## ME 386P-2: Mechanical Behavior of Materials

Dislocations Handout
Date: February 27, 2014

Practice Problem: Consider an array of edge dislocations in an FCC metal forming the hexagonal array shown below. The sense, $\hat{\xi}_{i}$, and Burgers, $\vec{b}_{i}$, vectors at one node are given for two dislocations. Calculate the sense and Burgers vectors of the third dislcoation at that node. What type of dislocations are these? In what crystallographic plane do these dislocation lie?


## Edge Dislocation in an FCC Lattice



Will the full dislocation $b_{1}$ decompose into two partial dislocations, $b_{2}$ and $b_{3}$ ? Use Frank's rule to answer this question. What are the ramifications of the full dislocation potentially decomposing into partial dislocations?

## Stress Field about an Edge Dislcoation



In polar coordinates:

$$
\begin{aligned}
\sigma_{r r}=\sigma_{\theta \theta} & =-\frac{G b}{2 \pi(1-v)} \frac{\sin \theta}{r} \\
\sigma_{r \theta} & =\frac{G b}{2 \pi(1-v)} \frac{\cos \theta}{r}
\end{aligned}
$$

In Cartesian coordinates:

$$
\begin{aligned}
\sigma_{x x} & =-\frac{G b}{2 \pi(1-v)} \frac{y\left(3 x^{2}+y^{2}\right)}{\left(x^{2}+y^{2}\right)^{2}} \\
\sigma_{y y} & =\frac{G b}{2 \pi(1-v)} \frac{y\left(x^{2}-y^{2}\right)}{\left(x^{2}+y^{2}\right)^{2}} \\
\tau_{x y} & =\frac{G b}{2 \pi(1-v)} \frac{x\left(x^{2}-y^{2}\right)}{\left(x^{2}+y^{2}\right)^{2}} \\
\sigma_{z z} & =v\left(\sigma_{x x}+\sigma_{y y}\right)
\end{aligned}
$$

and $\tau_{x z}=\tau_{y z}=0$.

Examples: D. Hull and D. J. Bacon, Introduction to Dislocations, Fourth Edition (ButterworthHeinemann, Oxford) 2001.


(a)

(b)

(c)

(d)
(e)

A Frank-Read dislocation source

