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1  #-----
2  # Name:      Markov Chain Land Cover Change Model
3  # Purpose:   Simple explanation of model with two land cover states
4  #
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6  #
7  # Created:   07/03/2017
8  # Copyright: (c) ea9267 2017
9  # Licence:   <your licence>
10 # Modifications:
11 #
12 #-----
13 # Import system modules
14 import sys, string, os
15 import numpy as np
16 import matplotlib.pyplot as plt
17 #suppose you have only two states, forest and deforested
18 # the transition matrix probability is
19 tmp = np.array([0.8, 0.2, 0.1, 0.9]).reshape(2,2)
20 print(tmp)
21 # probability of forest --> remain forest = 0.8
22 # probability of forest --> deforest = 0.2
23 # probability of deforest --> regrowth back to forest = 0.1
24 # probability of deforest --> remain deforest = 0.9
25 # Suppose initial state is forest
26 lc0 = np.array([[1.0,0]])
27 #python: the double square brackets forces the array to be 2D instead of
28 # a 1D array (important later on when we concatenate arrays)
29
30 # What is the probability of forest or deforested after 3 periods?
31
32 # Can calculate in two ways.
33 # 1) As a Markov Chain
34 #  $p(t) = f(p(t-1))$ 
35 lc1 = np.dot(lc0, tmp)
36 lc2 = np.dot(lc1, tmp)
37 lc3 = np.dot(lc2, tmp)
38 print(lc3)
39
40 # 2) As matrix exponentiation
41 tmp2 = np.dot(np.dot(tmp, tmp), tmp)
42 lc3_2 = np.dot(lc0,tmp2)
43 print(lc3_2)
44
45 #Both return the same result after three periods
46 # Probability of forest = 0.562
47 # probability of deforested = 0.438
48
49 tmp_0 = tmp
50 # Convergence, steady state
51 # run the same MC for a long time
52 #Let's also store the probabilities in an array lcprob
53 lcprob = lc0
54 for t in range(1,30):

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55     tmp_f = np.dot(tmp_0, tmp)
56     tmp_prob = np.dot(lc0, tmp_f)
57     lc_prob = np.concatenate((lc_prob, tmp_prob), axis=0)
58     tmp_0 = tmp_f
59
60     # Steady state probability
61     lc_f = np.dot(lc0, tmp_f)
62     print("Probability remain forested: {:.4f}".format(lc_f[0][0]))
63     print("Probability deforested: {:.4f}".format(lc_f[0][1]))
64     # 1/3 chance it will be forest
65     # 2/3 chance it will deforested
66
67     # plot steady state convergence
68     t = np.arange(1, 31)
69
70     plt.plot(t, lc_prob[:,0], 'g:', label = "Forested", marker = 'o')
71     plt.plot(t, lc_prob[:,1], 'b-', label = "Deforested", marker = 'x')
72     plt.xlabel('Time')
73     plt.ylabel('Probability')
74     plt.xlim(1, 30)
75     plt.ylim(0, 1)
76     plt.legend(loc=1, prop={'size':11})
77     plt.title('Steady State Land Cover Probabilities')
78     plt.show()

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