30	34.9
			30	33.6
			60	38.6
			60	37.0

**Appendix C.**  
**Model Computer Program**

```

PROGRAM REAREO(INPUT,OUTPUT,TTY,TAPE1=INPUT,TAPE2=OUTPUT,
&TAPE3=TTY)
C *****
C THIS IS A PROGRAM TO INTEGRATE THE REACTION OF SO2 WITH
C CA(OH)2 ALONG THE REACTOR AND IN TIME.THE PROGRAM
C ASSUMES A ZERO ORDER KINETICS IN SO2.
C THIS PROGRAM USES DGEAR TO INTEGRATE IN TIME AND IN
C DISTANCE AND IT USES VARIABLE STEP SIZE.
C THE SURFACE AREA IS ALLOWED TO DECREASE WHEN THE
C REACTION OCCURS. THE SURFACE AREA DECREASE
C FOLLOWS THE EQUATION:
C
C AREA F = (1.0 + EXP(13.428*XLIME-10.7424))/15.667
C
C THIS EQUATION ASSUMES THAT THE ROUGHNESS IS 15.667 WHEN ALL
C THE LIME IS UNREACTED AND THAT IS 2.0 WHEN 20 % OF THE
C LIME HAS BEEN CONVERTED.
C *****

INTEGER NZ,IC,NZN,ICN,IPRINT
REAL K1,K2,K3,CAG,VXLIME,VXSO2,VMC,X(3)
REAL VZ,C,H,VZN(200),VXLN(200),NB,SO2EXP(12)
COMMON /CONST1/ K1,K2,K3,CAG
COMMON /CONST2/ VMC
COMMON /CONST3/ H
COMMON /CONST4/ NB
COMMON /CONST5/ NZ,VZ(200),VXLIME(200)
COMMON /CONST6/ C(200,3),IC
COMMON /CONST7/ VXSO2(200)
COMMON /CONST8/ IPRINT,XAVERA(12),CONC(12),TIME(12)
COMMON /CONST9/ XLEXP(12),XDEV(12)
READ(1,*) NUMEXP
READ(1,*) DE,DKS,DKC
READ(1,*) CAG,VMC,NB,TREAC
DO 17 I=1,12
READ(1,*) SO2EXP(I),XLEXP(I)
17 CONTINUE
VMC=VMC*((273.25+TREAC)/273.15)
K1=9.4E4*NB*DE/(3.958156*2.273E-4)
K2=9.4E4*NB*2.2*DKS/74.1
K3=DKC*NB*9.4E4
NB=NB/74.1
CAG=CAG*0.000001/(82.06*(273.15+TREAC))
X(1)=K1
X(2)=K2
X(3)=K3
CALL FUNCT(X,F)
WRITE(2,900) NUMEXP
WRITE(3,900) NUMEXP
900 FORMAT('          EXPERIMENT NUMBER =',I4)

```

```

WRITE(2,910) DE,DKS,DKC
WRITE(3,910) DE,DKS,DKC
WRITE(2,909) K1,K2
WRITE(3,909) K1,K2
909 FORMAT('          K1 =',E12.7,/,',          K2 =',
&E12.7)
910 FORMAT('          DE =',E12.7,/,',          KS =',E12.7
&,/,',          KC =',E12.7)
STDEV=(F/11.0)**0.5
WRITE(2,920) F
WRITE(3,920) F
920 FORMAT('          SUM OF SQUARE ERRORS =',E12.7)
WRITE(2,923) STDEV
WRITE(3,923) STDEV
923 FORMAT('          STANDARD DEVIATION =',F5.2,/)
WRITE(2,*)'          TIME(I)  SO2EXP(I)  CONC(I)  XLEXP(I)  XAVE
&RA(I)  XDEV(%)'
WRITE(3,*)'          TIME(I)  SO2EXP(I)  CONC(I)  XLEXP(I)  XAVE
&RA(I)  XDEV(%)'
DO 500 I=1,IPRINT
XDEV(I)=100.0*(XAVERA(I)-XLEXP(I))/XLEXP(I)
WRITE(2,930) TIME(I),SO2EXP(I),CONC(I),XLEXP(I),XAVERA(I),XDEV(I)
WRITE(3,930) TIME(I),SO2EXP(I),CONC(I),XLEXP(I),XAVERA(I),XDEV(I)
500 CONTINUE
930 FORMAT(8X,G10.5,4(1X,G10.5),F7.2)
STOP
END

```

## SUBROUTINE FUNCT(X,F)

```

*****
THIS SUBROUTINE DOES THE ACTUAL INTEGRATION, THE MAIN
PROGRAM ONLY READ DATA AND PRINT THE RESULTS
*****
DIMENSION VZN(200),VXLN(200),X(5)
INTEGER NZ,IC,NZN,ICN,IER,IPRINT
REAL K1,K2,K3,CAG,VXLIME,VXSO2,VMC
REAL VZ,C,HZ,VZN,VXLN,NB,X,XAVERA,CONC,T,TINI,TEND
REAL TDEL,TPRINT,DELTT
COMMON /CONST1/ K1,K2,K3,CAG
COMMON /CONST2/ VMC
COMMON /CONST3/ H
COMMON /CONST4/ NB
COMMON /CONST5/ NZ,VZ(200),VXLIME(200)
COMMON /CONST6/ C(200,3),IC
COMMON /CONST7/ VXSO2(200)
COMMON /CONST8/ IPRINT,XAVERA(12),CONC(12),TIME(12)
COMMON /CONST9/ XLEXP(12),XDEV(12)
K1=X(1)
K2=X(2)
K3=X(3)
C SET INITIAL VALUES OF NZ,VZ(I),VXLIME(I)
NZ=11
IC=NZ-1
DO 10 I=1,NZ
VZ(I)=0.1*FLOAT(I-1)
VXLIME(I)=1.0
10 CONTINUE
C SET VALUE OF TPRINT AND INITIAL VALUES FOR T,DELTT,IPRINT
T=0.0
TDEL=5.0
TINI=T
TEND=TDEL
DELTT=(TEND-TINI)/100.0
IPRINT=1
TPRINT=300.0
TMAX=3600.0
C NOW THE INTEGRATION IN THE Z DIRECTION WILL BE PERFORMED
DO 100 J=1,2000
WRITE(3,2) J
2 FORMAT(I4)
CALL INTEGZ(VXSO2,VXLN,VZN,NZN,ICN)
NZ=NZN
IC=ICN
DO 20 I=1,NZ
VZ(I)=VZN(I)
VXLIME(I)=VXLN(I)
20 CONTINUE
C NOW THE INTEGRATION IN TIME WILL BE PERFORMED

```

```

85  CALL INTEG(TINI,TEND,VXLN,DELTT,INDEX,IER)
    WRITE(2,*)'      T      TINI      TEND      DELTT' ;
    WRITE(2,87) T,TINI,TEND,DELTT
    WRITE(3,87) T,TINI,TEND,DELTT
87  FORMAT (3(1X,F10.3),E12.5)
    IF (TEND.EQ.TPRINT) GO TO 32
    CALL STPCHG(T,TEND,DELTT,INDEX,TPRINT)
32  IF (INDEX.EQ.1) THEN
    DO 30 I=1,NZ
    VXLN(I)=VXLIME(I)
30  CONTINUE
    TINI=T
    TDEL=TEND
    DELTT=DELTT*0.1
    GO TO 85
ELSE
    DO 35 I=1,NZ
    VXLIME(I)=VXLN(I)
35  CONTINUE
    IF (ABS(TEND-TPRINT).LE.1.0E-6) THEN
    WRITE(2,800) NZ
800  FORMAT('      NZ =',I4)
    WRITE(2,*)'      # Z POINTS      VZ(I)      VXSO2(I)      VXLIME(I)
&      VXLN(I)'
    DO 500 IZ=1,NZ
    WRITE(2,550) IZ,VZ(IZ),VXSO2(IZ),VXLIME(IZ),VXLN(IZ)
550  FORMAT(4X,I10,4(1X,G12.5))
500  CONTINUE
    TIME(IPRINT)=TEND
    CONC(IPRINT)=1.0-VXSO2(NZ)
    XAVERA(IPRINT)=0.0
    DO 65 I=1,NZ-1
    XAVERA(IPRINT)=XAVERA(IPRINT)+(VZ(I+1)-VZ(I))*
&      (VXLIME(I)+VXLIME(I+1))/2.0
65  CONTINUE
    XAVERA(IPRINT)=(1.0-XAVERA(IPRINT))*100.0
    IF (ABS(TEND-TMAX).LE.1.0E-6) THEN
C    CALCULATION OF SUM OF SQUARE ERRORS
    F=0.0
    DO 95 I=1,IPRINT
    F=F+(XAVERA(I)-XLEXP(I))*(XAVERA(I)-XLEXP(I))
95  CONTINUE
    RETURN
    ENDIF
    IPRINT=IPRINT+1
    TPRINT=TPRINT+300.0
    ENDIF
    TINCRE=TEND-T
    IF (TINCRE.LT.DELTT) TINCRE=DELTT*2.2
    T=TEND

```

```
TINI=T
TDEL=T+TINCRE
TEND=TDEL
IF(TEND.GE.TPRINT) THEN
  TEND=TPRINT
  TDEL=TPRINT
ENDIF
ENDIF
100 CONTINUE
WRITE(3,*) 'INSUFFICIENT ITERATIONS IN TIME'
RETURN
END
```

```

SUBROUTINE INTEGZ(VXSO2,VXLN,VZN,NZN,ICN)
C *****
C THIS SUBROUTINE USE DGEAR TO INTEGRATE THE FRACTION OF
C SO2 REMAINING IN THE REACTOR AT ANY GRID POINT ALONG
C THE REACTOR VXSO2(I), IT ALSO PROVIDES VALUES FOR THE
C LIME FRACTION INTERPOLATED AT THE NEW GRID POINTS,
C VXLN(I).
C VARIABLES ENTERING THE SUBROUTINE THROUGH COMMON
C BLOCKS ARE:
C
C NZ = NUMBER OF GRID POINTS IN THE Z DIRECTION
C VXLIME(I) = FRACTION OF LIME UNCONVERTED AT ALL GRID
C POINTS
C K1 = CONSTANT FOR THE DIFFUSION OF SO2 THROUGH THE ASH
C LAYER
C K2 = CONSTANT FOR CHEMICAL REACTION
C K3 = CONSTANT FOR DIFFUSION THROUGH THE GAS FILM
C CAG = SO2 CONCENTRATION ENTERING THE REACTOR
C VMC = N2 FLOW RATE (CC/SEC) AT THE REACTOR TEMPERATURE
C THE FOLLOWING VARIABLES ARE USED INSIDE THE SUBROUTINE:
C
C HZ = STEP SIZE IN THE Z DIRECTION
C H = STEP SIZE FOR DGEAR
C N = NUMBER OF DIFFERENTIAL EQUATIONS TO BE INTEGRATED
C XSO2 = FRACTION OF SO2 REMAINING IN THE GAS
C THE FOLLOWING VARIABLES EXIT THE SUBROUTINE:
C
C NZN = NEW NUMBER OF GRID POINTS
C ICN = NEW NUMBER OF SPLIT SPINE COEFFICIENTS
C VZN(I) = Z COORDINATE OF NEW GRID POINTS
C VXLN(I) = FRACTION OF LIME REMAINING AT NEW GRID POINTS
C *****
C DIMENSION VXSO2(1001),VZN(1001),VXLN(1001)
C COMMON /CONST1/ K1,K2,K3,CAG
C COMMON /CONST2/ VMC
C COMMON /CONST3/ H
C COMMON /CONST5/ NZ,VZ(200),VXLIME(200)
C COMMON /CONST6/ C(200,S),IC
C INTEGER METH,MITER,INDEX,IWK(2),IER,K,IC,NZ,N
C REAL K1,K2,K3,CAG,XLIME,H
C REAL VXSO2,Z,HZ,XSO2,ZEND,TOL,WK(35),VZ,C
C EXTERNAL FCN,FCNJ
C CALL THE INTERPOLATION ROUTINE ICSCCU TO DETERMINE THE
C SPLINE COEFFICIENTS C, FROM THE VXLIME(I) OF THE
C PREVIOUS TIME
C CALL ICSCCU(VZ,VXLIME,NZ,C,IC,IER)
C INITIALIZE VARIABLES FOR DGEAR
C N=1
C METH=2
C MITER=2

```

```

INDEX=1
TOL=1.0E-4
Z=0.0
ZMAX=1.0
XSO2=1.0
VZN(1)=0.0
VXSO2(1)=1.0
VXLN(1)=VXLIME(1)
HZ=VZ(2)-VZ(1)
ZGI=Z
ZEND=Z+HZ/100.0
H=(ZEND-ZGI)/1000.0
ZEGI=ZEND
TMPSO2=XSO2
IZ=1
DO 10 J=1,200
  IF (ABS(ZMAX-ZGI).LE.1.0E-6) THEN
    NZN=IZ
    ICN=IZ-1
    RETURN
  ENDIF
  IF (ZEGI.GE.ZMAX) THEN
    ZEGI=ZMAX
    ZEND=ZMAX
  ENDIF
  IF (XSO2.GT.1.0E-12) THEN
C    DGEAR IS CALLED TO PERFORM THE INTEGRATION
    CALL DGEAR(N,FCN,FCNJ,ZGI,H,XSO2,ZEGI,TOL,METH,MITER,INDEX,
&      IWK,WK,IER)
  ELSE
    INDEX=0
    IER=0
    H=0.05
    XSO2=0.0
  ENDIF
  IF (XSO2.LT.0.0) XSO2=0.0
C  STPCHG IS CALLED TO CHECK IF THE STEP SIZE USED FOR
C  DGEAR IS SMALL ENOUGH
  CALL STPCHG (Z,ZEND,H,INDEX,ZMAX)
  IF (INDEX.EQ.1) THEN
    ZEGI=ZEND
    ZGI=Z
    XSO2=TMPSO2
    H=H*.1
  ELSE
    TMPSO2=XSO2
    IZ=IZ+1
    VZN(IZ)=ZEND
    VXSO2(IZ)=XSO2
C  THE INTERPOLATION SUBROUTINE XINTER IS CALLED TO

```

```
C      DETERMINE THE FRACTION OF LIME AT THE NEW GRID
C      POINT, VXLN(I)
      CALL XINTER(VZ,VXLIME,NZ,C,IC,VZN(IZ),VXLN(IZ),IER)
      DELTZ=ZEND-Z
      Z=ZEND
      ZEND=Z+DELTZ
      ZGI=Z
      ZEGI=ZEND
      ENDIF
10  CONTINUE
      NZN=IZ
      ICN=IZ-1
      RETURN
      END
```

```

SUBROUTINE STPCHG(Z,ZEND,H,INDEX,ZMAX)
C *****
C THIS SUBROUTINE DETERMINE IF THE DIFFERENCE BETWEEN Z AND
C ZEND IS SMALL ENOUGH TO ENSURE AN ACCURATE INTEGRATION.
C THE CRITERIA USED IS THAT DELTZ = ZEND -Z MUST BE LESS THAN
C 5 TIMES BUT GREATER THAN 2 TIMES H, THE STEP SIZE USED
C FOR DGEAR.
C VARIABLES ENTERING THE SUBROUTINE ARE:
C
C Z = VALUE OF Z AT WHICH THE INTEGRATION IS STARTED
C ZEND = VALUE OF Z AT WHICH THE INTEGRATION END
C H = INTEGRATION STEP SIZE USED BY DGEAR
C INDEX = DGEAR PARAMETER EQUAL TO 1 FOR FIRST CALL TO
C DGEAR AND EQUAL TO 0 FOR OTHER CALLS.
C ZMAX = MAXIMUN POSSIBLE VALUE OF ZEND, REACTOR LENGTH
C VARIABLES USED INSIDE SUBROUTINE:
C
C DELTZ = ZEND - Z, INTEGRATION STEP SIZE
C VARIABLES LEAVING SUBROUTINE:
C
C ZEND = NEW VALUE FOR ENDING THE INTEGRATION OF DGEAR IF
C STEP SIZE WAS CHANGED, OTHERWISE THE SAME ENTERING
C VALUE
C INDEX = PARAMETER WITH VALUE 1 IF STEP SIZE WAS CHANGED
C AND VALUE 0 IF THE STEP SIZE WAS NOT CHANGED
C *****
INTEGER INDEX
REAL Z,ZEND,H,DELTZ
DELTZ=ZEND-Z
IF(DELTZ.GT.5.0*H) THEN
  ZEND=Z+DELTZ*0.7
  INDEX=1
ENDIF
IF (DELTZ.LT.(H*2.0).AND.(ZMAX-ZEND).GT.2.0E-6) THEN
  ZEND=Z+DELTZ*1.6
  INDEX=1
ENDIF
IF (ZEND.GE.ZMAX) ZEND=ZMAX
RETURN
END

```

```

SUBROUTINE FCN(N,Z,XSO2,DXSO2)
C *****
C THIS SUBROUTINE IS AN EXTERNAL FUNCTION OF DGEAR.
C IT CALCULATE THE DERIVATIVE DXSO2/DZ AT ANY POINT
C Z ALONG THE REACTOR.
C THIS SUBROUTINE IN TURN CALL THE SUBROUTINE XINTER THAT
C DETERMINE THE VALUE OF VXLIME AT THE GIVEN Z.
C VARIABLES ENTERING THE SUBROUTINE ARE:
C
C N = NUMBER OF DIFFERENTIAL EQUATIONS TO BE SOLVED
C BY DGEAR
C Z = Z COORDINATE ALONG THE REACTOR
C XSO2 = FRACTION OF SO2 REMAINING IN THE GAS
C VARIABLES ENTERING THE SUBROUTINE BY COMMON BLOCKS:
C
C K1 = CONSTANT FOR DIFFUSION OF SO2 THROUGH ASH LAYER
C K2 = CONSTANT FOR CHEMICAL REACTION
C K3 = CONSTANT FOR DIFFUSION OF SO2 THROUGH THE GAS FILM
C CAG = SO2 CONCENTRATION ENTERING THE REACTOR
C VMC = VOLUMETRIC NITROGEN FLOW RATE (CC/SEC)
C NZ = NUMBER OF GRID POINT AT WHICH VXLIME IS KNOWN FROM
C PREVIOUS INTEGRATION
C VZ(I) = Z COORDINATE OF GRID POINT AT WHICH VXLIME IS
C KNOWN
C VXLIME(I) = VALUES OF FRACTION OF LIME AT GRID POINTS,
C KNOWN FROM PREVIOUS INTEGRATION
C C(I,J) = SPLINE COEFFICIENTS DETERMINED FOR VXLIME BY THE
C IMSL INTERPOLATION ROUTINE ICSCCU
C IC = NZ-1, ONE OF THE DIMENSIONS OF THE SPLINE COEFFICIENTS
C MATRIX
C VARIABLES USED INSIDE THE SUBROUTINE:
C
C XINT = FRACTION OF LIME AT Z, INTERPOLATED BY XINTER
C VARIABLES EXITING THE SUBROUTINE:
C
C DXSO2 = DERIVATIVE OF XSO2 WITH RESPECT TO DISTANCE, AT Z
C *****
C
C INTEGER N,IER,NZ,IC
C REAL Z,XSO2(N),DXSO2(N),K1,K2,K3,CAG,VMC
C REAL VZ,VXLIME,C,XINT,H
C COMMON /CONST1/ K1,K2,K3,CAG
C COMMON /CONST2/ VMC
C COMMON /CONST3/ H
C COMMON /CONST5/ NZ,VZ(200),VXLIME(200)
C COMMON /CONST6/ C(200,3),IC
C CALL XINTER(VZ,VXLIME,NZ,C,IC,Z,XINT,IER)
C AREAF=(1.0+EXP(13.428*XINT-10.7424))/15.667
C RATE1=K2*AREAF*XINT**(2./3.)
C ALFA=(XINT**(-1./3.)-1.0)/(K1*SQRT(AREAF))
C RATE2=CAG*XSO2(1)/(ALFA+(1./K3))

```

```
IF(RATE2.LT.RATE1) THEN
  DXSO2(1)=-.(1./(VMC*CAG))*RATE2
ELSE
  DXSO2(1)=-.(1./(VMC*CAG))*RATE1
ENDIF
RETURN
END
```

```
SUBROUTINE FCNJ(N,Z,XSO2,PD)
```

```
*****
```

```
C THIS SUBROUTINE ESTIMATE THE PARTIAL DERIVATIVES OF XSO2.
C NOT NEEDED IN OUR PROBLEM, SO A DUMMY SUBROUTINE WILL BE
C USED.
```

```
*****
```

```
INTEGER N
REAL XSO2(N),PD(N,N),Z
RETURN
END
```

```

SUBROUTINE XINTER(VZ,VXLIME,NZ,C,IC,ZINT,XINT,IER)
C *****
C THIS SUBROUTINE PROVIDE AN INTERPOLATED VALUE OF VXLIME
C AT ANY GIVEN VALUE VALUE OF Z
C THE VARIABLES ENTERING THE SUBROUTINE ARE:
C VZ = VECTOR OF DISTANCES ALONG THE REACTOR WERE XLIME IS
C AVAILABLE
C VXLIME = FRACTION OF LIME REMAINING AT ANY GIVEN VZ
C NZ = NUMBER OF GRID POINTS IN THE Z DIRECTION
C IC = NZ-1
C C = SPLINE COEFFICIENTS DETERMINED BY THE INTERPOLATION
C ROUTINE ICSCCU. C IS A MATRIX OF NZ-1 BY 3
C ZINT = VALUE OF Z WERE THE VXLIME IS DESIRED
C THE OUTPUT OF THE PROGRAM ARE:
C XINT = VALUE OF FRACTION OF LIME REMAINING AT Z = ZINT
C IER = ERROR PARAMETER
C *****
INTEGER NZ,IC,IER,ISAV
REAL VZ(NZ),C(IC,3),VXLIME(NZ),ZINT,XINT,D
ISAV=0
DO 10 I=1,NZ-1
IF((VZ(I).LE.ZINT).AND.(ZINT.LT.VZ(I+1))) THEN
ISAV=I
GO TO 20
ENDIF
10 CONTINUE
20 CONTINUE
IF (ZINT.EQ.VZ(NZ)) ISAV=NZ-1
IF (ISAV.EQ.0) THEN
IER=60
IF (ZINT.GE.VZ(NZ)) ISAV=NZ-1
IF (ZINT.LT.0.0) ISAV=1
DSLPL=(VXLIME(ISAV+1)-VXLIME(ISAV))/(VZ(ISAV+1)-VZ(ISAV))
XINT=VXLIME(ISAV+1)+DSLPL*(ZINT-VZ(ISAV+1))
ELSE
IER=0
D=ZINT-VZ(ISAV)
XINT=((C(ISAV,3)*D+C(ISAV,2))*D+C(ISAV,1))*D+VXLIME(ISAV)
ENDIF
IF (XINT.LT.0.0) XINT=0.0
IF (XINT.GT.1.0) XINT=1.0
RETURN
END

```

```

SUBROUTINE INTEGT(TINI,TEND,VXLN,DELTT,INDEX,IER)
C *****
C THIS SUBROUTINE USE DGEAR TO INTEGRATE THE FRACTION
C OF LIME REMAINING IN THE REACTOR AT TIME TEND, FOR
C ALL GRID POINTS GIVEN THE FRACTION OF LIME REMAINING
C AT EACH POINT AT TIME TINI.
C
C THE VARIABLES ENTERING THE SUBROUTINE ARE:
C TINI      = INITIAL TIME OF THE INTEGRATION
C TEND      = FINAL TIME OF THE INTEGRATION (SEC)
C
C VARIABLES ENTERING THROUGH COMMON BLOCK ARE:
C NZ        = NUMBER OF POINT IN THE GRID
C VZ(I)     = Z COORDINATE FOR ALL GRID POINTS
C VXLIME(I) = FRACTION OF LIME REMAINING AT EACH GRID POINT
C           AT TIME TINI
C VXSO2(I)  = FRACTION OF SO2 REMAINING IN THE GAS AT EACH
C           GRID POINT
C K1        = CONSTANT FOR THE DIFFUSION OF SO2 THROUGH THE
C           ASH LAYER
C K2        = CONSTANT FOR THE CHEMICAL REACTION
C K3        = CONSTANT FOR DIFFUSION OF SO2 THROUGH THE GAS
C           FILM
C CAG       = SO2 CONCENTRATION ENTERING THE REACTOR
C NB       = MOLES OF LIME PLACED IN REACTOR
C           SURFACE
C
C VARIABLES EXITING THE SUBROUTINE ARE:
C VXLN(I)   = FRACTION OF LIME AT EACH GRID POINT AT TIME TEND
C DELTT     = TIME STEP SIZE FROM DGEAR
C IER       = ERROR PARAMETER FROM DGEAR
C *****
C DIMENSION VXLN(200),IWK(200),WK(3420)
C COMMON /CONST1/ K1,K2,K3,CAG
C COMMON /CONST4/ NB
C COMMON /CONST5/ NZ,VZ(200),VXLIME(200)
C COMMON /CONST6/ C(200,3),IC
C COMMON /CONST7/ VXSO2(200)
C EXTERNAL FTN,FTNJ
C INTEGER NZ,METH,MITER,INDEX,IER,IWK
C REAL TINI,TEND,DELTT,TOL,CAG,NB
C REAL VZ,VXSO2,VXLIME,VXLN,K1,K2,K3
C REAL WK
C DO 10 I=1,NZ
C VXLN(I)=VXLIME(I)
10 CONTINUE
C INITIALIZE VARIABLES IN DGEAR
C N=NZ
C METH=1
C MITER=0

```

```
INDEX=1
TOL=1.0E-6
DELTT=(TEND-TINI)/10.0
CALL DGEAR(N,FTN,FTNJ,TINI,DELTT,VXLN,TEND,TOL,METH,MITER,
&INDEX,IWK,WK,IER)
RETURN
END
```

```

SUBROUTINE FTN(N,TINI,VXLN,DXLIME)
C *****
C THIS SUBROUTINE IS CALLED BY DGEAR IN THE TIME INTEGRATION
C IT CALCULATE THE DERIVATIVE OF XLIME WITH RESPECT TO TIME
C FOR EVERY GRID POINT.
C *****
COMMON /CONST1/ K1,K2,K3,CAG
COMMON /CONST4/ NB
COMMON /CONST5/ NZ,VZ(200),VXLIME(200)
COMMON /CONST6/ C(200,3),IC
COMMON /CONST7/ VXSO2(200)
INTEGER IER
REAL TINI,VXLN(200),DXLIME(200),K1,K2,K3,CAG,NB,VXSO2
DO 10 I=1,N
  AREAF=(1.0+EXP(13.428*VXLN(I)-10.7424))/15.667
  RATE1=K2*AREAF*VXLN(I)**(2./3.)
  ALFA=(VXLN(I)**(-1./3.)-1.0)/(K1*SQRT(AREAF))
  RATE2=CAG*VXSO2(I)/(ALFA+(1./K3))
  IF(RATE2.LT.RATE1) THEN
    DXLIME(I)=-(.1./NB)*RATE2
  ELSE
    DXLIME(I)=-(.1./NB)*RATE1
  ENDIF
10 CONTINUE
RETURN
END

SUBROUTINE FTNJ(N,TINI,VXLN,PD)
C *****
C THIS SUBROUTINE IS CALLED BY DGEAR IN THE INTEGRATION
C IN TIME IT ESTIMATE THE PARTIAL DERIVATIVES OF XLIME
C WITH RESPECT TO TIME. NOT NEEDED IN OUR CASE, SO A
C DUMMY SUBROUTINE WILL BE USED.
C *****
REAL TINI,VXLN(200),PD(200,200)
INTEGER N
RETURN
END

```

```

SUBROUTINE STPCHT(T,TEND,DELTT,INDEX,TPRINT)
C *****
C THIS SUBROUTINE DETERMINE IF THE DIFFERENCE BETWEEN T AND
C TEND IS SMALL ENOUGH TO ENSURE AN ACCURATE INTEGRATION.
C THE CRITERIA USED IS THAT DELTA = TEND - T MUST BE LESS
C THAN 3 TIMES BUT GREATER THAN 1 TIMES DELTT, THE STEP
C SIZE USED FOR DGEAR.
C VARIABLES ENTERING THE SUBROUTINE ARE:
C
C T = VALUE OF T AT WHICH THE INTEGRATION IS STARTED
C TEND = VALUE OF T AT WHICH THE INTEGRATION END
C DELTT = INTEGRATION STEP SIZE USED BY DGEAR
C INDEX = DGEAR PARAMETER EQUAL TO 1 FOR FIRST CALL TO
C DGEAR AND EQUAL TO 0 FOR OTHER CALLS.
C TPRINT = MAXIMUM POSSIBLE VALUE OF TEND
C VARIABLES USED INSIDE SUBROUTINE:
C
C DELTA = TEND - T, INTEGRATION STEP SIZE
C VARIABLES LEAVING SUBROUTINE:
C
C TEND = NEW VALUE FOR ENDING THE INTEGRATION OF DGEAR IF
C STEP SIZE WAS CHANGED, OTHERWISE THE SAME ENTERING
C VALUE
C INDEX = PARAMETER WITH VALUE 1 IF STEP SIZE WAS CHANGED
C AND VALUE 0 IF THE STEP SIZE WAS NOT CHANGED
C *****
INTEGER INDEX
REAL T,TEND,DELTT,DELTA
DELTA=TEND-T
IF(DELTA.GT.3.0*DELTT) THEN
  TEND=T+DELTA*0.7
  INDEX=1
ENDIF
IF (DELTA.LT.(DELTT).AND.(TPRINT-TEND).GT.1.0E-6) THEN
  TEND=T+DELTA*1.7
  INDEX=1
ENDIF
IF (TEND.GE.TPRINT) TEND=TPRINT
RETURN
END

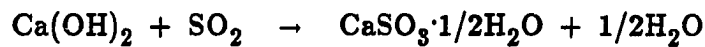
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**Appendix D.**

**Sample Calculation for Lime Conversion**

The raw data from the experiments is concentration of  $\text{SO}_2$  leaving the reactor vs time. Figure D-1 shows the raw data obtained for Experiment 132, run at 74% RH, 64.4°C, using 1.0 g lime A with 10 mole%  $\text{NaNO}_2$  as additive.

The  $\text{SO}_2$  reacts with  $\text{Ca}(\text{OH})_2$  according to the reaction:



The fraction of  $\text{Ca}(\text{OH})_2$  converted,  $x_{\text{lime}}$  is given by;

$$x_{\text{lime}} = \frac{\text{gmol Ca}(\text{OH})_2 \text{ reacted}}{\text{initial moles of Ca}(\text{OH})_2} \quad (\text{D.1})$$

For each mol of  $\text{SO}_2$  removed 1 mol of  $\text{Ca}(\text{OH})_2$  will react, so Equation (D.1) can also be written as:

$$x_{\text{lime}} = \frac{\text{gmol SO}_2 \text{ removed}}{\text{initial moles of Ca}(\text{OH})_2} \quad (\text{D.2})$$

the initial moles of  $\text{Ca}(\text{OH})_2$  can be calculated as;

$$\text{initial gmol Ca}(\text{OH})_2 = \frac{m}{\text{MW of Ca}(\text{OH})_2} \quad (\text{D.3})$$

$m$  being the amount of  $\text{Ca}(\text{OH})_2$  in the reactor in grams.

The amount of  $\text{SO}_2$  removed can be obtained from a mass balance in the reactor as;

$$\text{gmol SO}_2 \text{ removed} = \int_0^t (C_{\text{SO}_2, \text{in}} - C_{\text{SO}_2, \text{out}}) v_m dt \quad (\text{D.4})$$

Where:

$$C_{\text{SO}_2, \text{in}} = \text{concentration SO}_2 \text{ entering reactor (gmol/cm}^3\text{)}$$

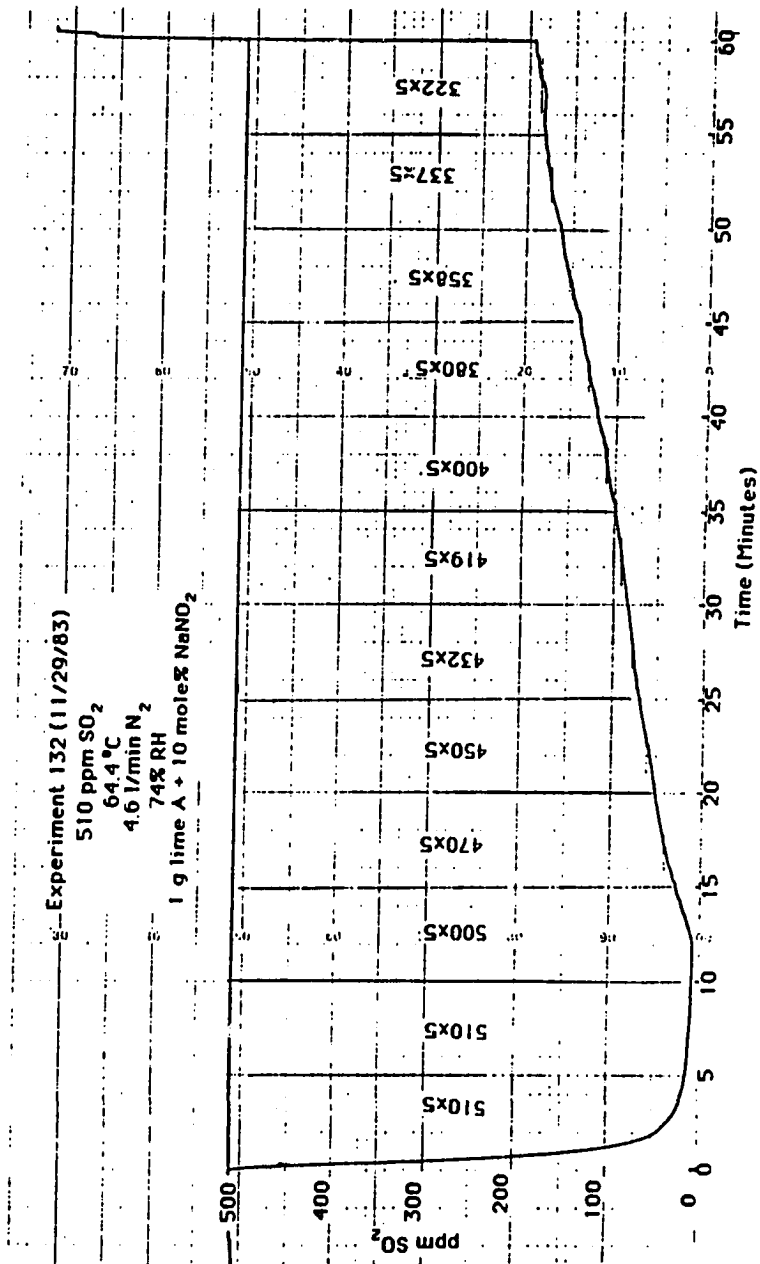


Figure D-1: Raw Data from Experiment 132

$C_{\text{SO}_2, \text{out}}$  = concentration  $\text{SO}_2$  leaving reactor ( $\text{gmol}/\text{cm}^3$ )

$v_m$  = volumetric flow rate of gas ( $\text{cm}^3/\text{minutes}$ )

$t$  = time (minutes)

Assuming the gas phase behaves as an ideal gas, the  $\text{SO}_2$  concentration can be expressed as;

$$C_{\text{SO}_2} = \frac{P_{\text{SO}_2}}{R T} = \frac{P x_{\text{SO}_2}}{R T} \quad (D.5)$$

Where:

$P_{\text{SO}_2}$  = partial pressure of  $\text{SO}_2$  (atm)

$P$  = total pressure (atm)

$R$  = gas constant ( $\text{atm cm}_3/\text{gmol K}$ )

$T$  = temperature (K)

$x_{\text{SO}_2}$  = mole fraction of  $\text{SO}_2 = \text{ppm SO}_2/10^6$

Substituting Equations (D.3) and (D.5) in Equation (D.4) we get:

$$x_{\text{lime}} = \frac{P v_m}{R T m} \int_0^t (x_{\text{SO}_2, \text{in}} - x_{\text{SO}_2, \text{out}}) dt \quad (D.6)$$

The integral is given by the area  $A_t$  between the data curve in Figure D-1 and the horizontal line corresponding to the inlet  $\text{SO}_2$  concentration.  $A_t$  has to be multiplied by  $10^{-6}$  to convert ppm to mole fraction.

After substituting:

$$P = 1 \text{ atm}$$

$$T = 273 \text{ K}$$

$$v_m = 4600 \text{ cm}^3/\text{min}$$

$$m = 1 \text{ g}$$

$$\text{MW} = 74.1$$

We finally get

$$\text{Ca(OH)}_2 \text{ Converted (\%)} = 1.573 \cdot 10^{-3} A_t$$

Integrating graphically the area  $A_t$ , the values of lime conversion shown in Table D-1 are obtained.

**Table D-1:** Conversion of  $\text{Ca}(\text{OH})_2$  versus reaction time  
Experiment 132

74% RH, 64.4°C, 4.6 l/min  $\text{N}_2$ , 1 g lime A, 10 mole%  $\text{NaNO}_2$

Time (minutes)	$\text{Ca}(\text{OH})_2$ Converted (%)
5	4.0
10	8.0
15	12.0
20	15.7
25	19.2
30	22.6
35	25.9
40	29.0
45	32.0
50	34.8
55	37.5
60	40.0

**Appendix E.**

**Error Analysis**

-

The experimental results were presented as  $\text{Ca(OH)}_2$  conversion.  $\text{Ca(OH)}_2$  conversion was determined by a gas phase material balance (explained in detail in Appendix D) and solids analysis. The main uncertainties in the calculation of  $\text{Ca(OH)}_2$  conversion by gas phase material balance are the gas flowrate and the  $\text{SO}_2$  concentration. The gas flowrate was measured with 2% precision and 5% accuracy by a rotameter (LabCrest Century) calibrated with a wet testmeter. The  $\text{SO}_2$  concentration was measured with 1% precision and 5% accuracy using a Thermolectron pulsed fluorescent  $\text{SO}_2$  analyzer calibrated weekly with a  $\text{SO}_2/\text{N}_2$  standard gas ( $\pm 2\%$ ). With relatively large amounts of  $\text{Ca(OH)}_2$  (1 g or more) giving high  $\text{SO}_2$  removal, conversion will be calculated with 3% precision and 10% accuracy. With smaller amounts of  $\text{Ca(OH)}_2$  and reduced  $\text{SO}_2$  removal (differential experiments), taking the difference in  $\text{SO}_2$  concentration before and after the reactor introduces larger errors. Therefore,  $\text{Ca(OH)}_2$  conversion in differential experiments can only be determined by solids analysis.

The chemical analysis was performed by combined iodometric and acid/base titration. The analysis was made with the entire amount of products solids, so selective sampling was not a problem. It determines total sulfite and total free  $\text{Ca(OH)}_2$ . The conversion is calculated assuming there is no  $\text{CaSO}_4$  formed. The precision of the method should be better than 5%. The accuracy will depend on side reactions such as oxidation that will cause conversion to be underpredicted. Using  $\text{O}_2$  free nitrogen oxidation should not be important and in this case an accuracy of 10% can be expected.

$\text{Ca(OH)}_2$  conversion is a strong function of relative humidity. relative humidity was calculated from the water and  $\text{N}_2$  flowrates and

the temperature. The water was injected with a calibrated Sage syringe pump with 2% precision and 5% accuracy. The N<sub>2</sub> flowrate was measured with 2% precision and 5% accuracy. The calculated relative humidity has a precision of about 4% and an accuracy of 10%.

During actual operation of the apparatus, when multiple experiments at identical conditions were performed, the deviation from the average was below  $\pm 8\%$ . The maximum deviation between experiments was below 15%.

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